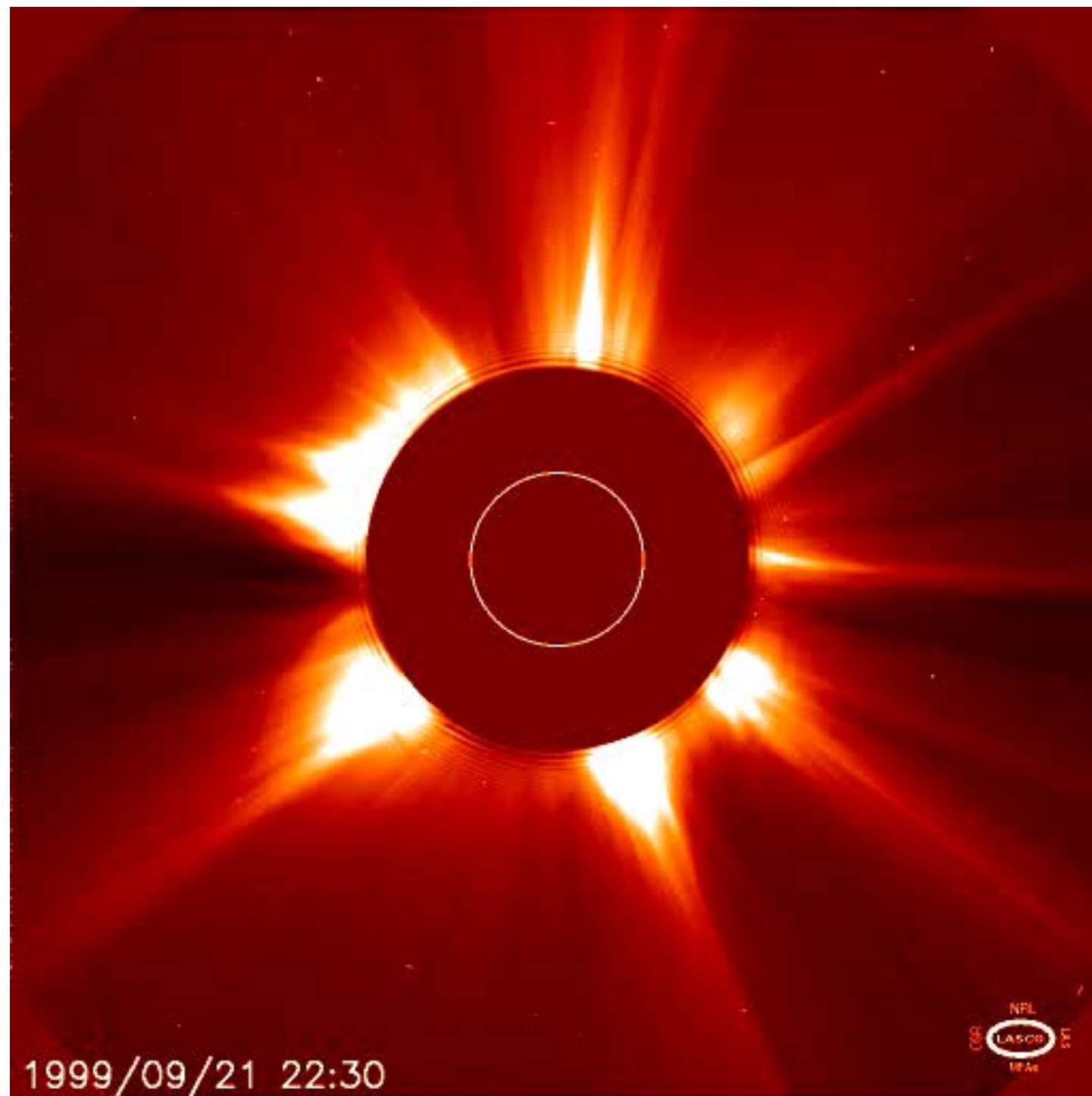


計算科学が拓く世界
地球・惑星・宇宙と計算科学2
宇宙プラズマ粒子シミュレーション

大村善治

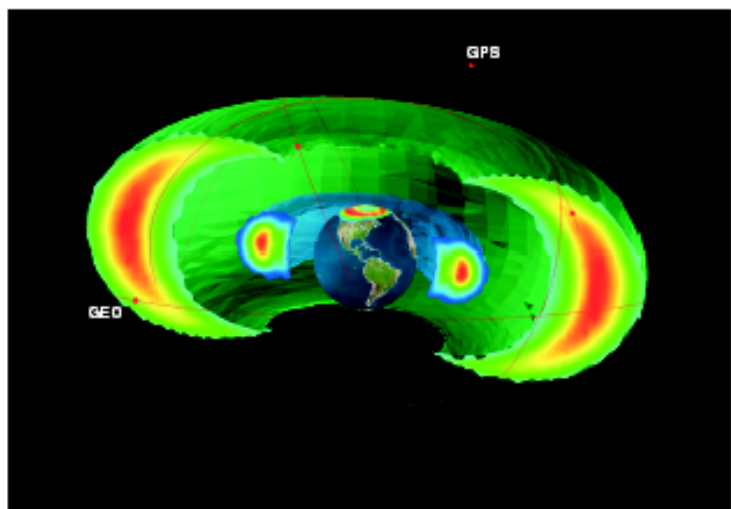
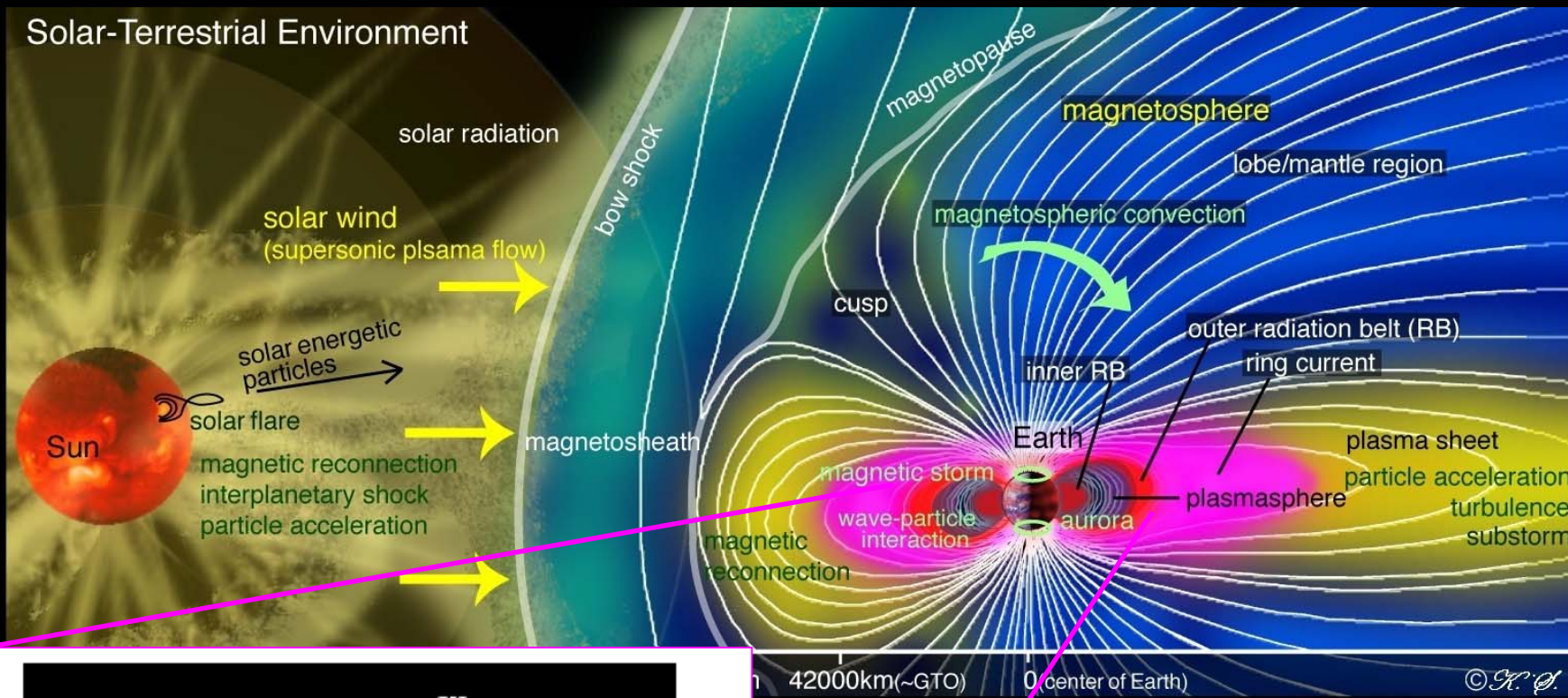
京都大学生存圏研究所,
omura@rish.kyoto-u.ac.jp

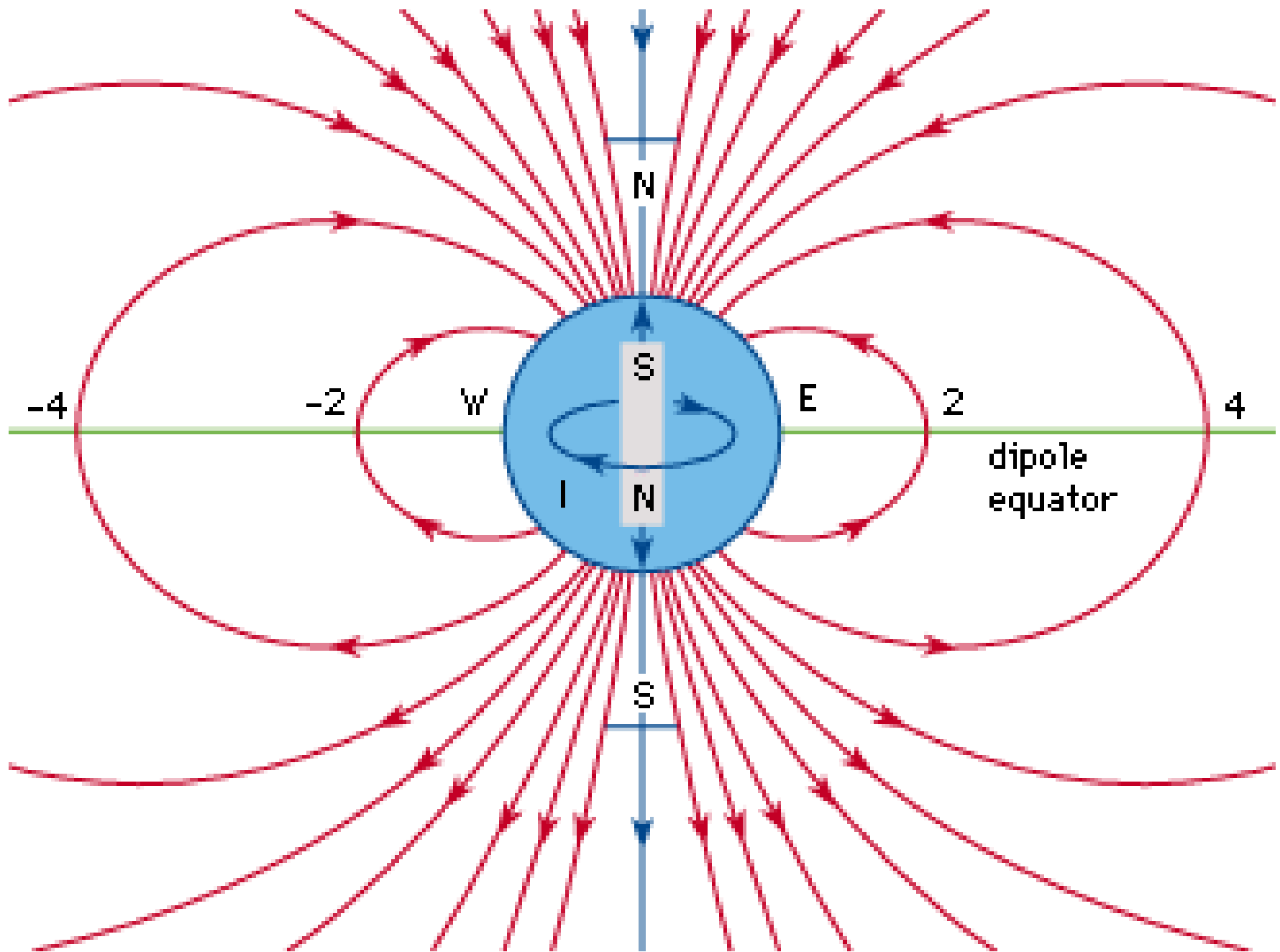
太陽風



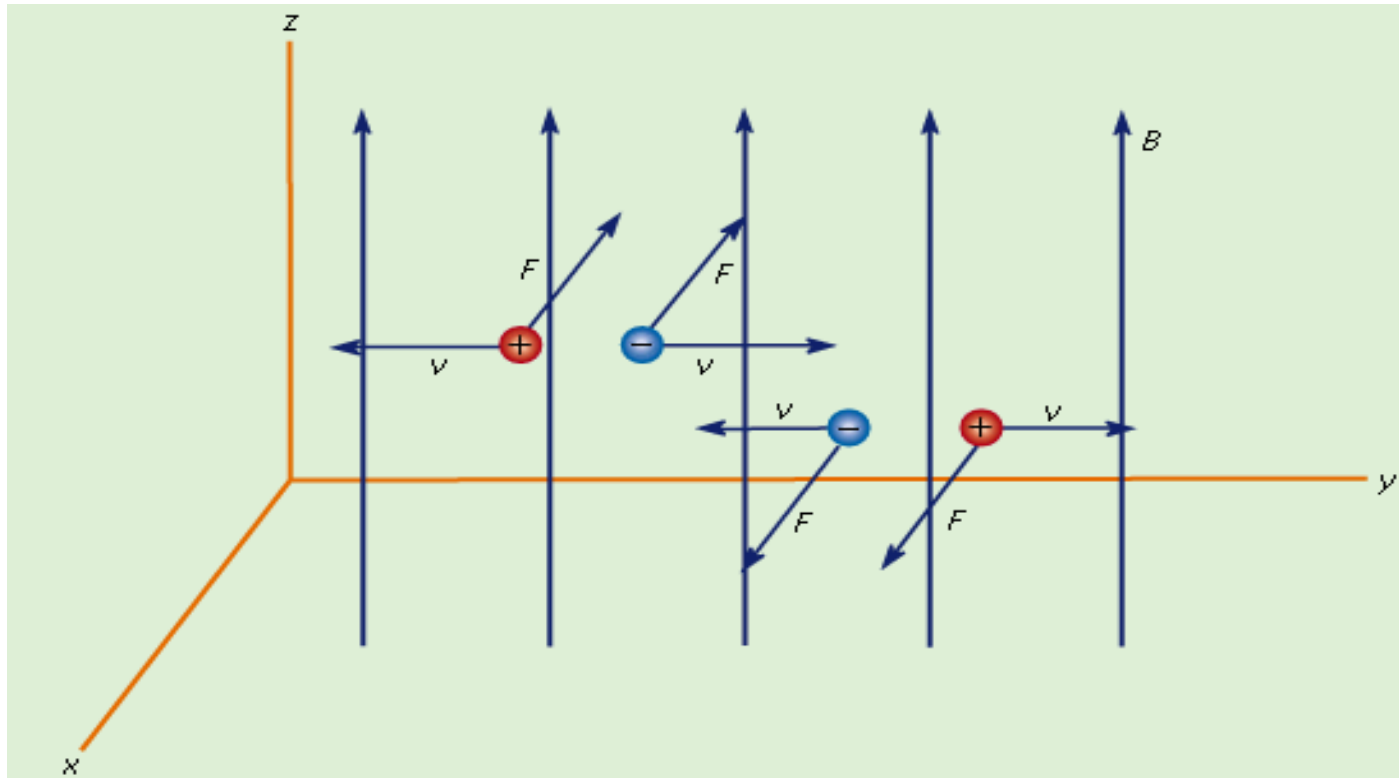
Geospace

Solar-Terrestrial Environment





Motion of Charged Particles (Lorentz Force)

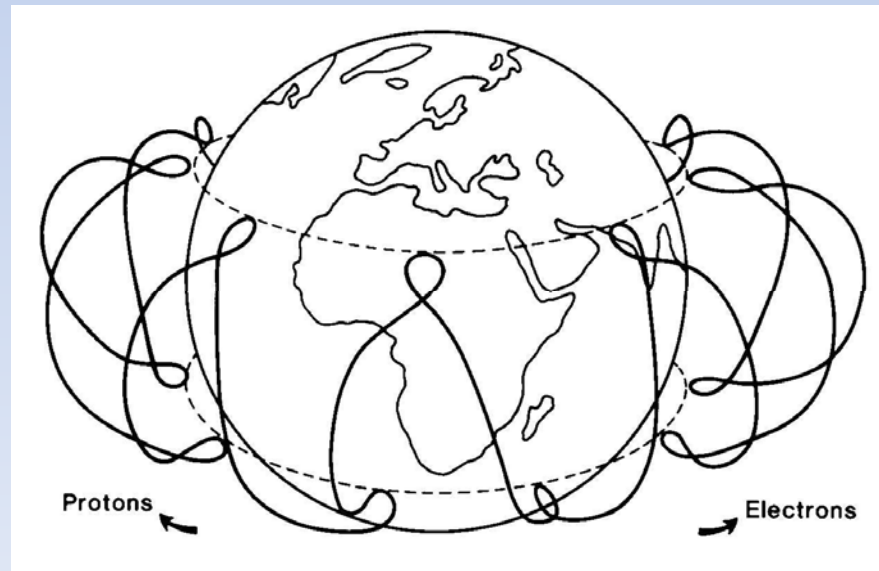
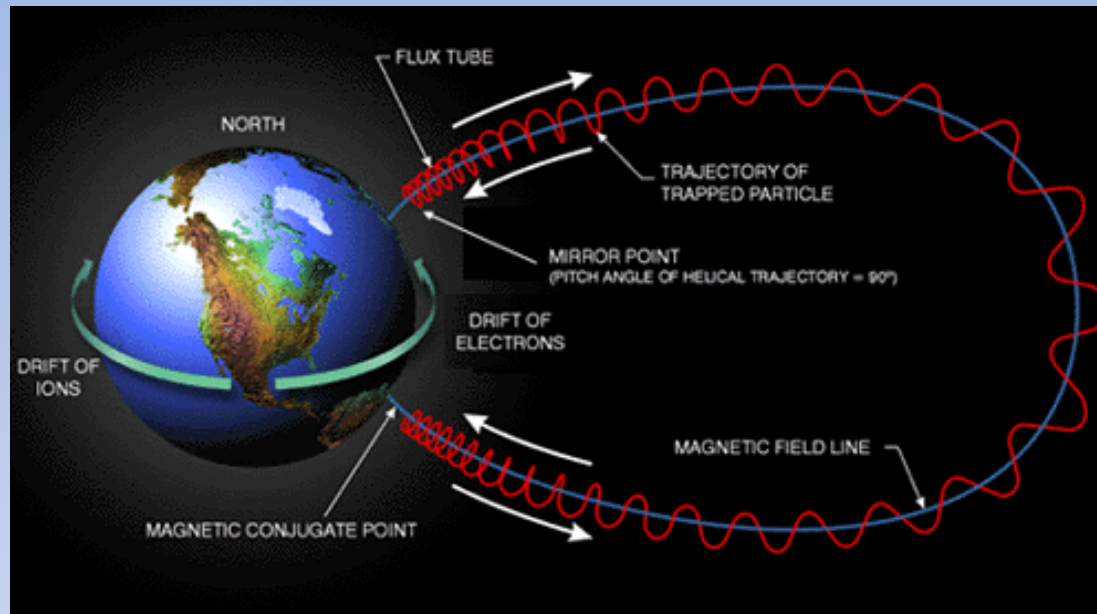


Equation of Motion of Relativistic Electrons

$$m_0 \frac{d(\gamma \mathbf{v})}{dt} = -e[\mathbf{E}_w + \mathbf{v} \times (\mathbf{B}_0 + \mathbf{B}_w)]$$

$$\gamma = \frac{1}{\sqrt{1 - (v/c)^2}}$$

Motion of Charged Particles in Dipole Magnetic Field

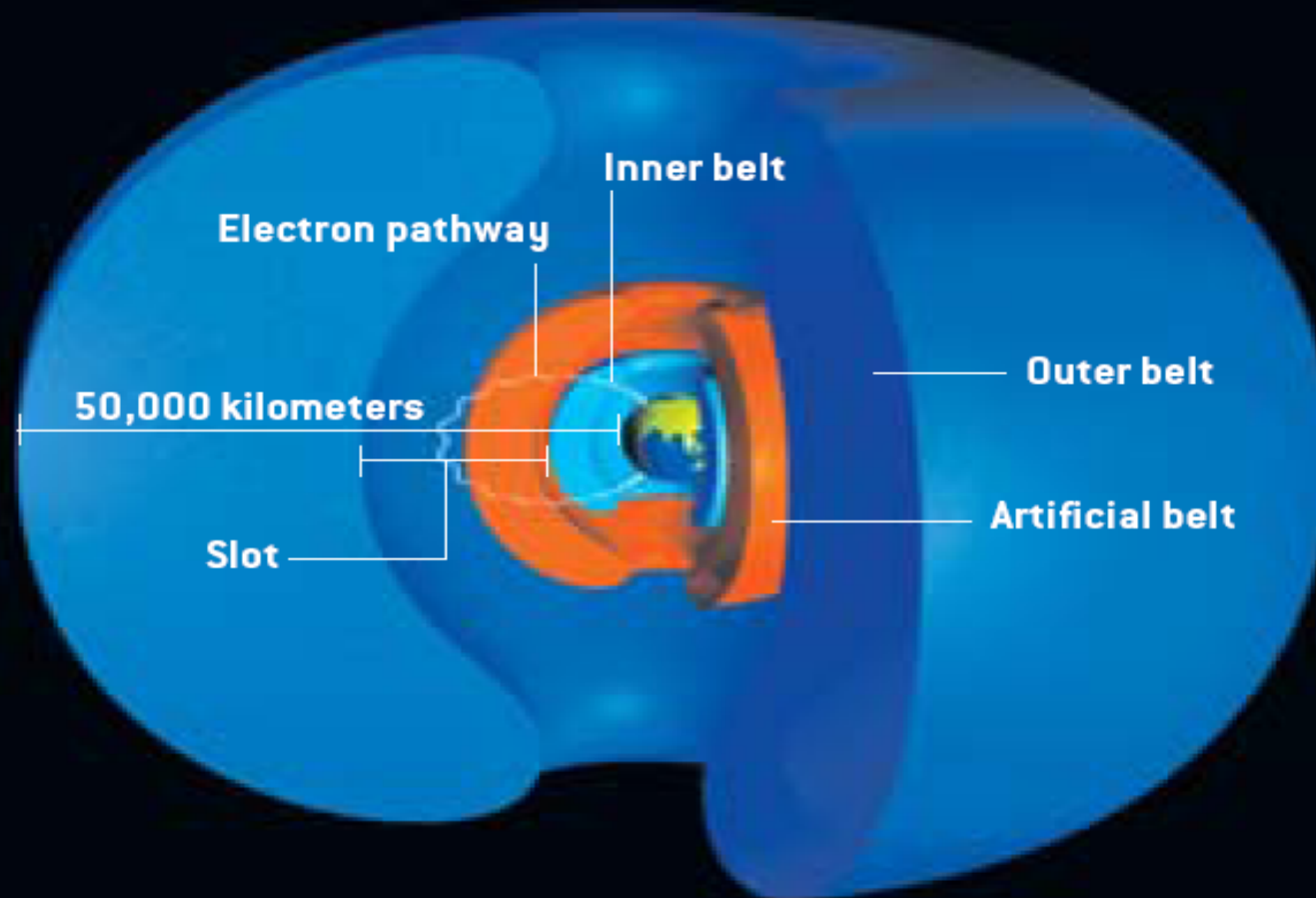
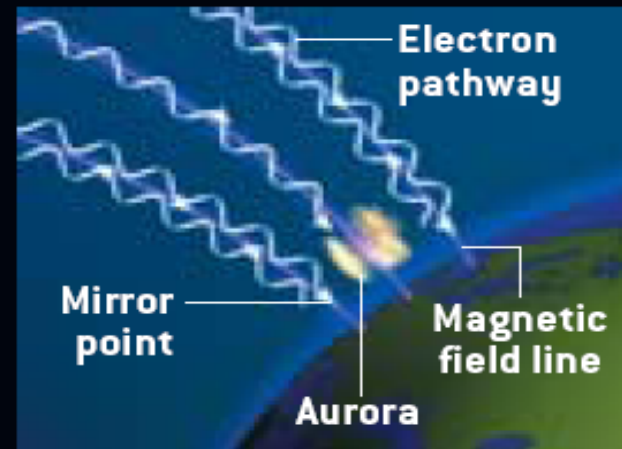


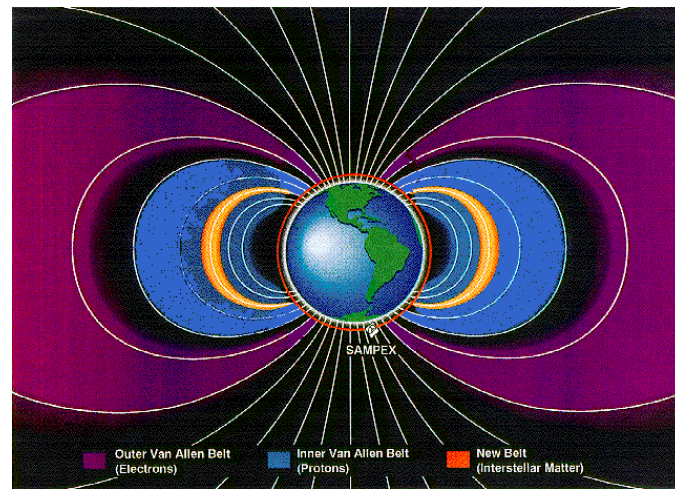
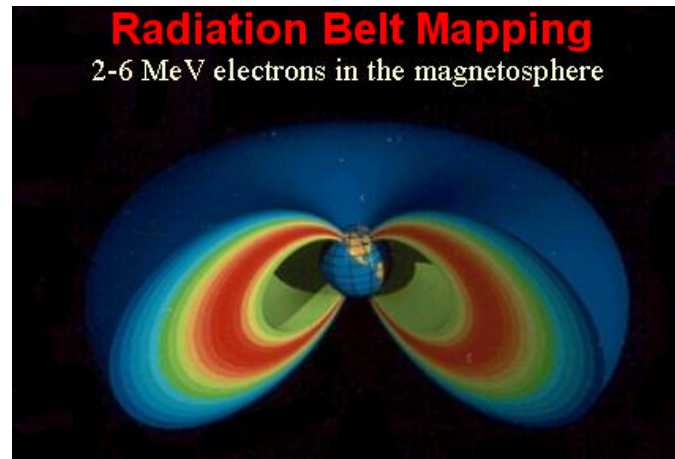
VAN ALLEN RADIATION BELTS

Inner electron belt:
600 to 5,000 kilometers

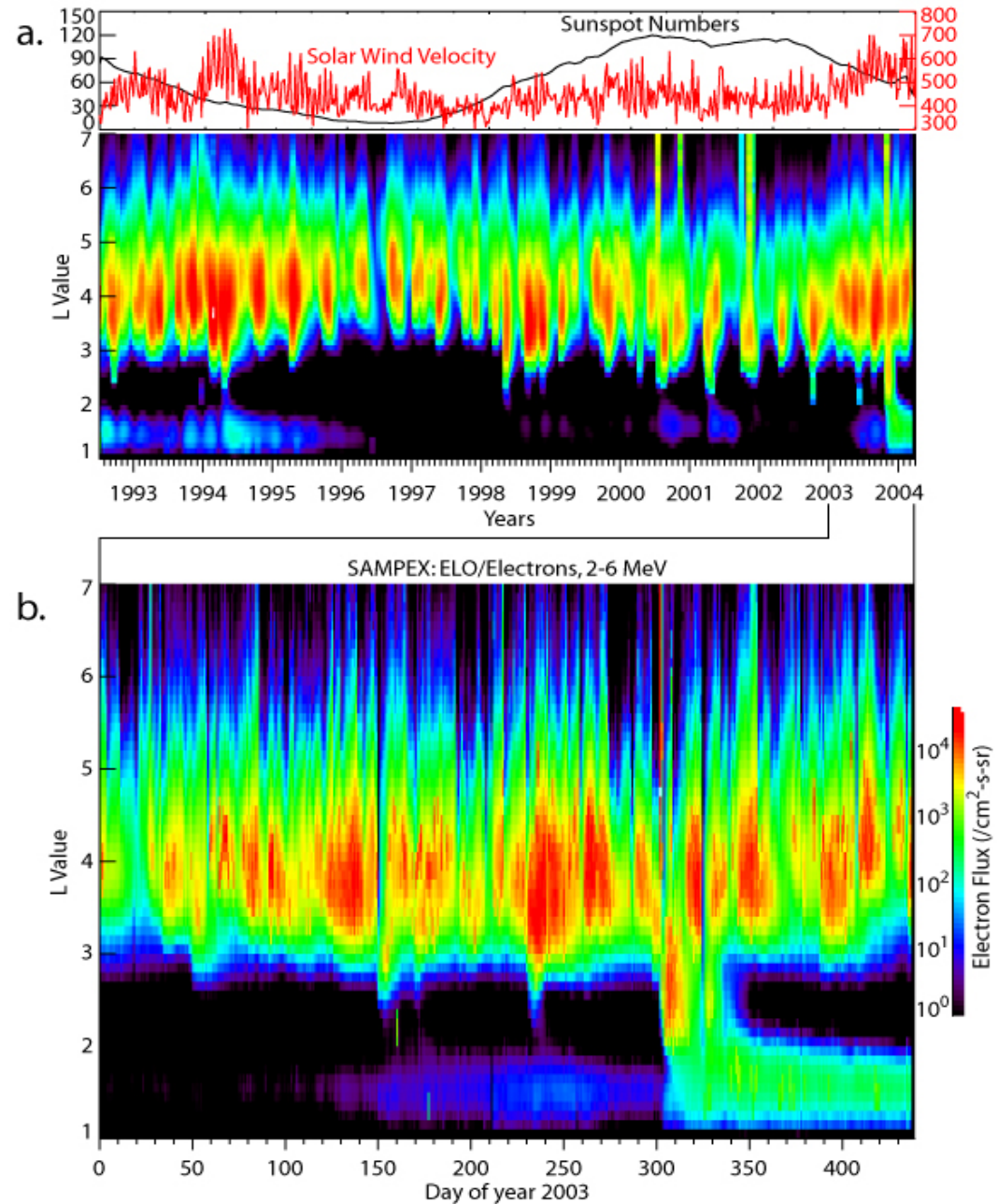
Slot (safety zone):
6,000 to 12,000 kilometers

Outer electron belt:
20,000 to 50,000 kilometers

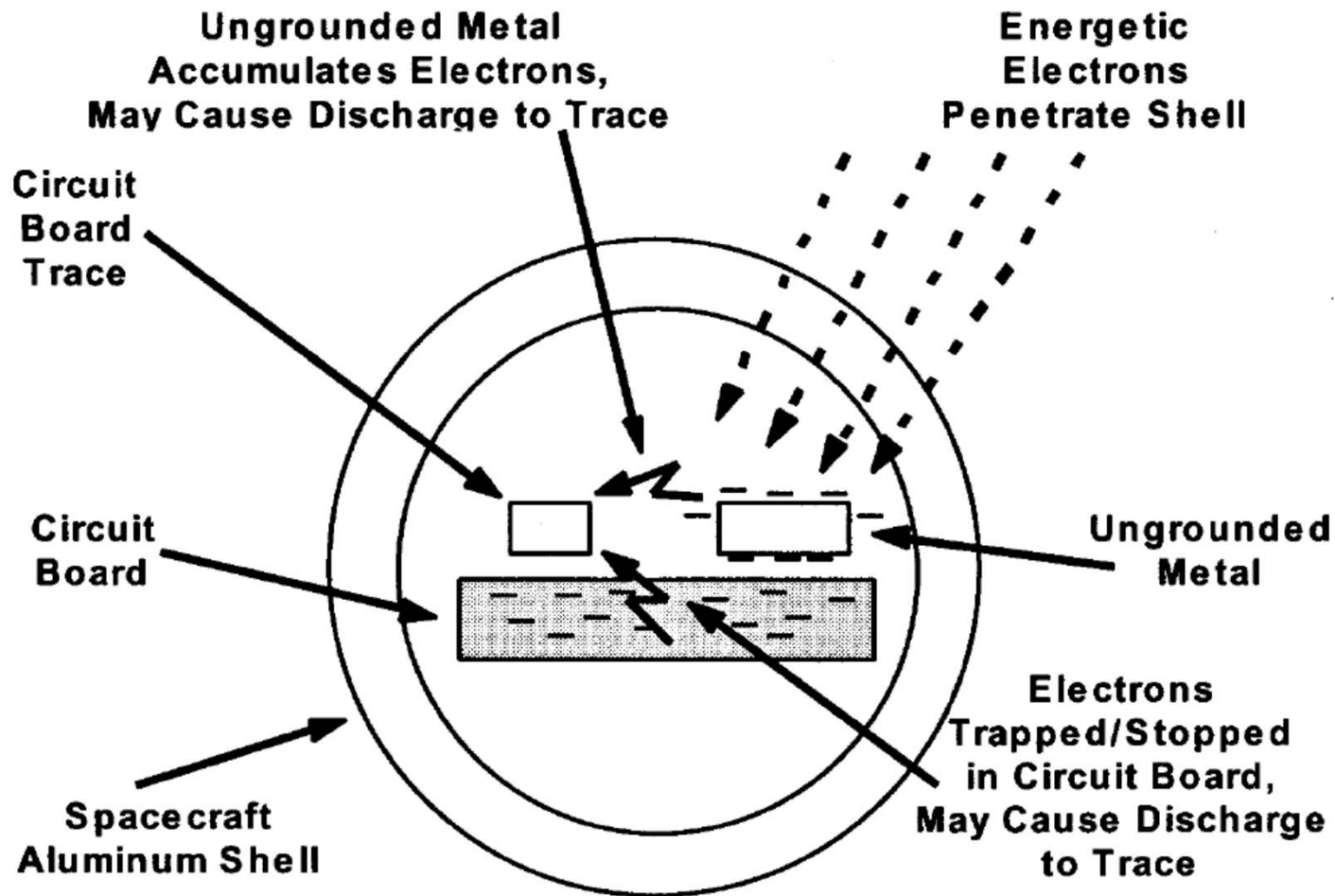




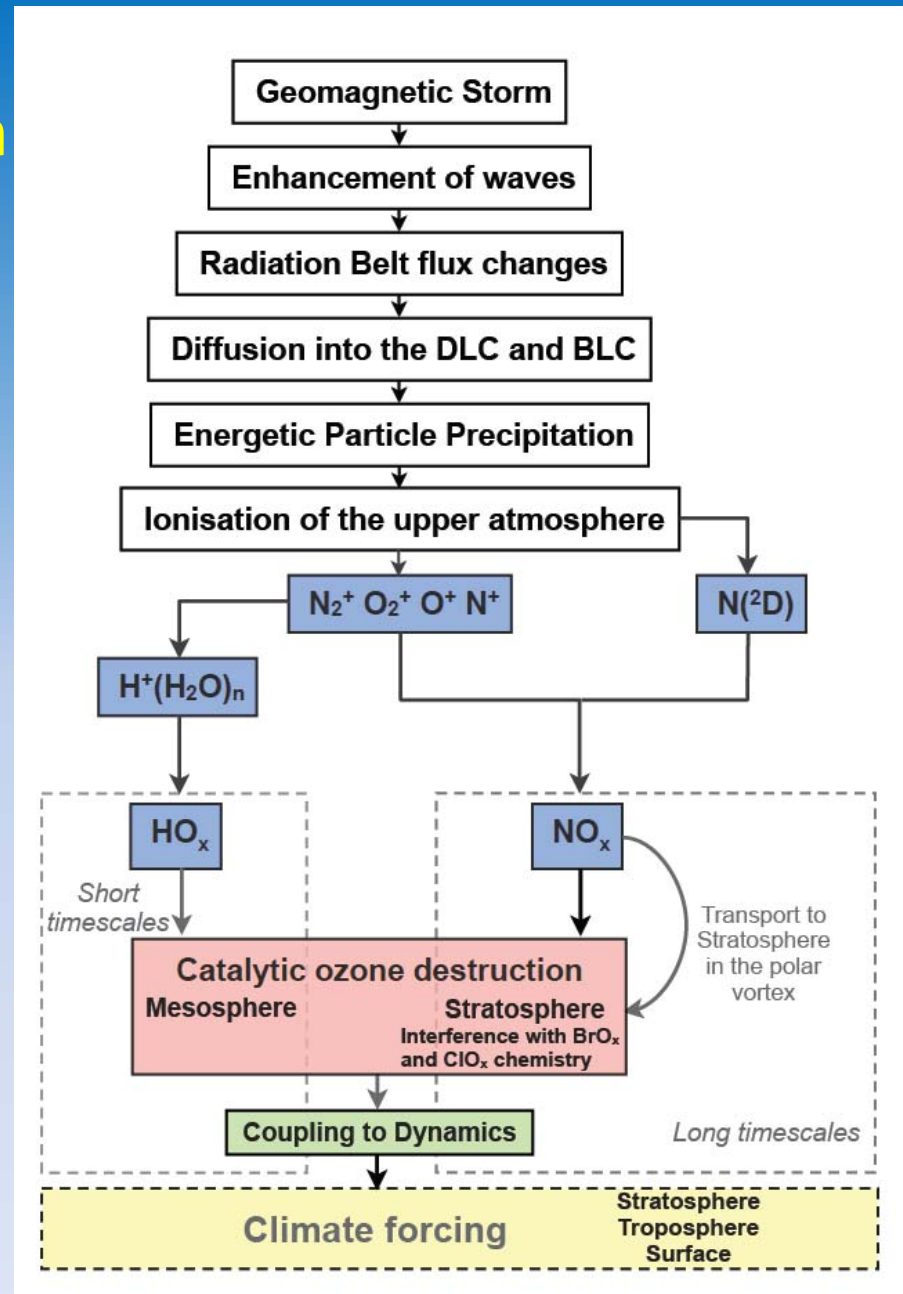
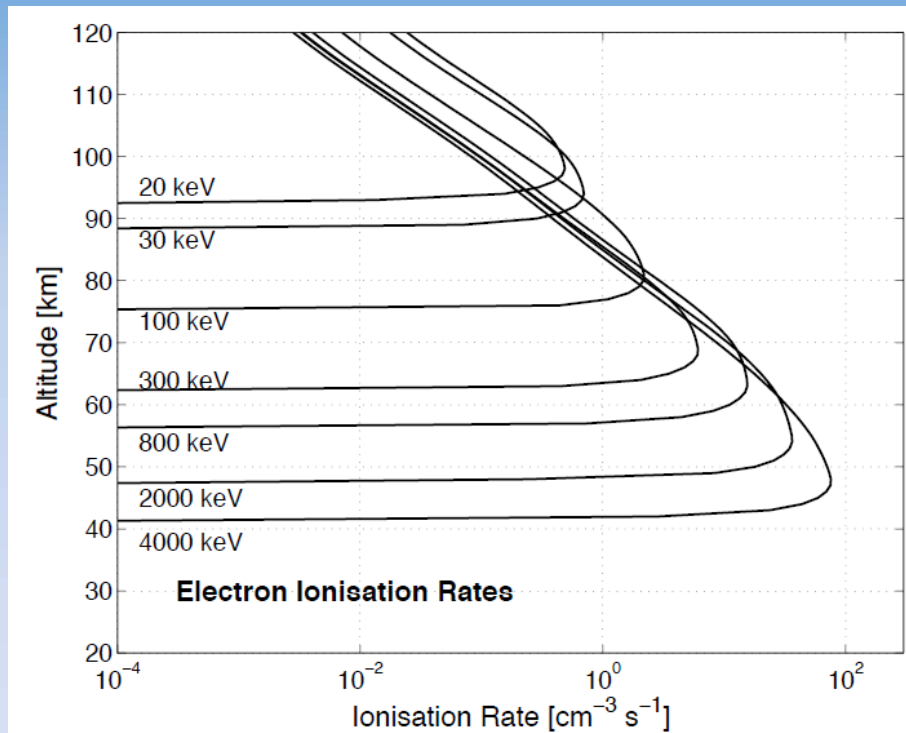
Radiation belt changes during Halloween storms: Baker et al. (*Nature*, 2004)



Internal Charging of Spacecraft



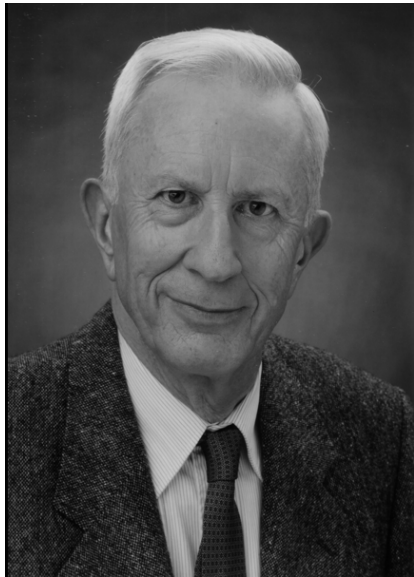
Energetic Electron Precipitation into the Atmosphere



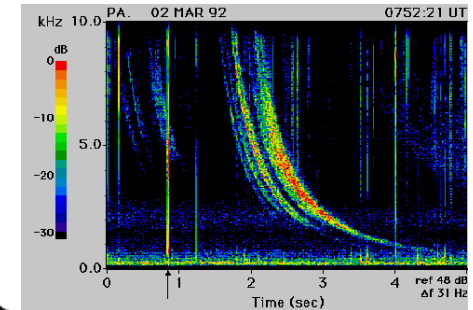
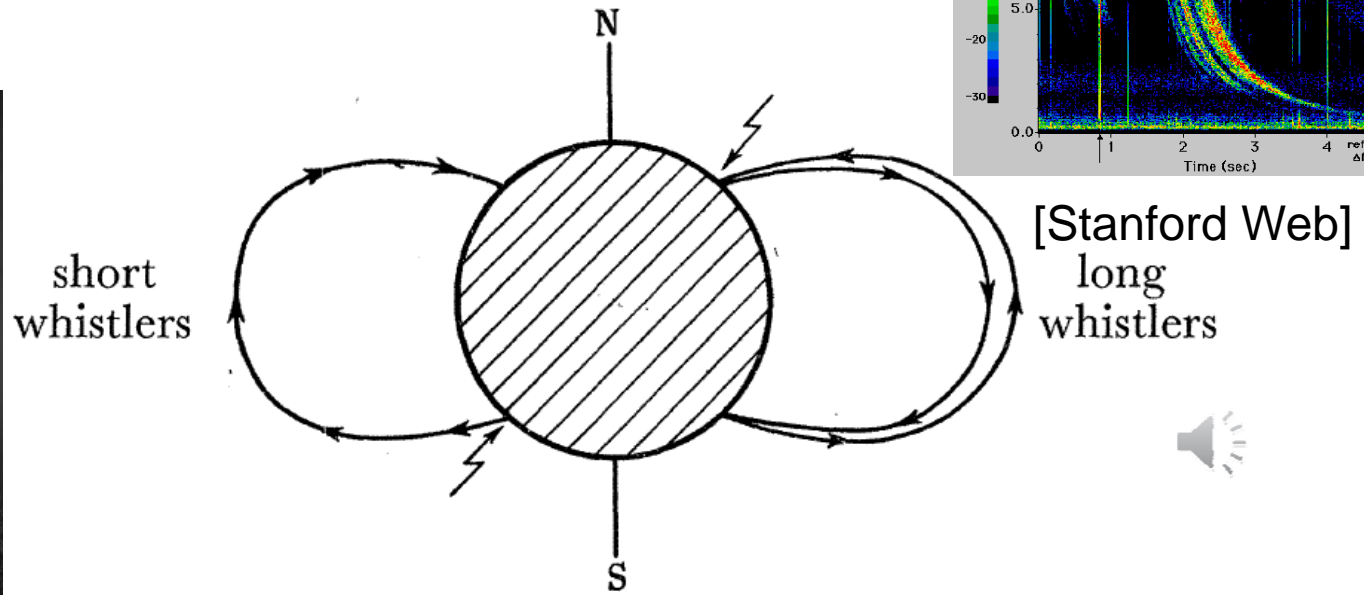
[Clilverd et al., Oxford Univ. Press, 2015]



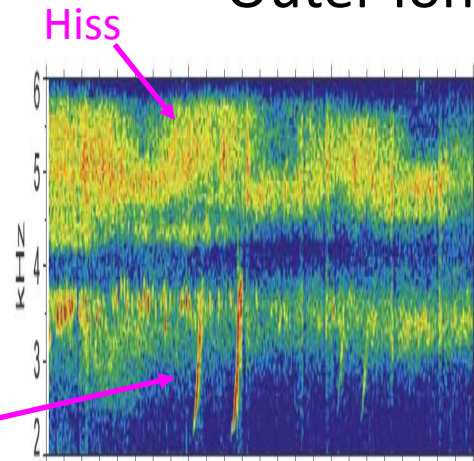
Whistling Atmospheric



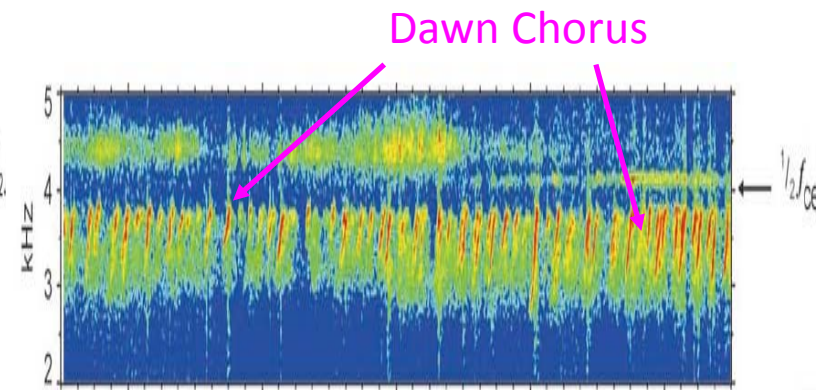
[L. R. O. Storey, 1953]



Outer Ionosphere = Magnetosphere



Isolated Rising Whistles

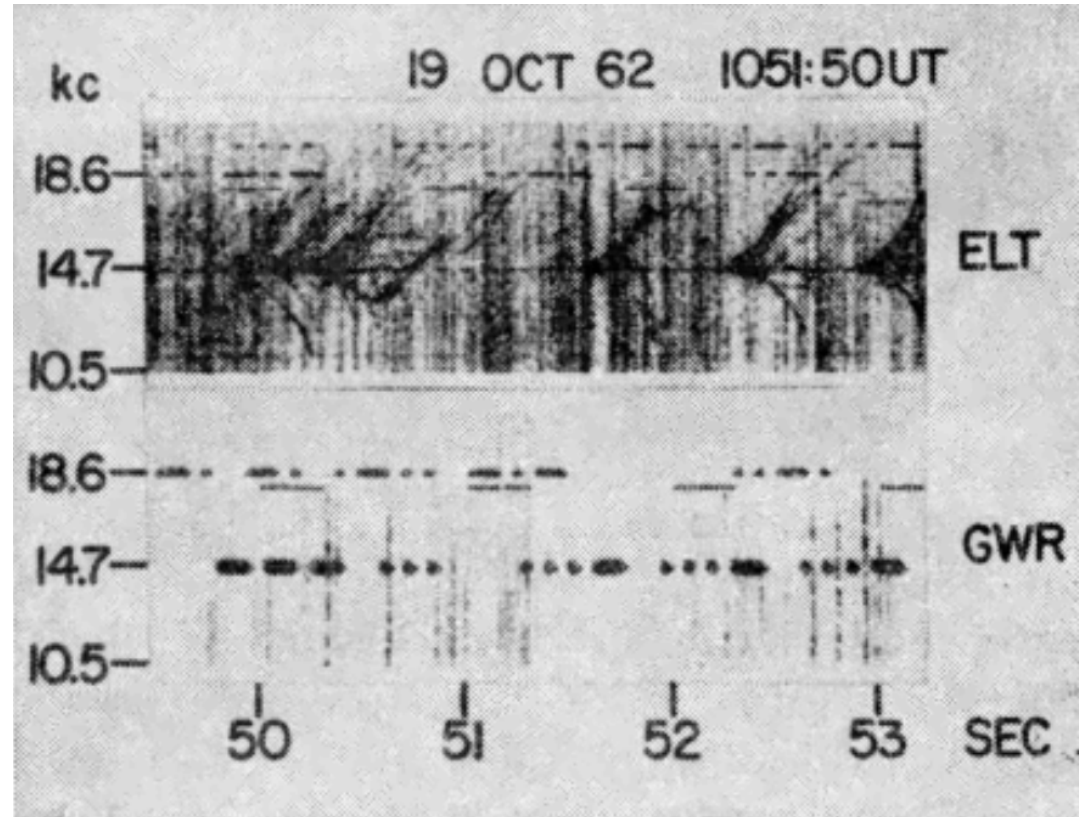


[Santolik et al., JGR, 2003]

VLF Triggered Emissions



[R. A. Helliwell, et al.,
JGR, 1964]



Rising and falling tones from the Morse code dashes

Linear Theory

$$\frac{\partial \omega}{\partial t} = 0$$

Linear Growth Rate

$$\gamma = \pi |\Omega^-| \left(1 - \frac{\omega}{|\Omega^-|}\right)^2 \eta^-(V_R) \cdot \left\{ A^-(V_R) - \frac{1}{|\Omega^-|/\omega - 1} \right\}$$

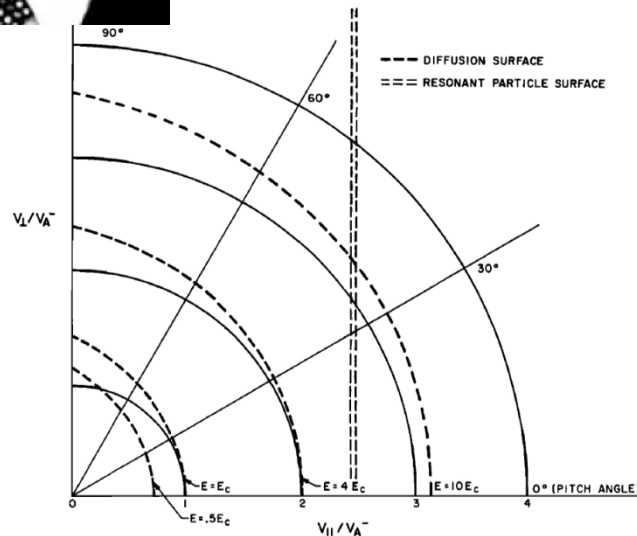


[C. F. Kennel and H. E. Petschek, JGR, 1966]

$$\eta^-(V_R) = 2\pi \frac{|\Omega^-| - \omega}{k} \cdot \int_0^\infty v_\perp dv_\perp F^-(v_\perp, v_\parallel = V_R)$$

$$A^-(V_R) = \frac{\int_0^\infty v_\perp dv_\perp \left(v_\parallel \frac{\partial F^-}{\partial v_\perp} - v_\perp \frac{\partial F^-}{\partial v_\parallel} \right) \frac{v_\perp}{v_\parallel}}{2 \int_0^\infty v_\perp dv_\perp F^-} \Bigg|_{v_\parallel = V_R}$$

Quasi-Linear Diffusion of Resonant Electrons



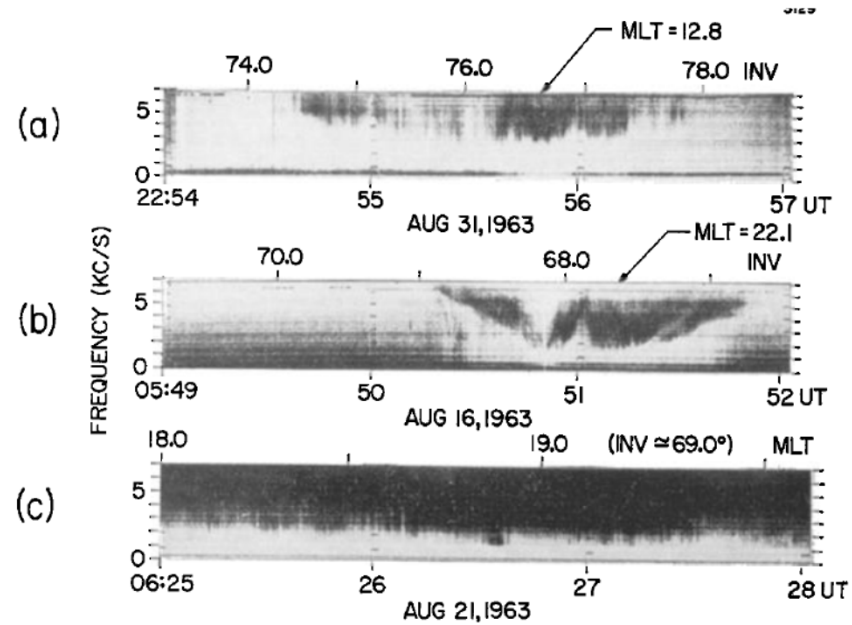
$$\frac{\partial F^-}{\partial t} = \frac{1}{\sin \alpha} \frac{\partial}{\partial \alpha} \cdot \left\{ -\sin \alpha \frac{\langle \Delta \alpha \rangle}{\Delta t} F^- + \sin \alpha \frac{\partial}{\partial \alpha} (D F^-) \right\}$$

$$D \approx \frac{(\Delta \alpha)^2}{2 \Delta t} \approx \frac{(\Omega^-)^2}{2} \left(\frac{B'}{B} \right)^2 \Delta t$$

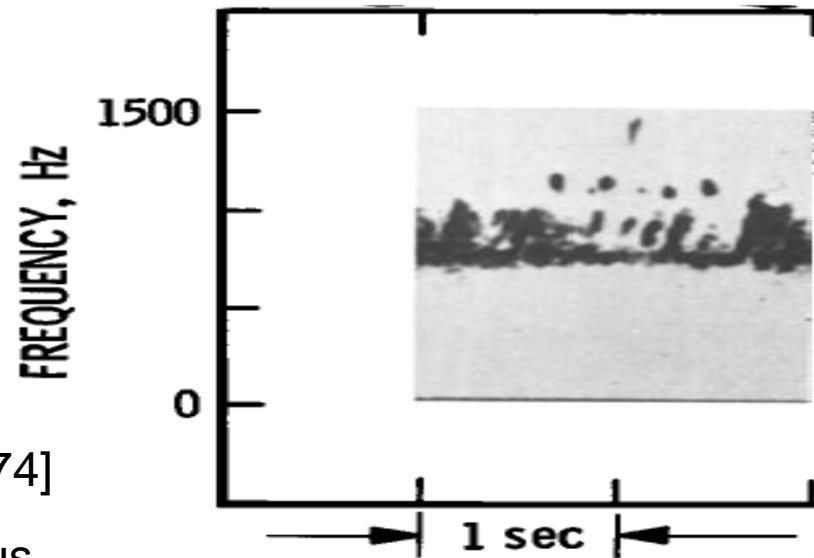
Spacecraft Observation



[D. Gurnett, 1966] VLF Hiss



[B. T. Tsurutani and E. J. Smith, 1974]
Upper-band and Lower-band Chorus



Theory and Simulations of Whistler-mode Waves



[I. Kimura, 1966]

Ray Tracing



[D. Nunn, 1971]

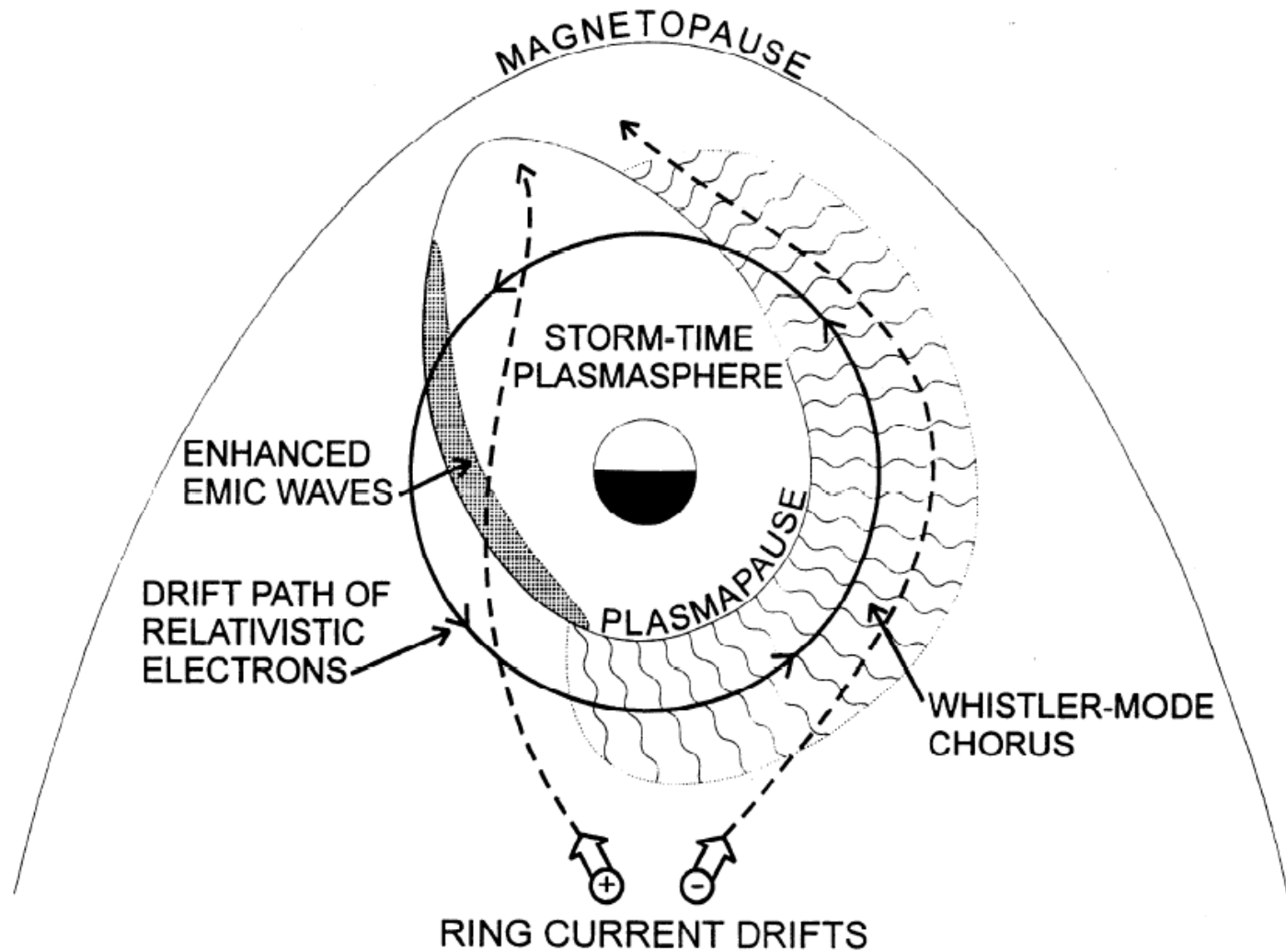
Nonlinear Theory and
Vlasov Simulations



[H. Matsumoto
and Y. Yasuda,
1976]

Particle Simulations of
Whistler Mode Instability

Relativistic Theory of Wave-Particle Resonant Diffusion with Application to Electron Acceleration in the Magnetosphere



[Summers et al., JGR, 1998]

New Generation of Spacecraft Observation

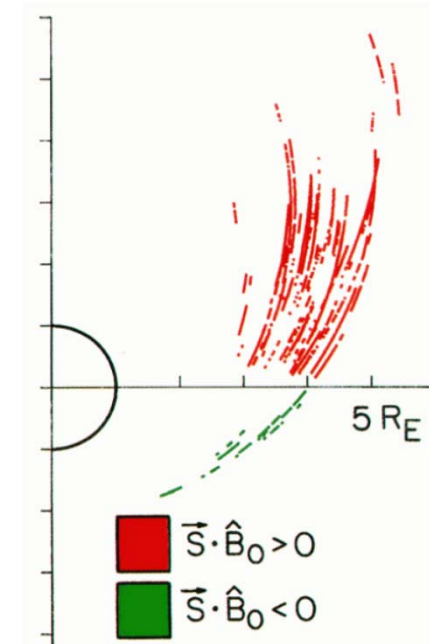
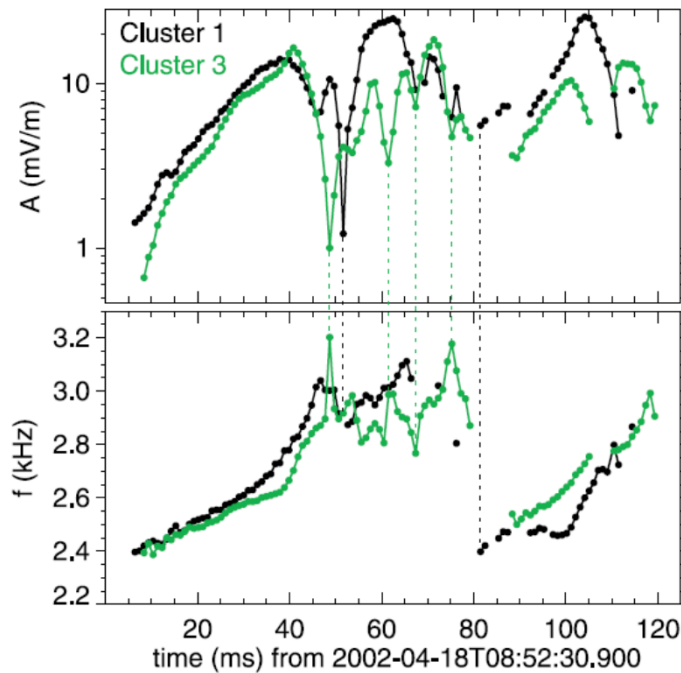
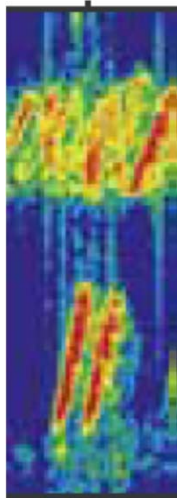
Polar spacecraft

Source very close to Geomagnetic Equator

Absolute Instability at the Equator

Cluster spacecraft

Large Wave Amplitude: 10-100pt



[LeDocq et al., 1998]

Nonlinear Wave-Particle Interaction

[Santolik et al., JGR, 2003]

EMFISIS Waves, Van Allen Probe B, 2 July 2014

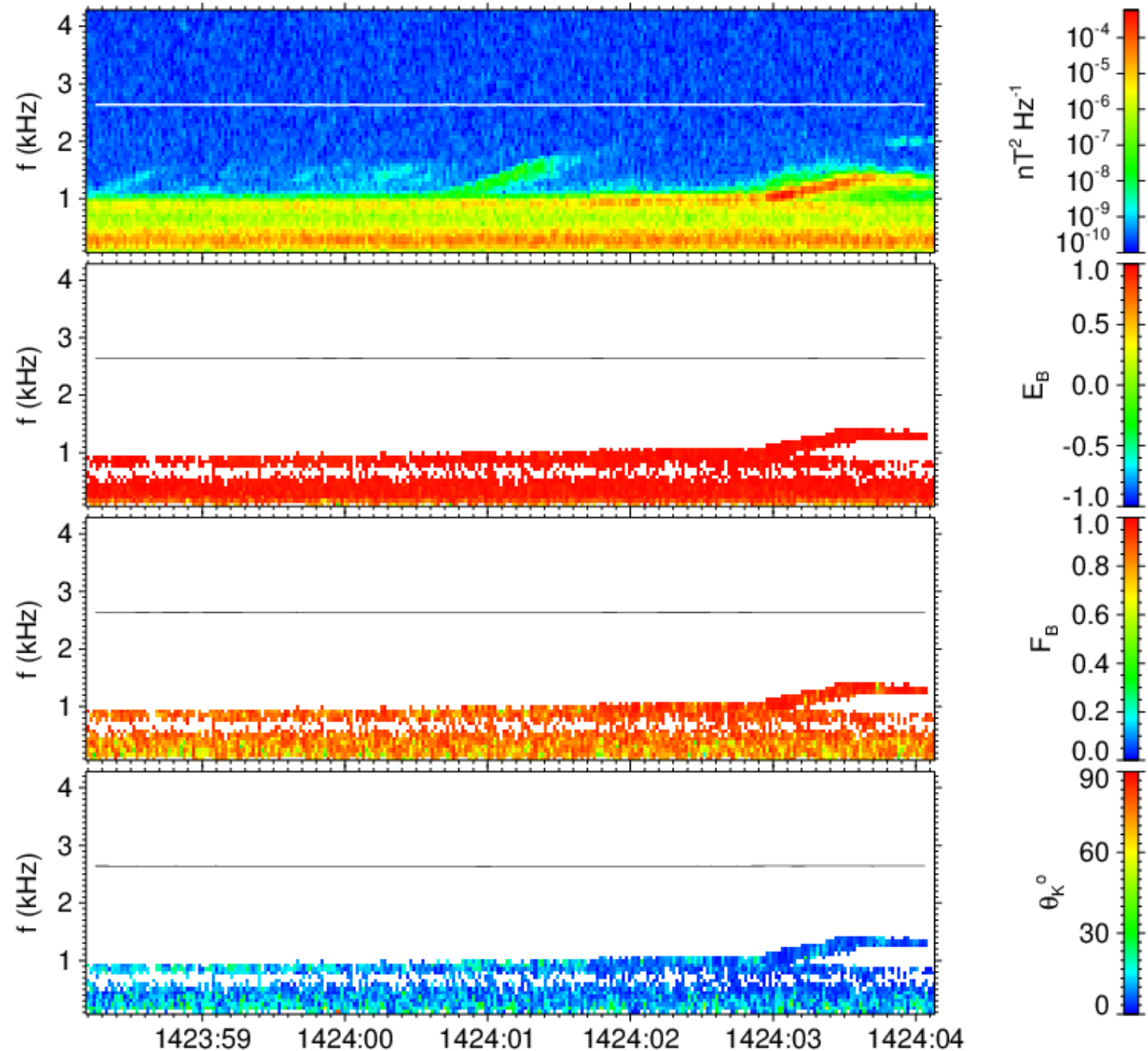
sum of the
power-spectral
densities of
magnetic
components



ellipticity of the
magnetic field
polarization

planarity of the
magnetic field
polarization

angle between
the wave vector
and the
background
magnetic field



EMFISIS Waves, Van Allen Probe A, 14 April 2014

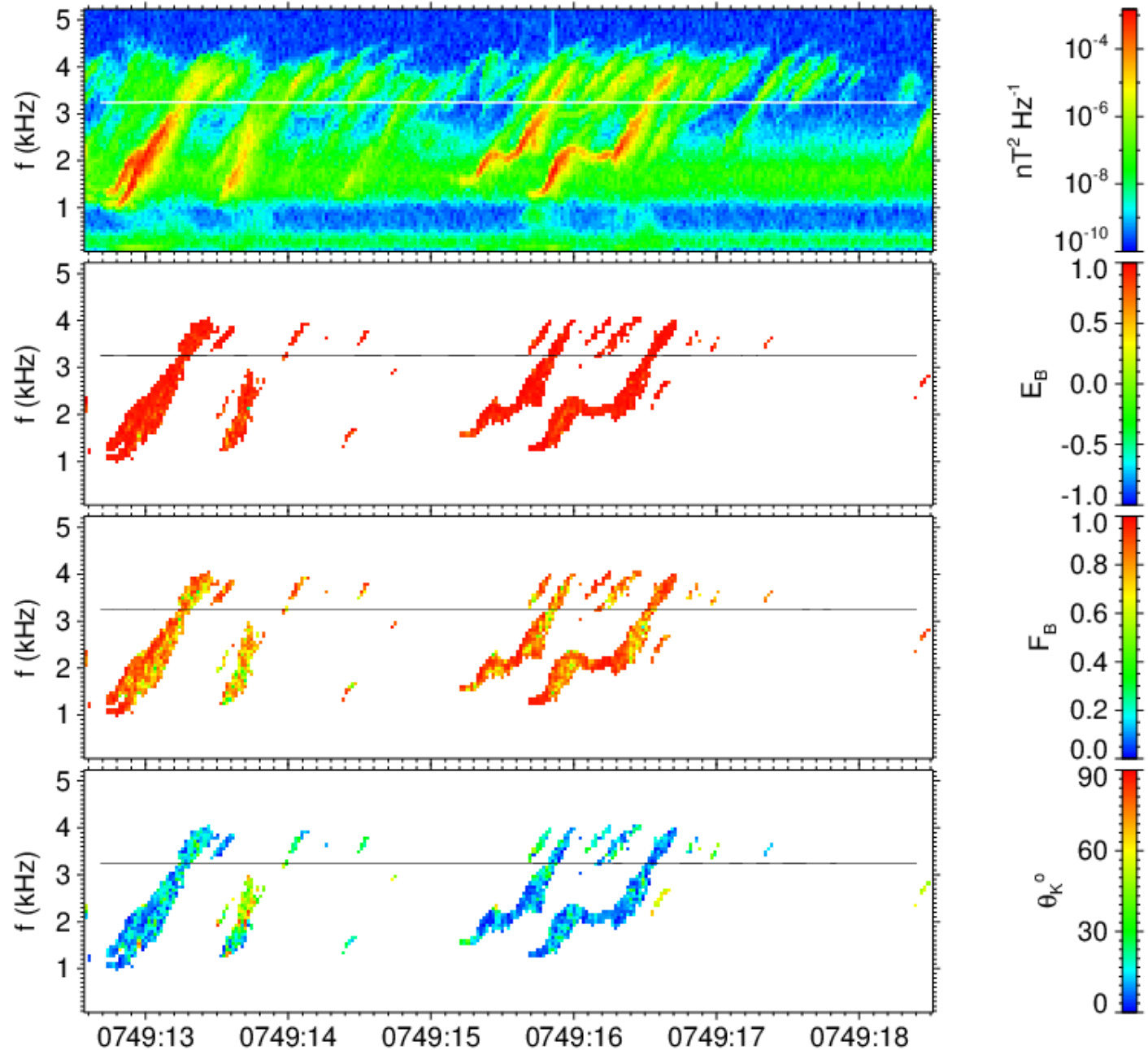
sum of the
power-spectral
densities of
magnetic
components



ellipticity of the
magnetic field
polarization

planarity of the
magnetic field
polarization

angle between
the wave vector
and the
background
magnetic field



EMFISIS Waves, Van Allen Probe A, 8 June 2014

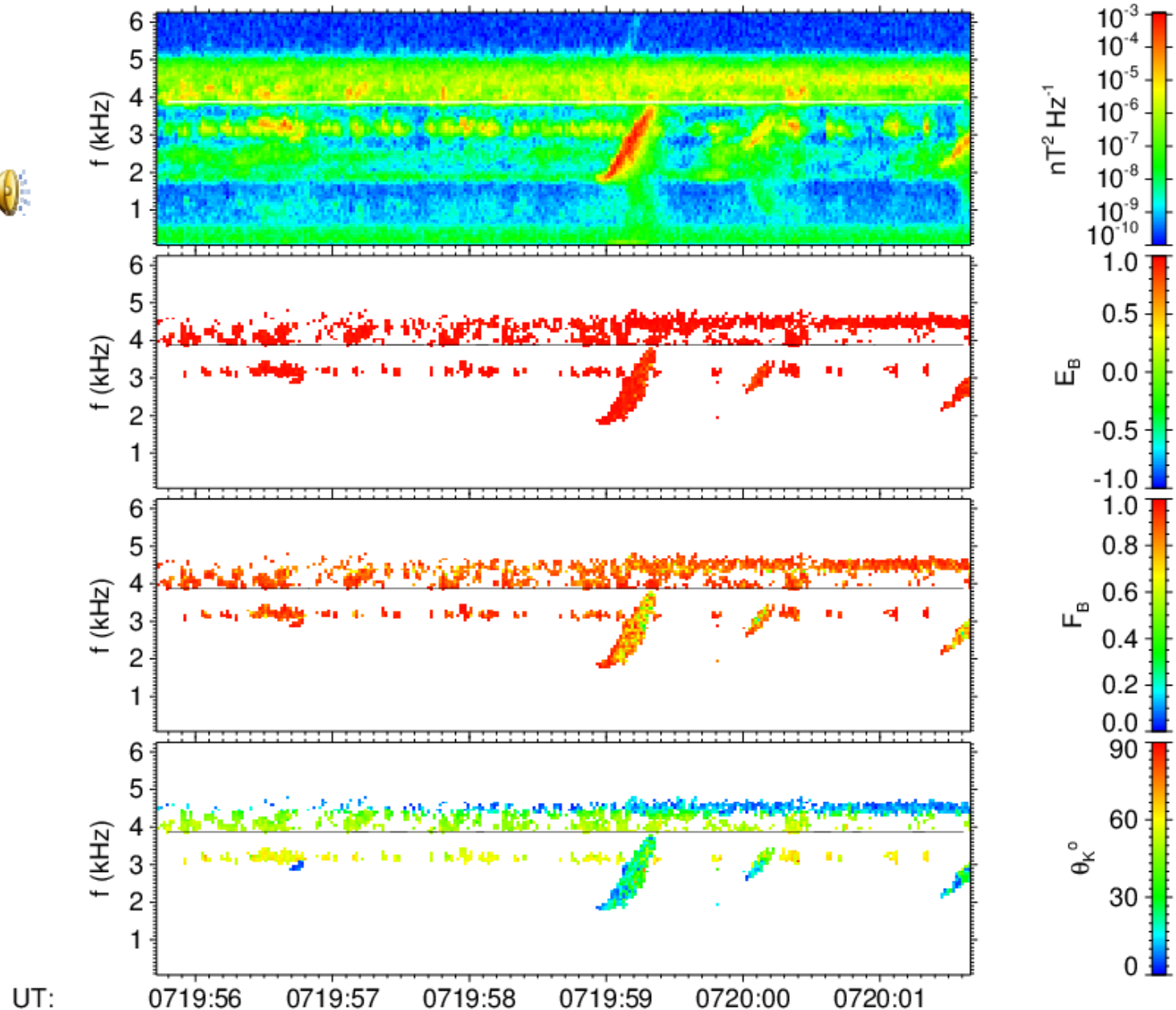
sum of the
power-spectral
densities of
magnetic
components



ellipticity of the
magnetic field
polarization

planarity of the
magnetic field
polarization

angle between
the wave vector
and the
background
magnetic field



EMFISIS Waves, Van Allen Probe A, 14 Nov 2012

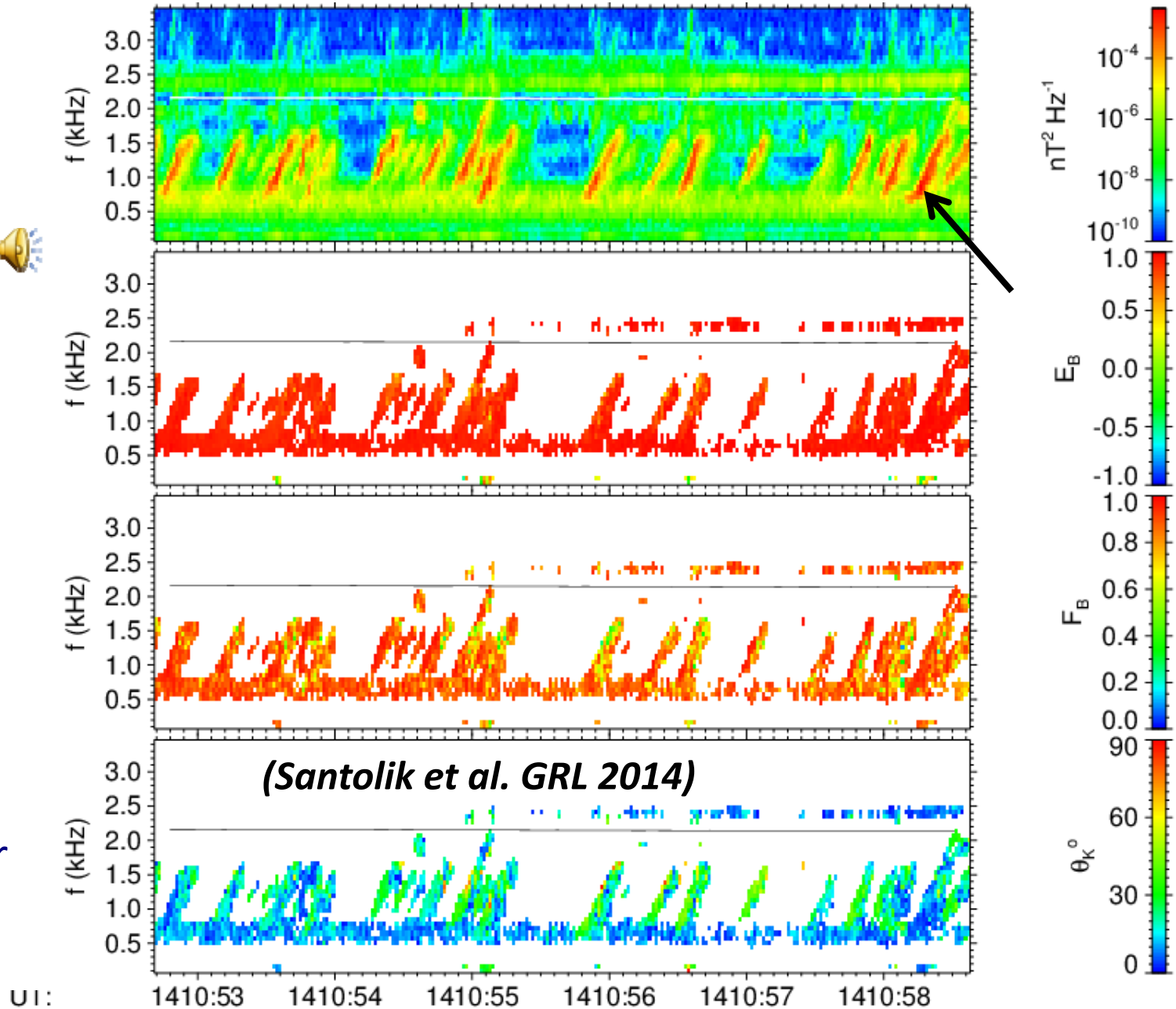
sum of the
power-spectral
densities of
magnetic
components



ellipticity of the
magnetic field
polarization

planarity of the
magnetic field
polarization

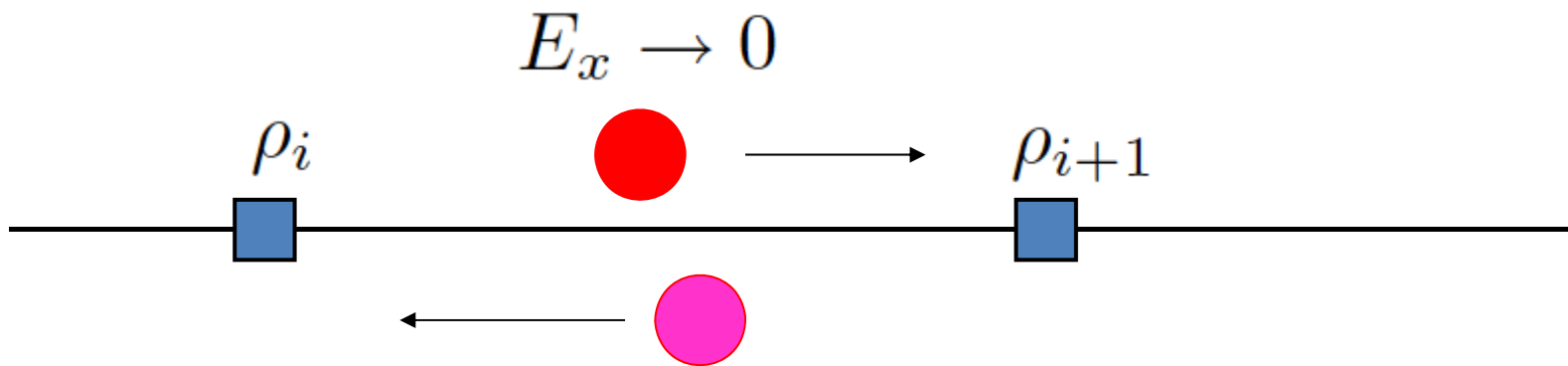
angle between
the wave vector
and the
background
magnetic field



PIC code for Space Plasmas

- Space Plasmas: **Collisionless**
- Particle-In-Cell Code
- Particles: $x(t)$, $v(t)$
- Fields: $E(t, X)$, $B(t, X)$

E and B are defined on grid points, and calculated from ρ and J . The electrostatic force between two particles in the same cell disappears.



Maxwell's Equations

$$\nabla \times \mathbf{B} = \mu_0 \mathbf{J} + \frac{1}{c^2} \frac{\partial \mathbf{E}}{\partial t}$$

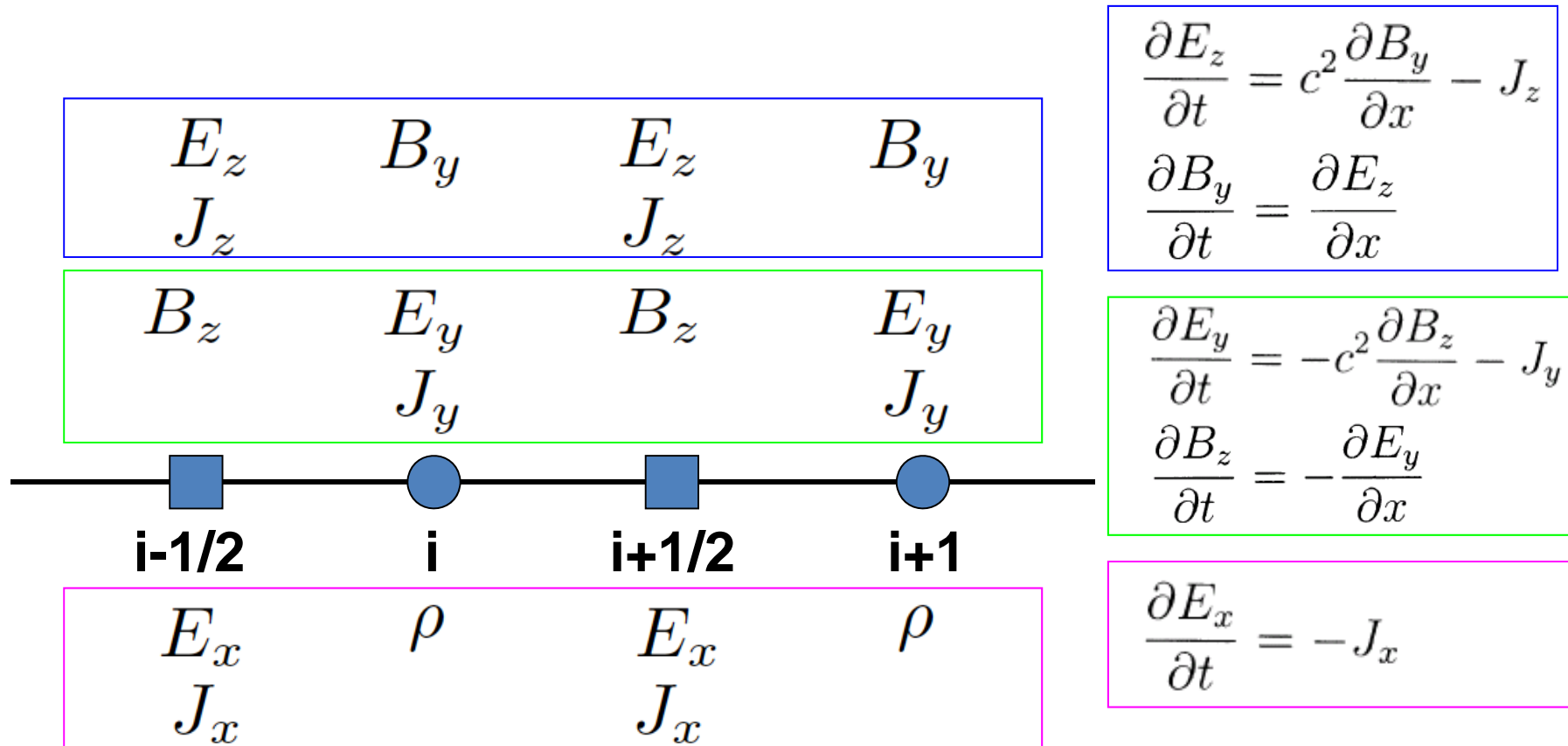
$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

$$\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0}$$

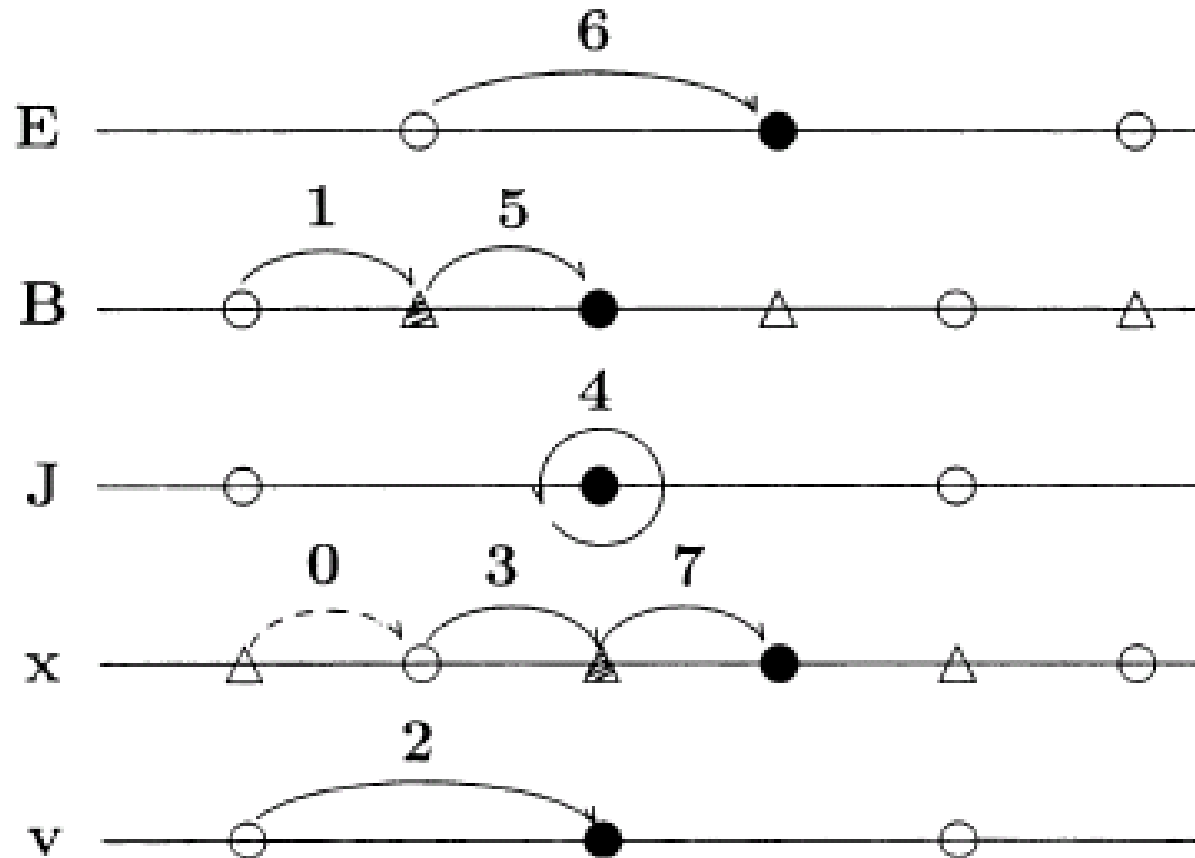
$$\nabla \cdot \mathbf{B} = 0$$

where $\epsilon_0 \mu_0 = \frac{1}{c^2}$

Grid Assignment



Time Step Chart





Centered Difference Scheme

$$E(X_i, t) = E_o \exp(ikX_i - i\omega t)$$

$$\frac{\partial E(X_i, t)}{\partial x} = \frac{E(X_i + \Delta x/2, t) - E(X_i - \Delta x/2, t)}{\Delta x}$$

$$= \frac{1}{\Delta x} [\exp(ik\Delta x/2) - \exp(-ik\Delta x/2)] E(X_i, t)$$

$$= i \frac{\sin(k\Delta x/2)}{\Delta x/2} E(X_i, t) = iK E(X_i, t)$$

k		$K = \frac{\sin(k\Delta x/2)}{\Delta x/2}$
ω		$\Omega = \frac{\sin(\omega\Delta t/2)}{\Delta t/2}$

Courant Condition

Electromagnetic modes in vacuum

$$\omega^2 = c^2 k^2$$

Centered Difference Scheme in space and time

$$\Omega^2 = c^2 K^2 \quad K = \frac{\sin(k\Delta x/2)}{\Delta x/2}$$

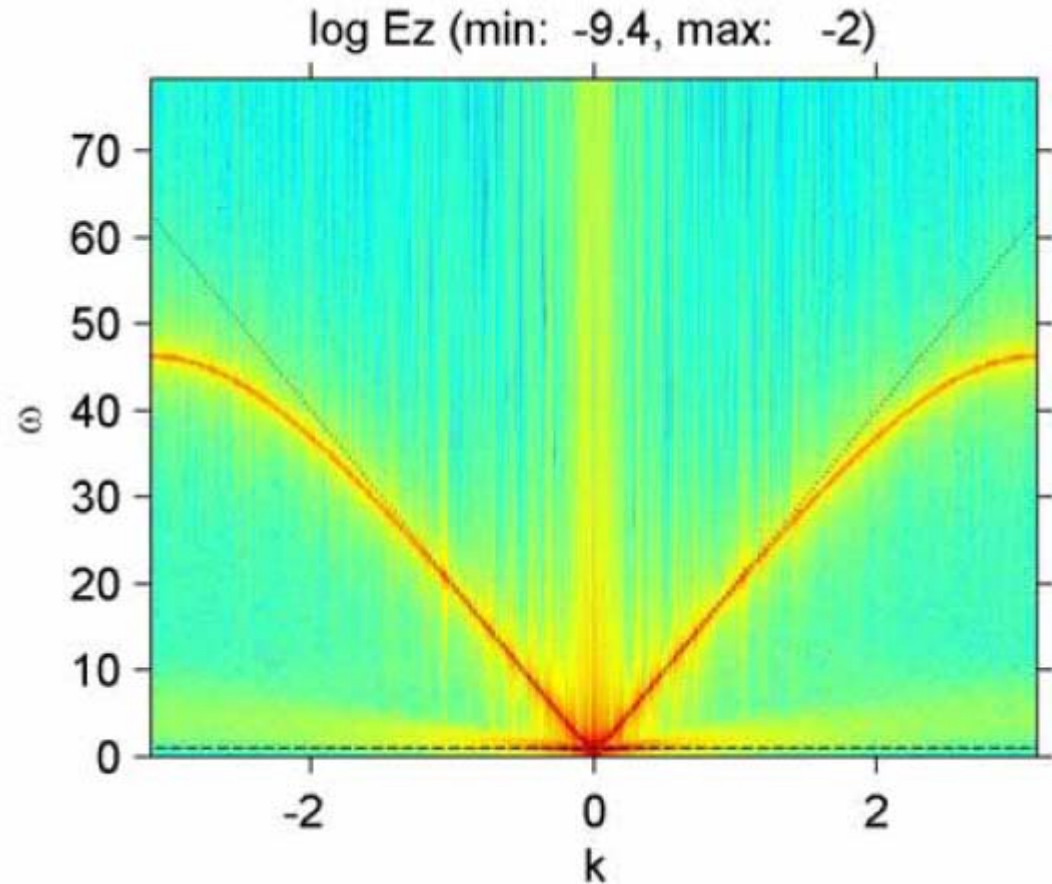
For $k = \frac{\pi}{\Delta x}$ we have $\sin\left(\frac{\omega\Delta t}{2}\right) = \frac{\Delta t}{\Delta x} c < 1$

Courant Condition

$$c\Delta t < \Delta x$$

Dispersion Relation of Light Mode

$$\Omega^2 = c^2 K^2$$



$$\Omega = \frac{\sin(\omega \Delta t / 2)}{\Delta t / 2},$$

$$K = \frac{\sin(k \Delta x / 2)}{\Delta x / 2}$$

Charge Density

$$\rho_i = \frac{1}{\Delta x} \sum_j^{N_p} q_j W(x_j - X_i)$$

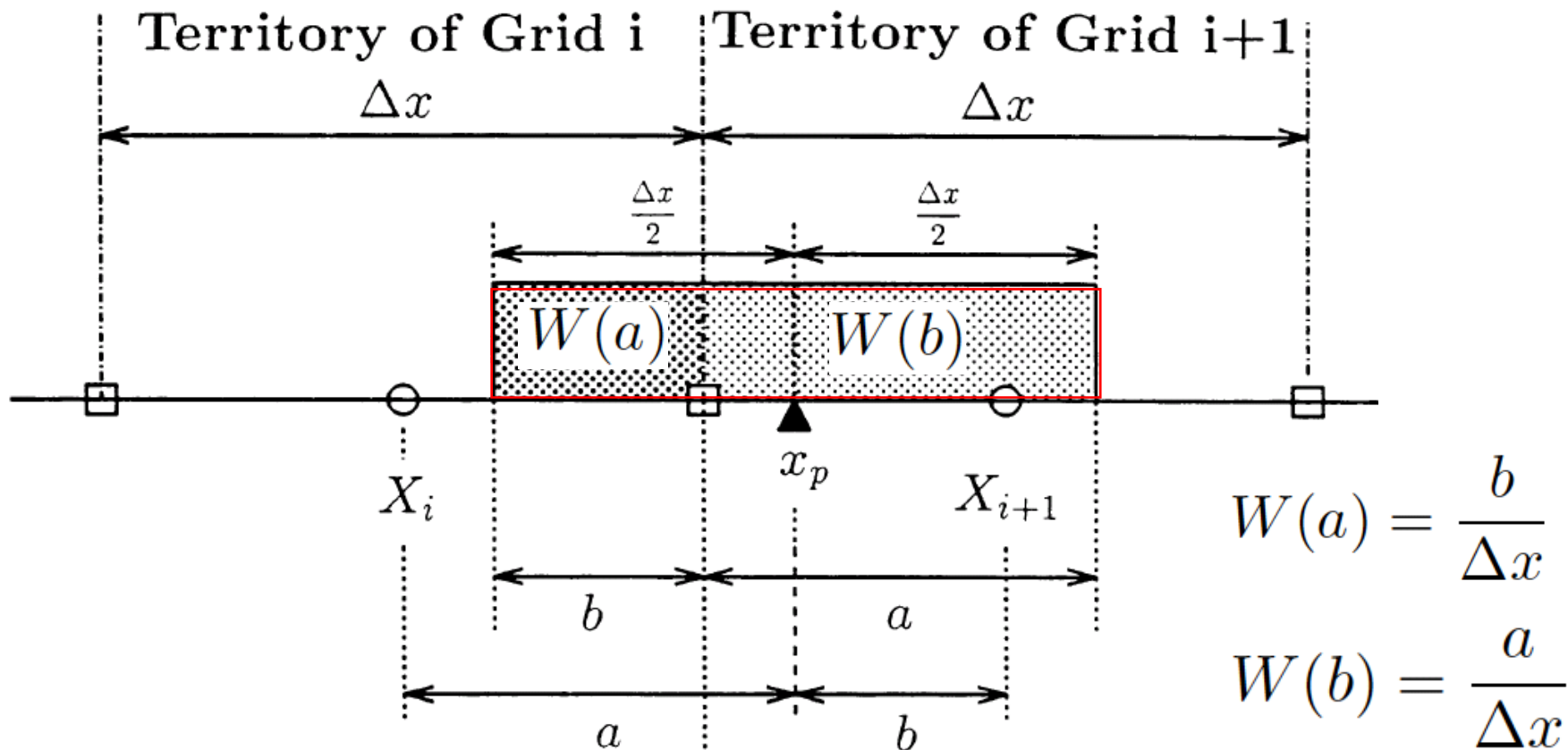
Shape Function

$$W(x) = 1 - \frac{|x|}{\Delta x}, \quad |x| \leq \Delta x$$

$$= 0, \quad |x| > \Delta x$$

N_p : Number of Particles

“fat particle”



Buneman-Boris Method

$$\frac{\mathbf{v}^{t+\Delta t/2} - \mathbf{v}^{t-\Delta t/2}}{\Delta t} = \frac{q_s}{m_s} \left(\mathbf{E}^t + \frac{\mathbf{v}^{t+\Delta t/2} + \mathbf{v}^{t-\Delta t/2}}{2} \times \mathbf{B}^t \right)$$

$$\mathbf{v}^- = \mathbf{v}^{t-\Delta t/2} + \frac{q_s}{m_s} \mathbf{E}^t \frac{\Delta t}{2} \quad \mathbf{v}^+ = \mathbf{v}^{t+\Delta t/2} - \frac{q_s}{m_s} \mathbf{E}^t \frac{\Delta t}{2}$$

$$\frac{\mathbf{v}^+ - \mathbf{v}^-}{\Delta t} = \frac{1}{2} \frac{q_s}{m_s} (\mathbf{v}^+ + \mathbf{v}^-) \times \mathbf{B}^t$$

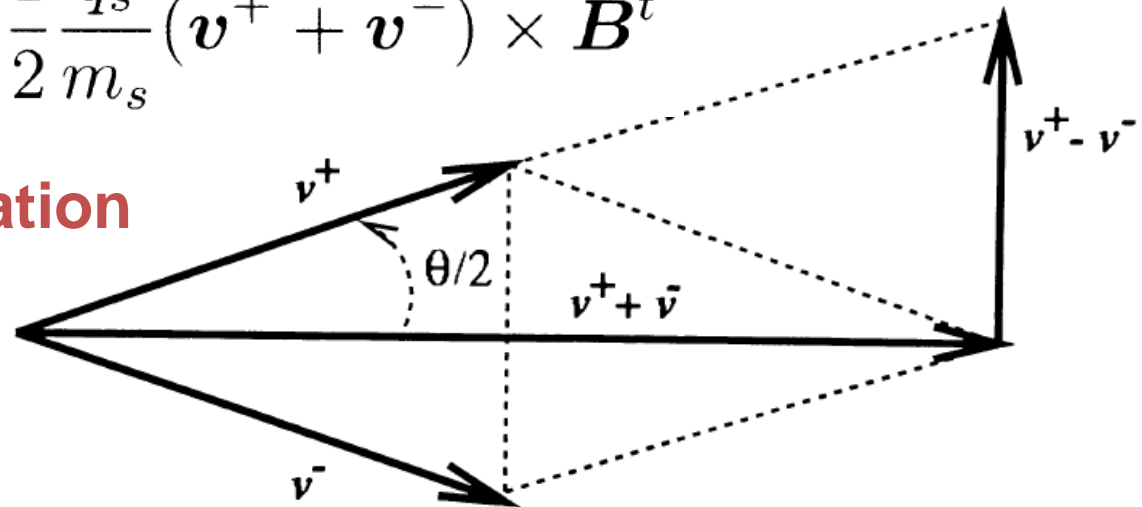
Kinetic Energy Conservation

$$(\mathbf{v}^+)^2 = (\mathbf{v}^-)^2$$

Small Phase Delay

$$\Omega_c = \frac{\tan^{-1} \omega_c \Delta t / 2}{\Delta t / 2}$$

$$\Omega_c / \omega_c = 0.9967 \text{ with } \omega_c \Delta t = 0.2$$



Relativistic Equation of Motion

$$\frac{d}{dt}(m\mathbf{v}) = q(\mathbf{E} + \mathbf{v} \times \mathbf{B})$$

$$m = \gamma m_0$$
$$\gamma = \frac{1}{\sqrt{1 - \left(\frac{v}{c}\right)^2}}$$

$$\mathbf{u} = \frac{c}{\sqrt{c^2 - |\mathbf{v}|^2}} \mathbf{v}$$

$$\mathbf{B}_u = \frac{c}{\sqrt{c^2 + |\mathbf{u}|^2}} \mathbf{B}$$

$$\frac{d\mathbf{u}}{dt} = \frac{q}{m_0} (\mathbf{E} + \mathbf{u} \times \mathbf{B}_u)$$

$$\mathbf{v} = \frac{c}{\sqrt{c^2 + |\mathbf{u}|^2}} \mathbf{u}$$

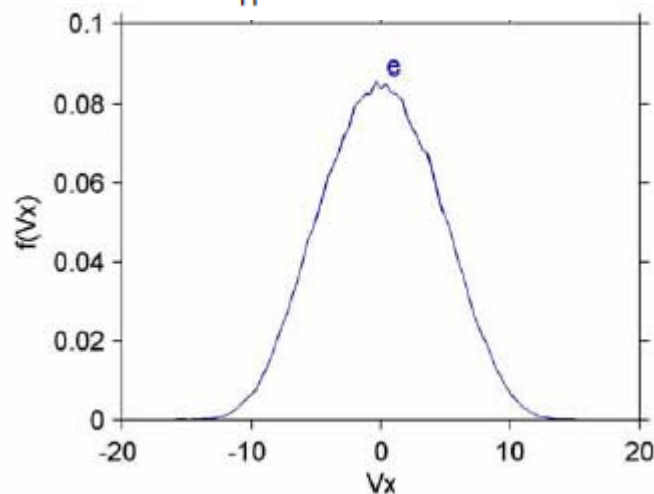
Initial Velocity Distribution Function

$$f(u_{\parallel}, u_{\perp}) \propto \exp\left(-\frac{(u_{\parallel} - V_{d\parallel})^2}{2V_{t\parallel}^2} - \frac{(u_{\perp} - V_{d\perp})^2}{2V_{t\perp}^2}\right)$$

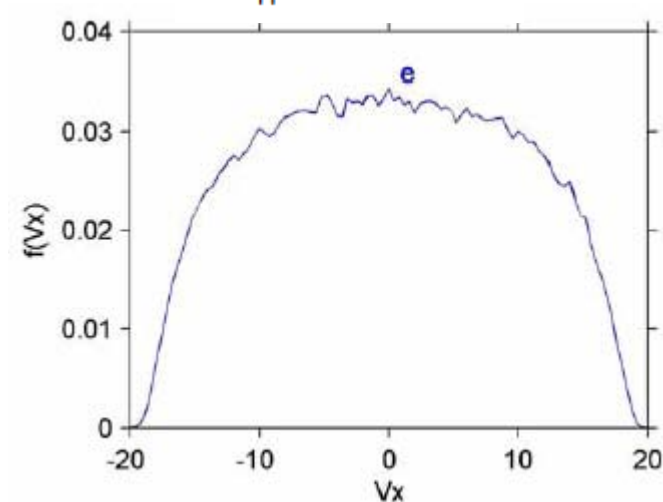
$$\mathbf{v} = \mathbf{u}/\gamma = \frac{c}{\sqrt{c^2 + u_x^2 + u_y^2 + u_z^2}} \mathbf{u}$$

$$V_{d\parallel} = V_{d\perp} = 0$$

$$V_{t\parallel}/c = 0.25$$

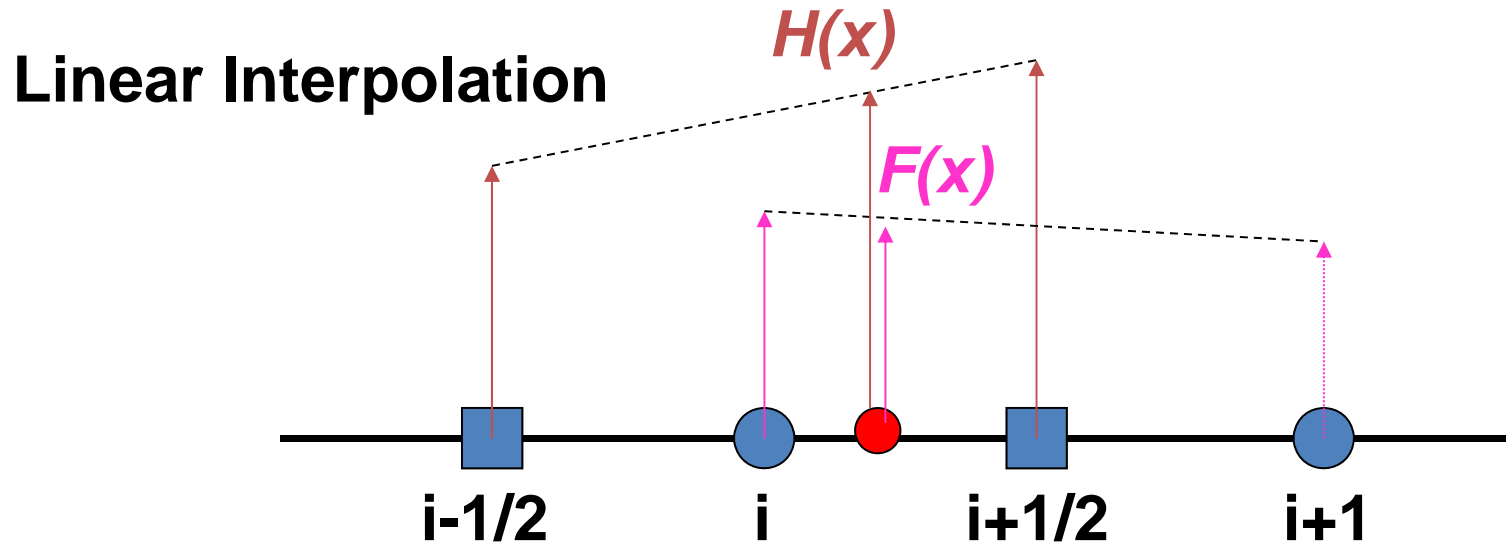


$$V_{t\parallel}/c = 1$$



Field Interpolation to Particle Position

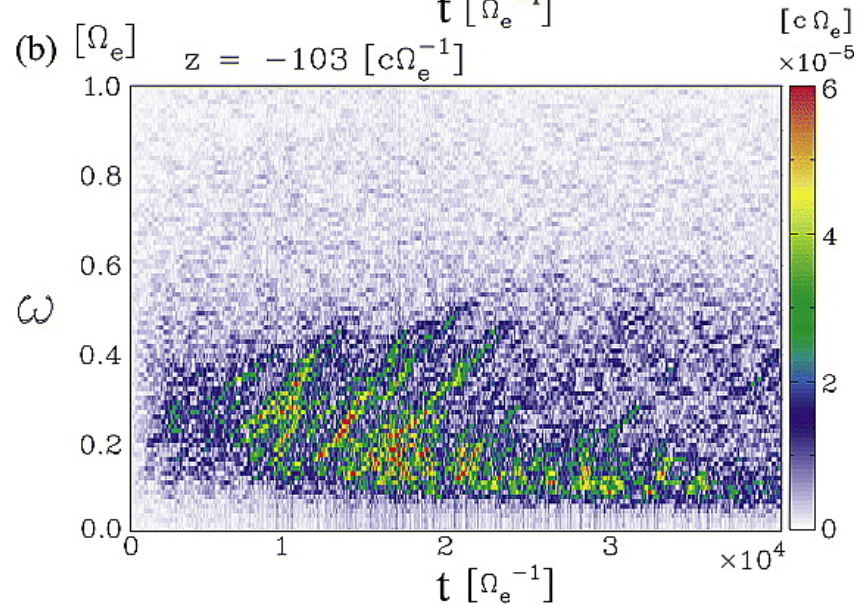
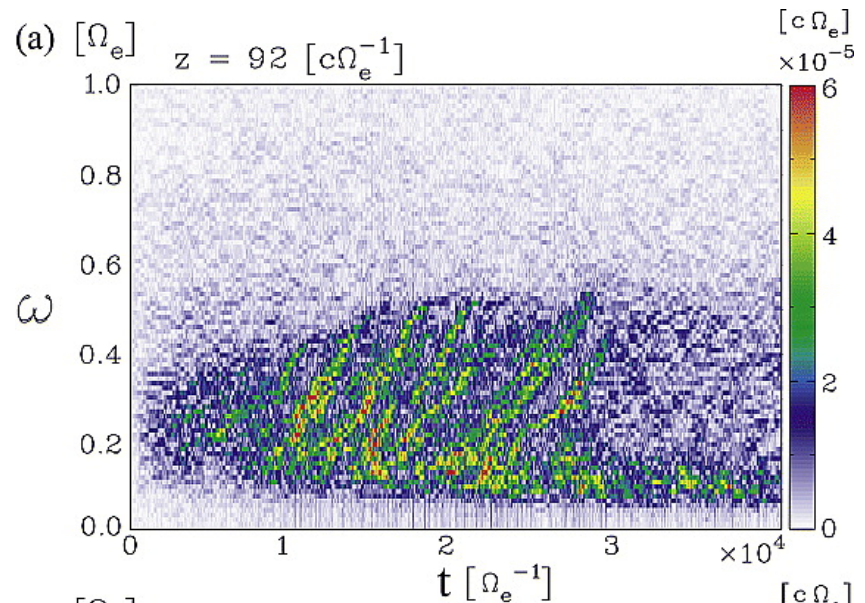
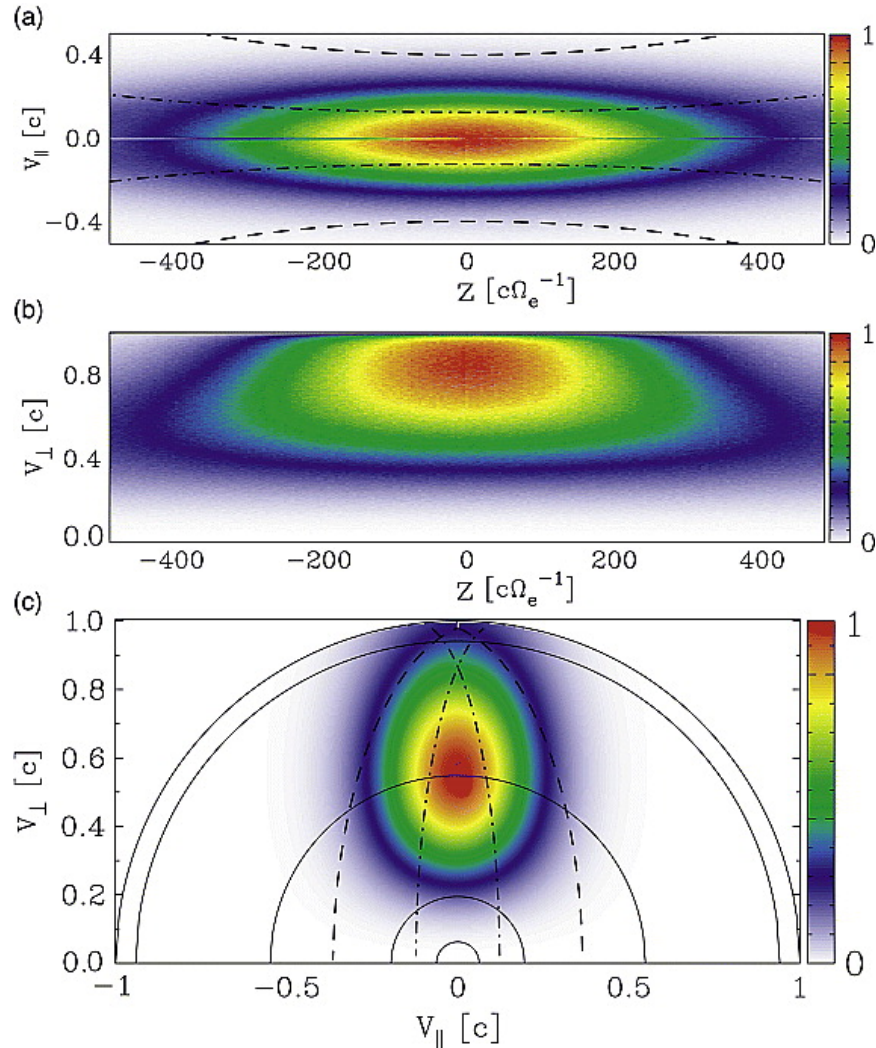
$$F(x) = \sum_{i=1}^{N_x} F_i W(x - X_i)$$
$$H(x) = \sum_{i=1}^{N_x} H_{i+1/2} W(x - X_{i+1/2})$$



Electron Hybrid Simulation

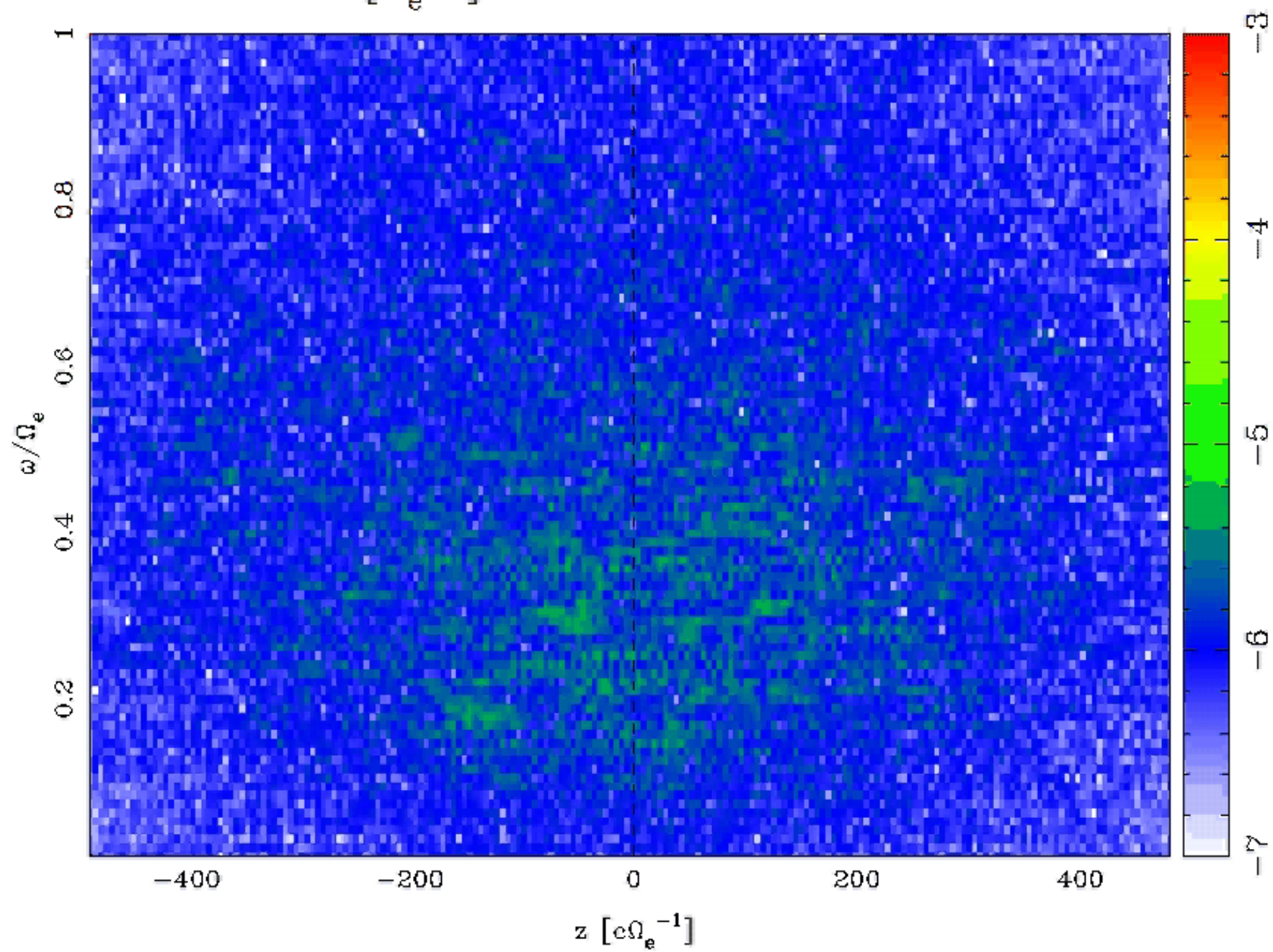
Cold electrons: Fluid

Hot electrons: Particles



[Kato and Omura, GRL, 2007]

$t = 599.04 [\Omega_e^{-1}]$



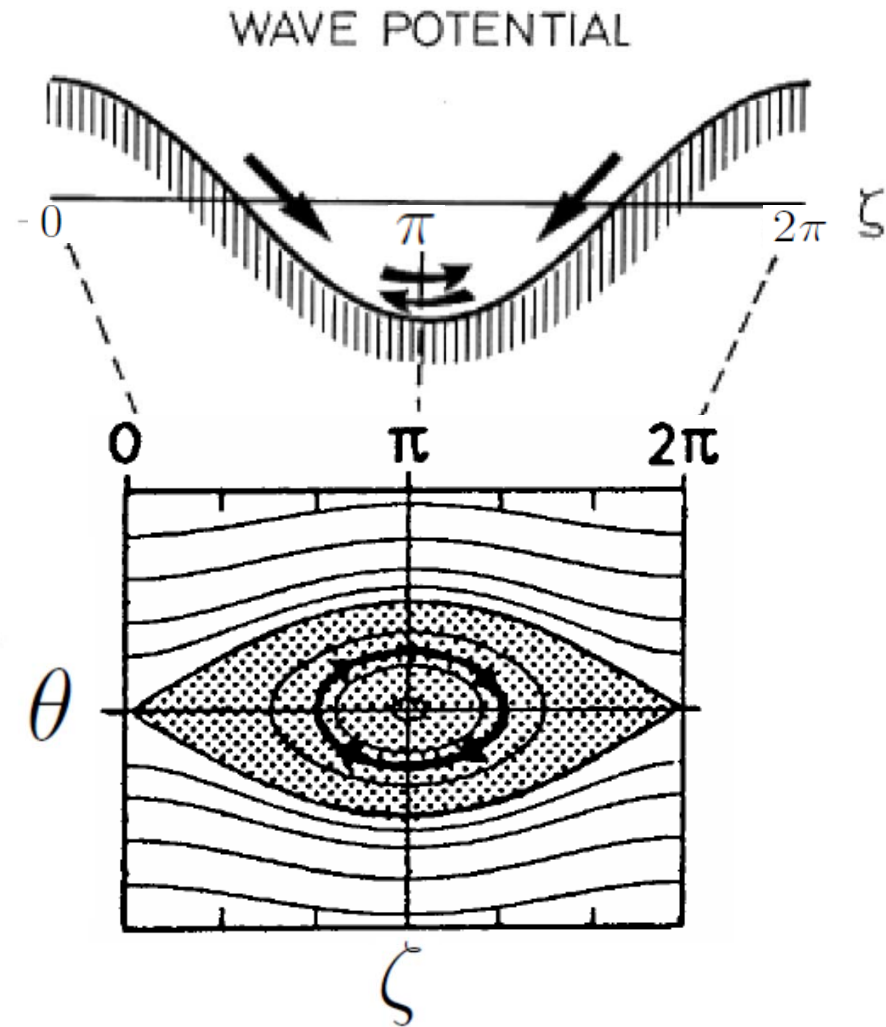
Equations of Resonant Particles

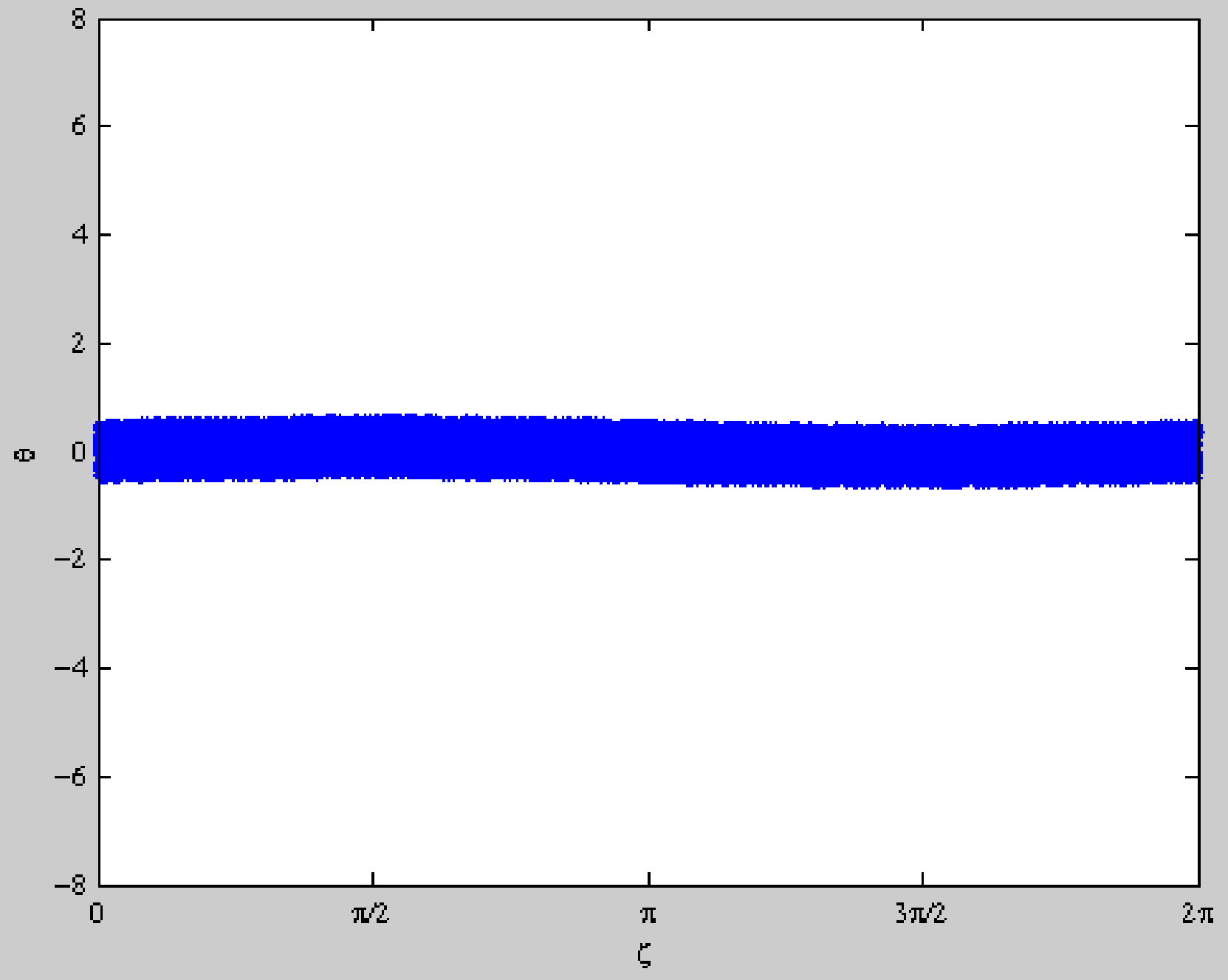
$$\frac{d\theta}{dt} = \omega_t^2 \sin \zeta$$

$$\frac{d\zeta}{dt} = \theta$$

Trapping Frequency

$$\omega_t = \sqrt{\frac{k |q_s| E_w}{m_s}}$$





$$\theta = k(v_{\parallel} - V_p) \quad \text{for Longitudinal Wave}$$

$$\theta = k(v_{\parallel} - V_R) \quad \text{for Whistler-mode Wave}$$

$$V_R = \frac{\omega - \Omega_e}{k}$$

$$\frac{d\theta}{dt} = \omega_t^2 (\sin \zeta + S)$$

$$\frac{d\zeta}{dt} = \theta$$

S : Inhomogeneity Factor

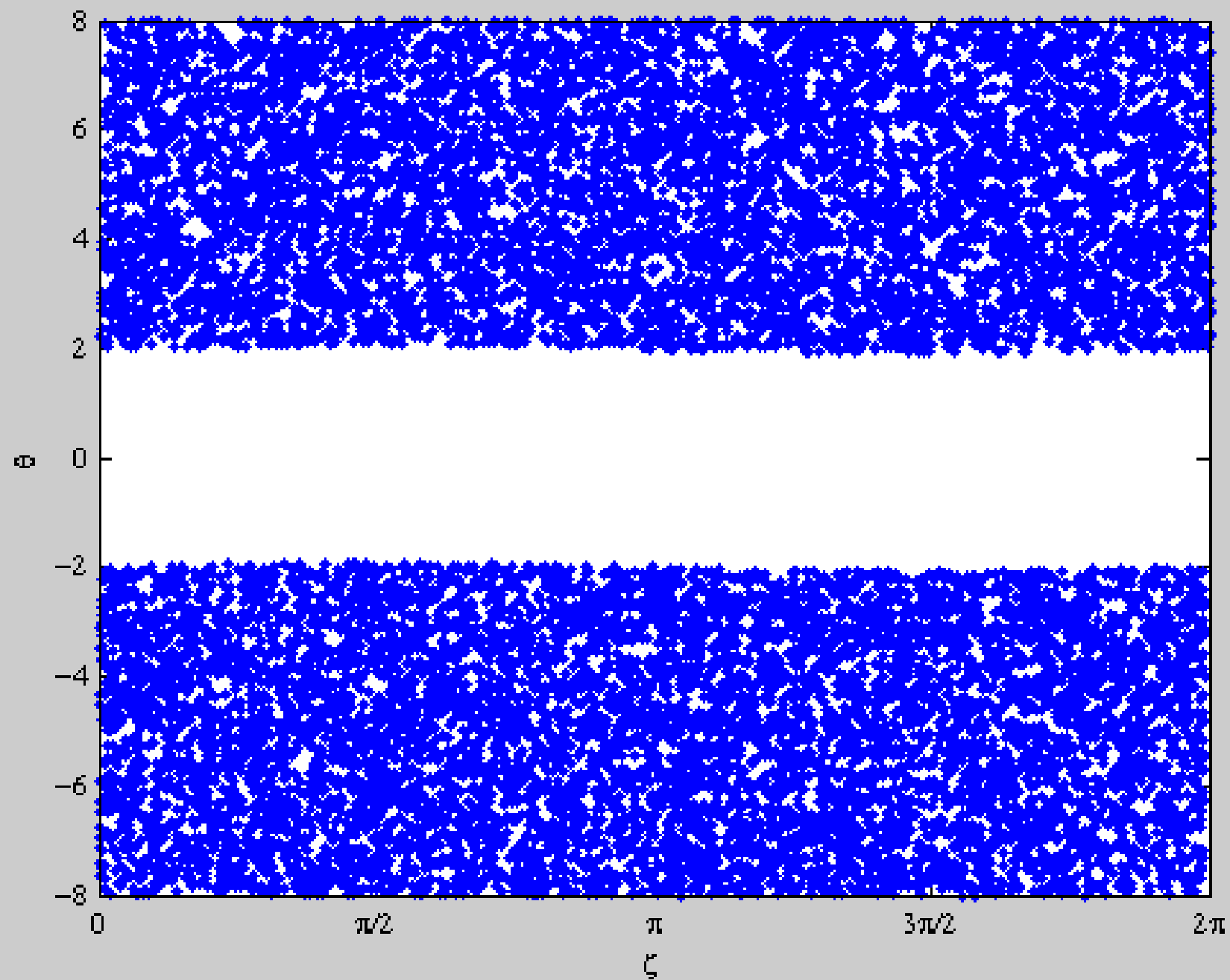
Inhomogeneity Factor

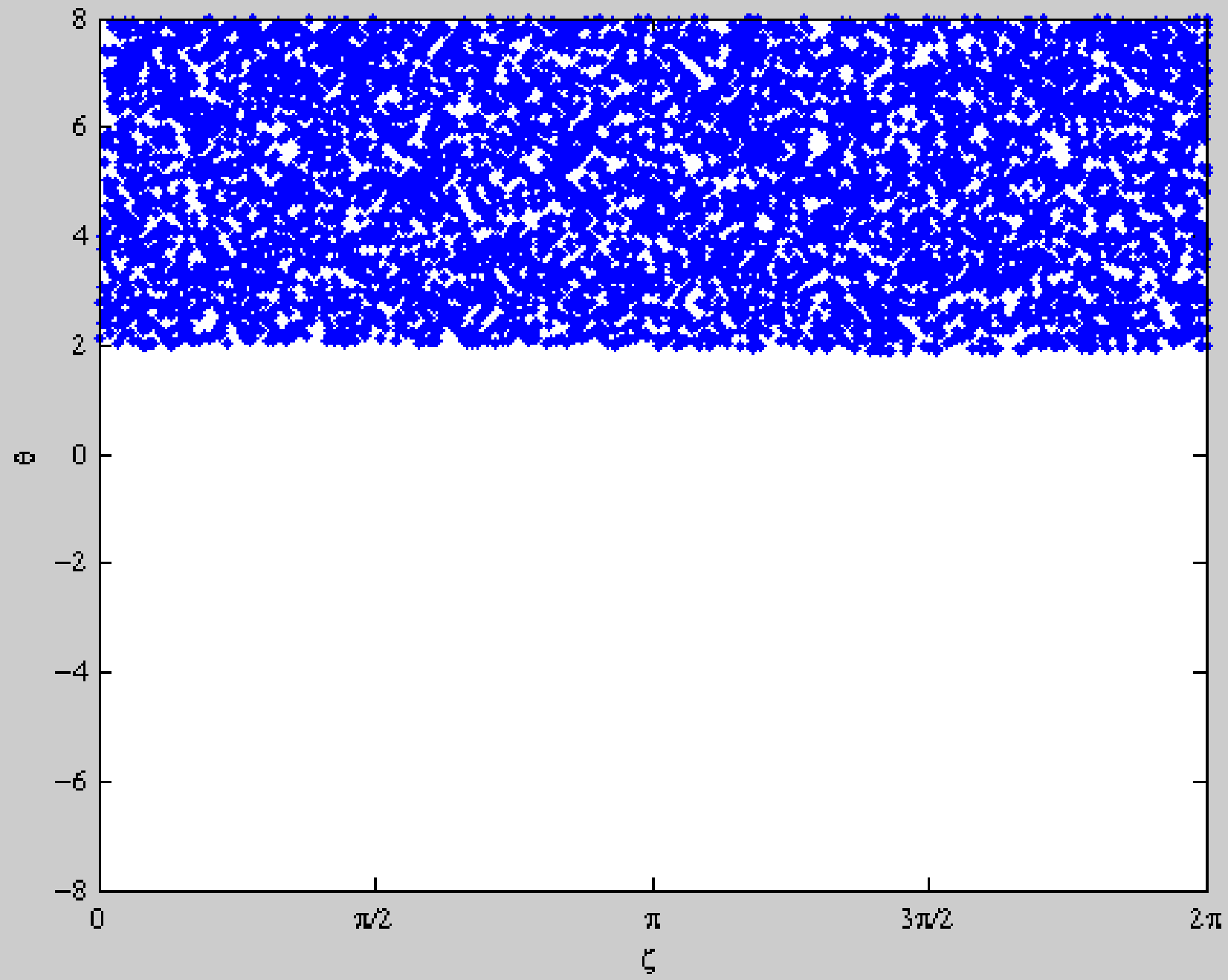
$$S = -\frac{1}{s_0 \omega \Omega_w} \left(s_1 \frac{\partial \omega}{\partial t} + c s_2 \frac{\partial \Omega_e}{\partial h} \right)$$

$$s_0 = \frac{\delta V_{\perp 0}}{\xi c} \quad s_1 = \gamma \left(1 - \frac{V_R}{V_g} \right)^2$$

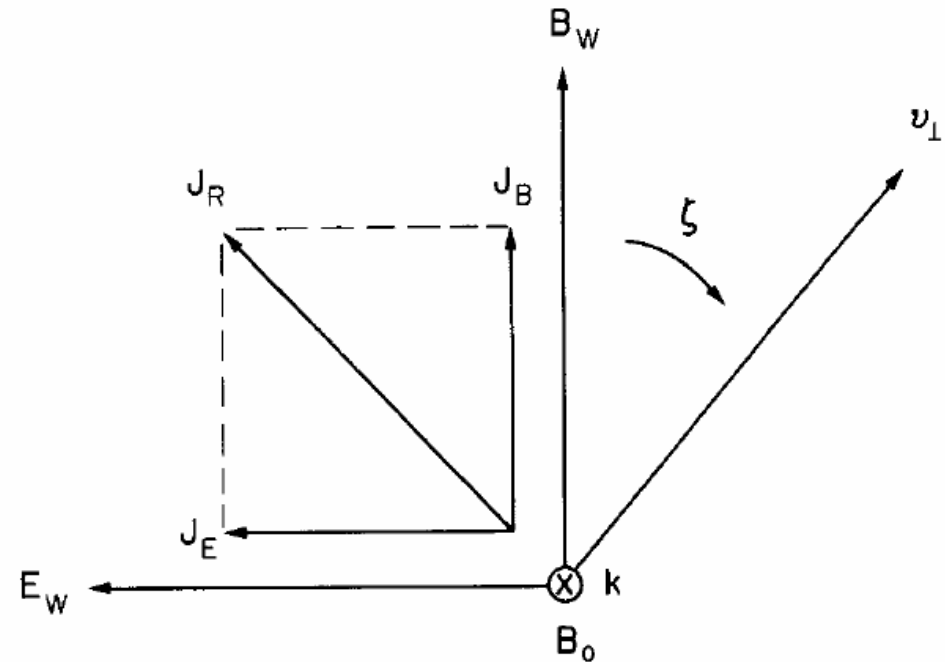
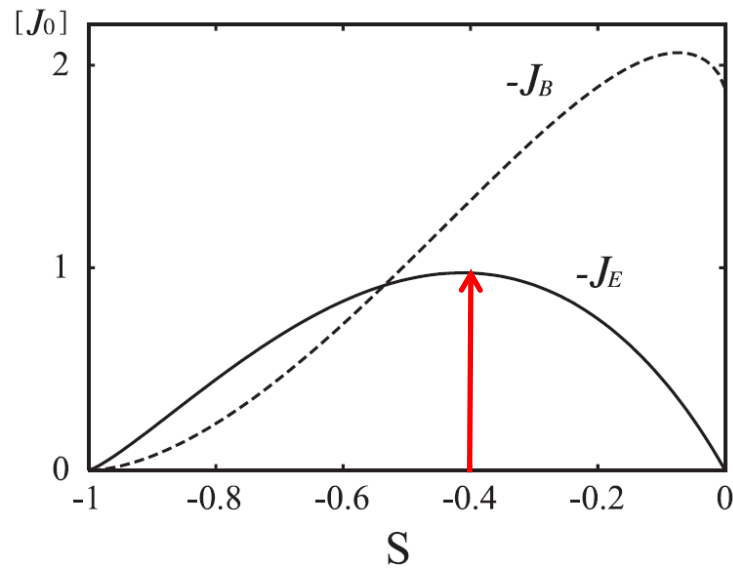
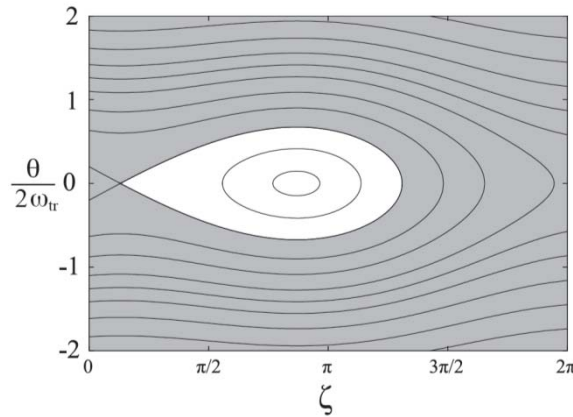
$$s_2 = \frac{1}{2\xi\delta} \left\{ \frac{\gamma\omega}{\Omega_e} \left(\frac{V_{\perp 0}}{c} \right)^2 - \left[2 + \Lambda \frac{\delta^2 (\Omega_e - \gamma\omega)}{\Omega_e - \omega} \right] \frac{V_R V_p}{c^2} \right\}$$

[Omura et al., JGR, 2008; 2009]





Nonlinear Wave Growth due to Formation of Electromagnetic Electron Hole



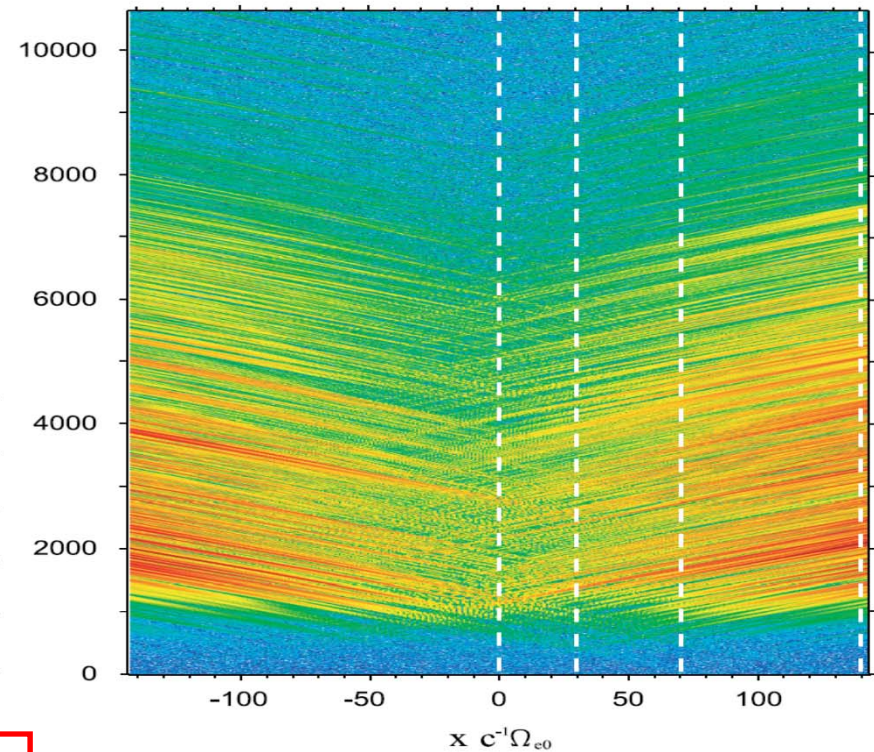
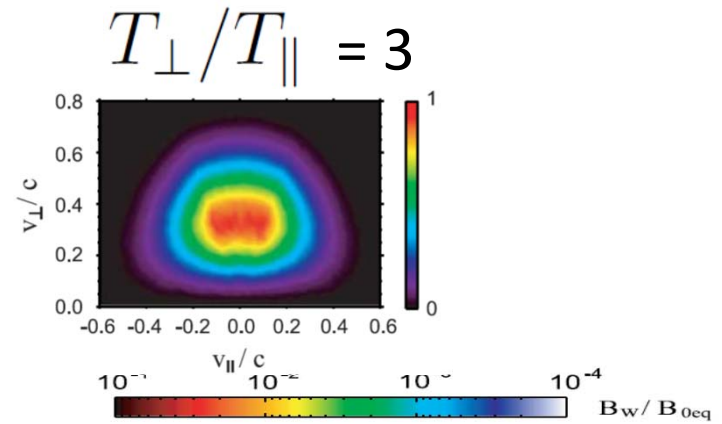
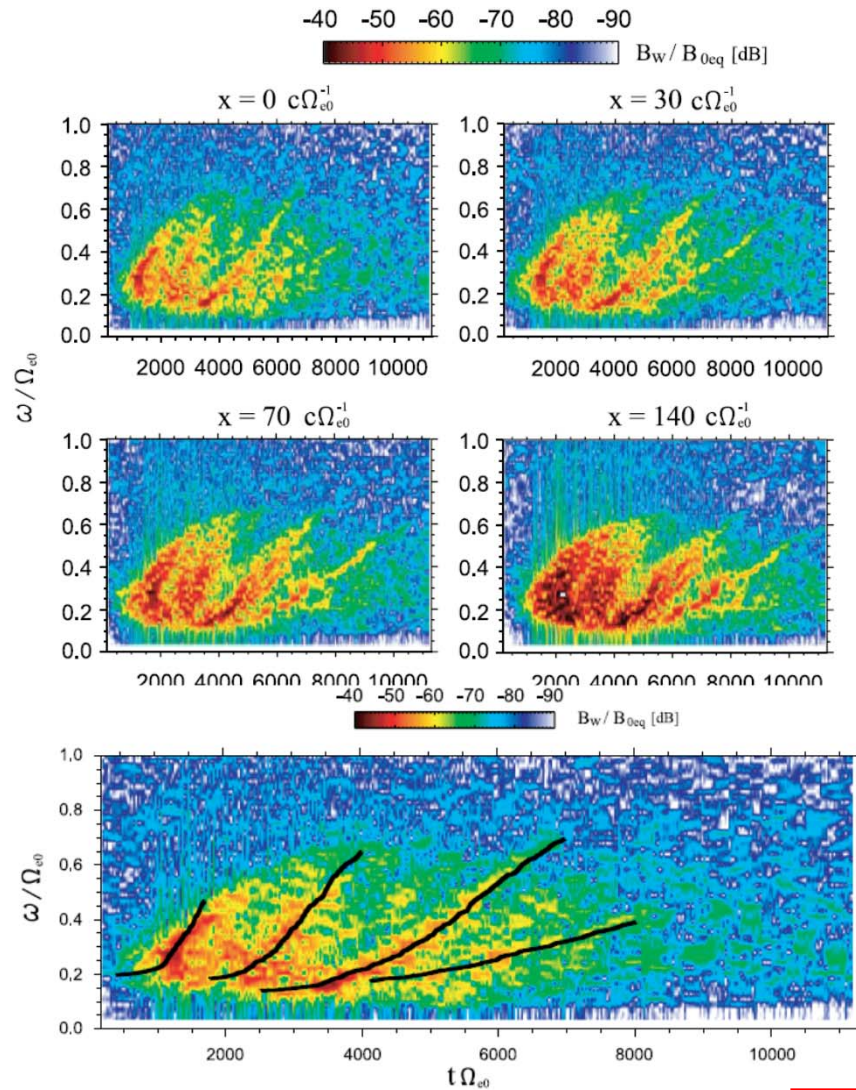
$J_E < 0$: Wave Growth

Maximum $-J_E$

$$S_{EQ} = -0.4$$

[Omura, Katoh, Summers, JGR, 2008]

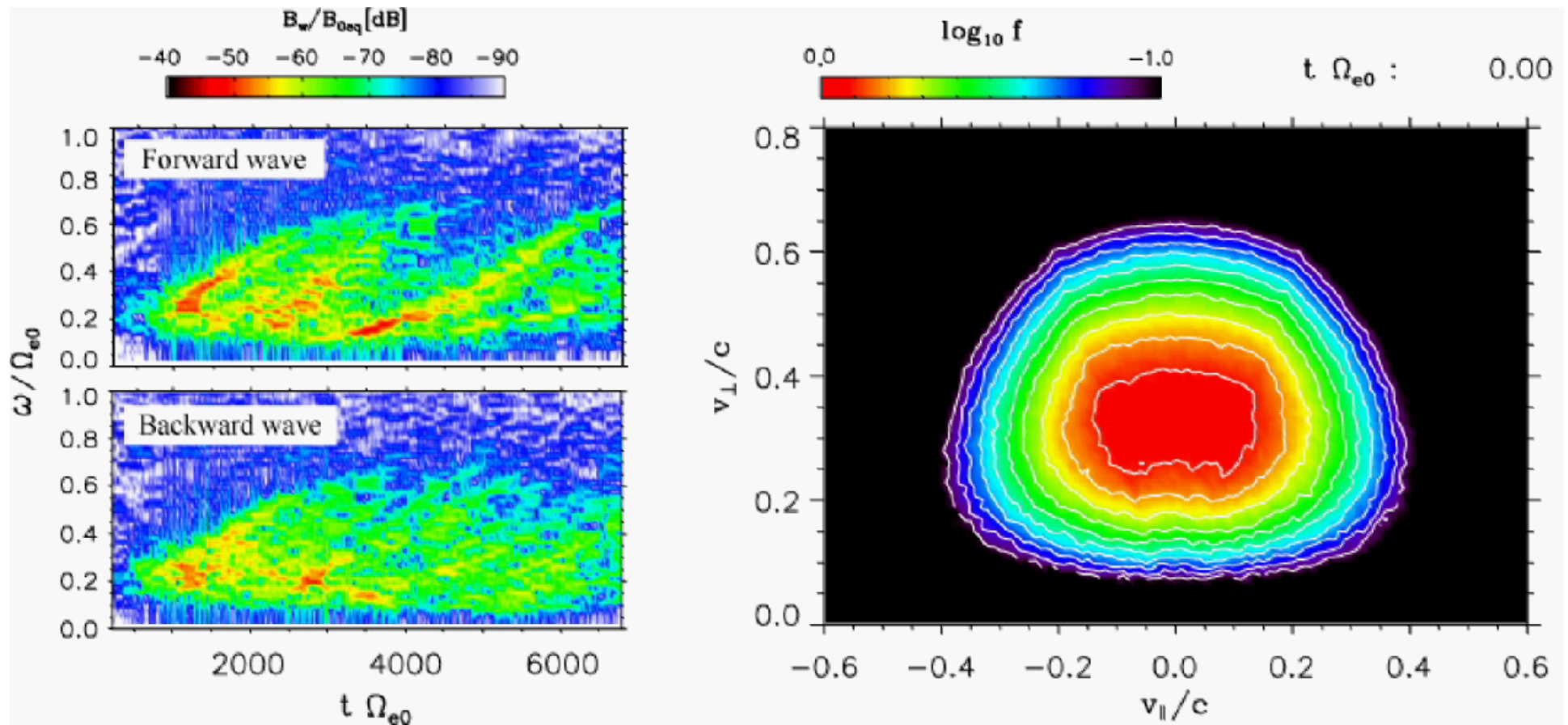
Full-Particle Simulation of Chorus Emission



$$\frac{\partial \omega}{\partial t} = \frac{0.4 \delta V_{\perp 0}}{\gamma \xi} \frac{\omega}{c \Omega_{e0}} \left(1 - \frac{V_R}{V_g}\right)^{-2} \frac{B_w}{B_{0eq}} \Omega_{e0}^2$$

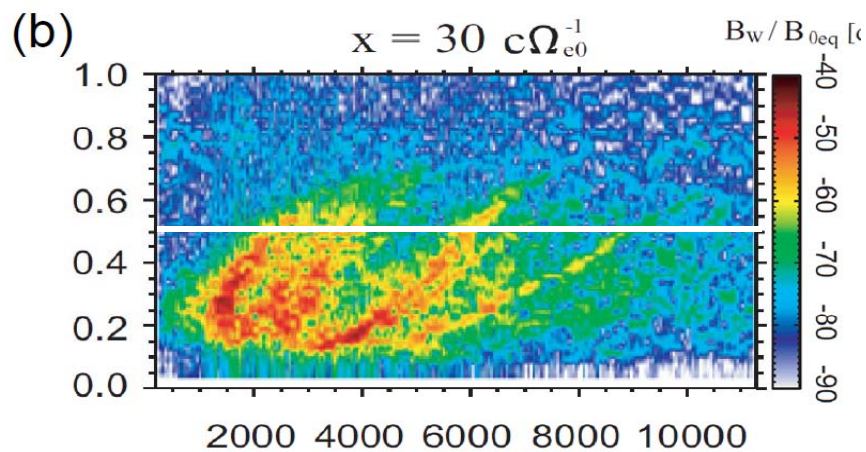
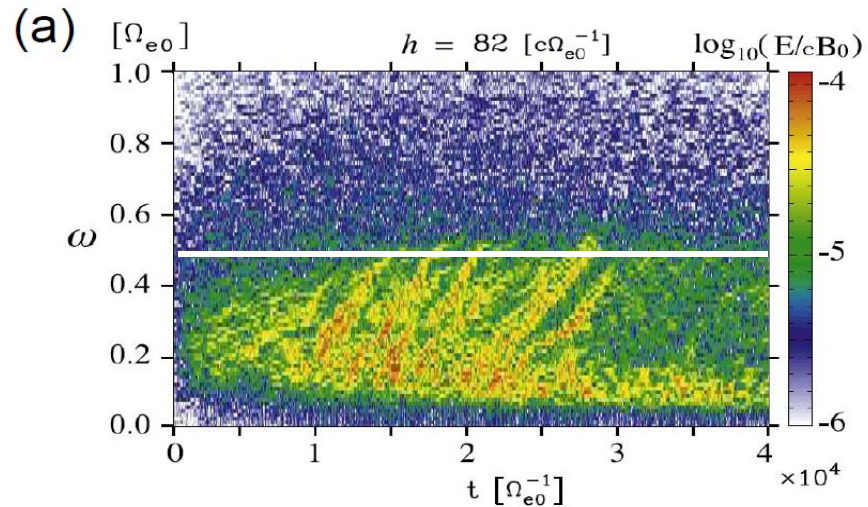
[Hikishima et al., JGR, 2009a]

Formation of Pancake Distribution through generation of Chorus emission



[Hikishima et al., JGR, 2009b]

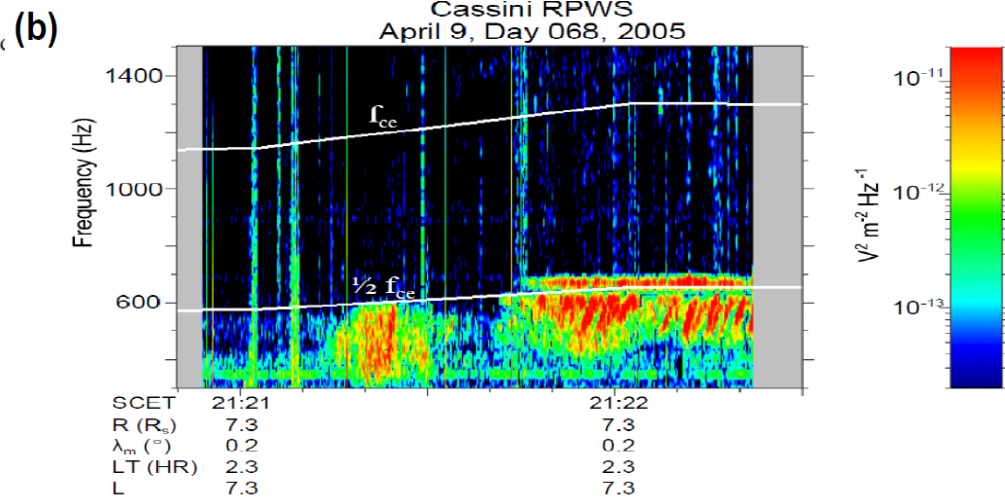
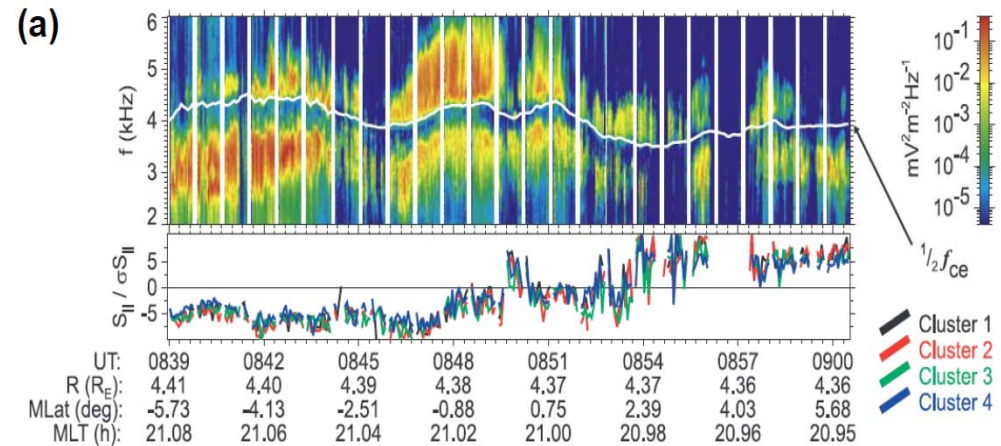
Simulations : parallel propagation



[Omura et al., JGR, 2008]

[Hikishima et al., JGR, 2009]

Observations: oblique propagation



[Santolik, et al., JGR, 2003]

[Hosphodarsky et al., JGR, 2008]

Quasi-parallel Propagation (**Oblique**) $\sin^2 \Psi \ll 1$

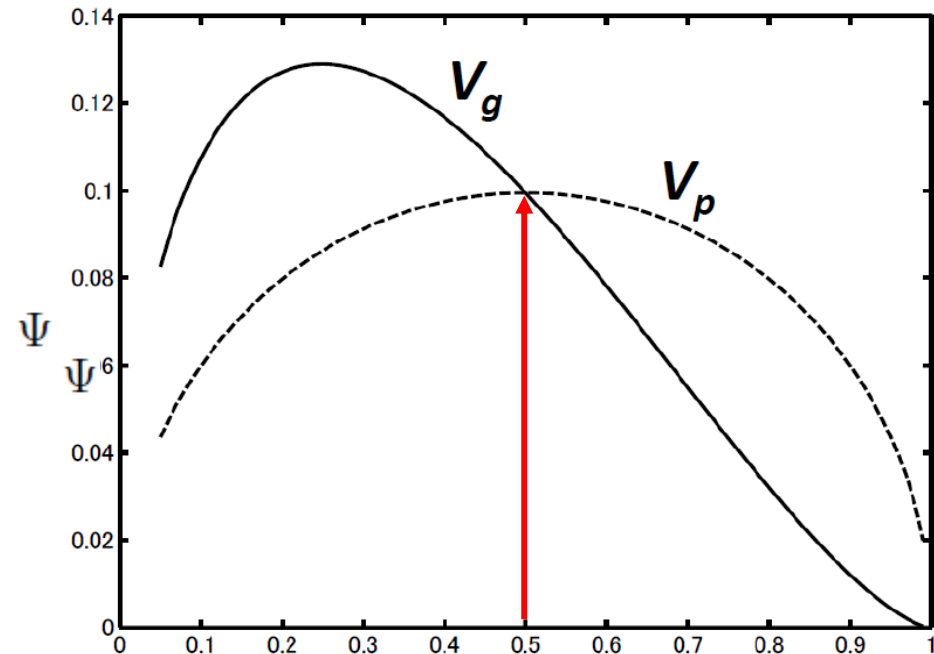
$$E_{w\parallel} = \frac{\omega \sin \Psi}{\delta^2 \Omega_e - \omega} E_w$$

Ψ : Wavenormal Angle

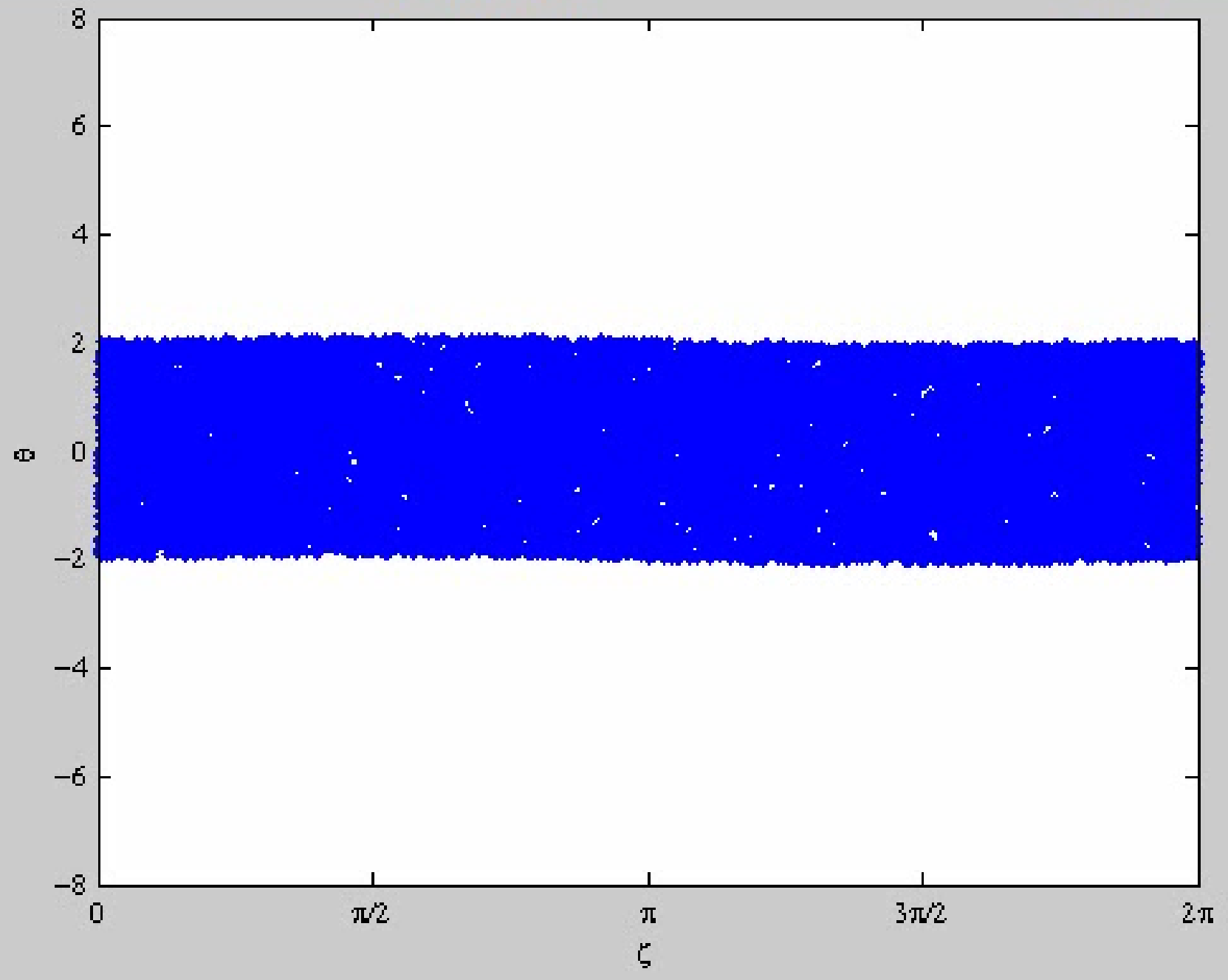
With $\omega = 0.5 \Omega_e$

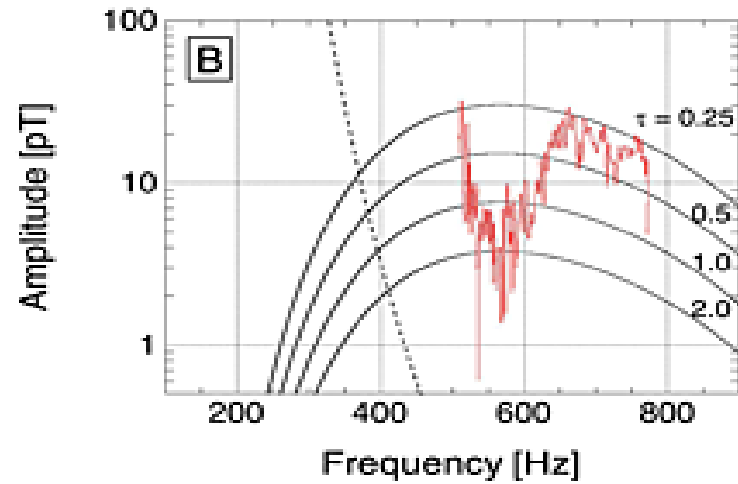
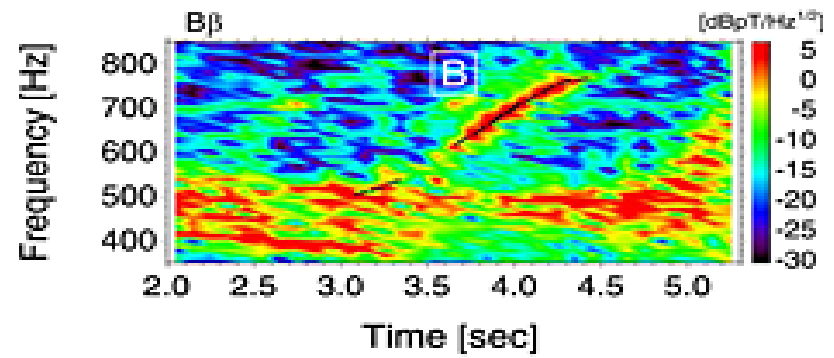
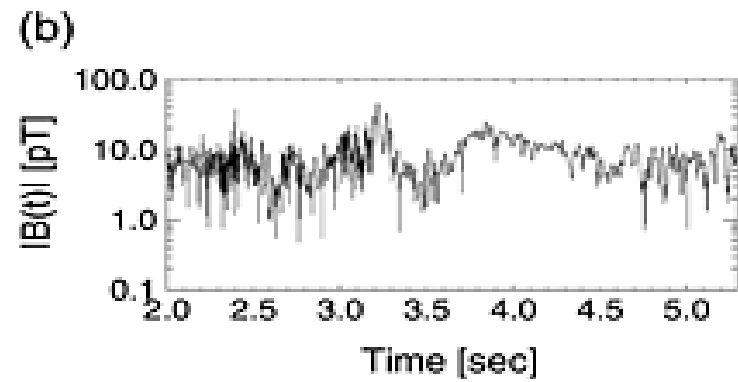
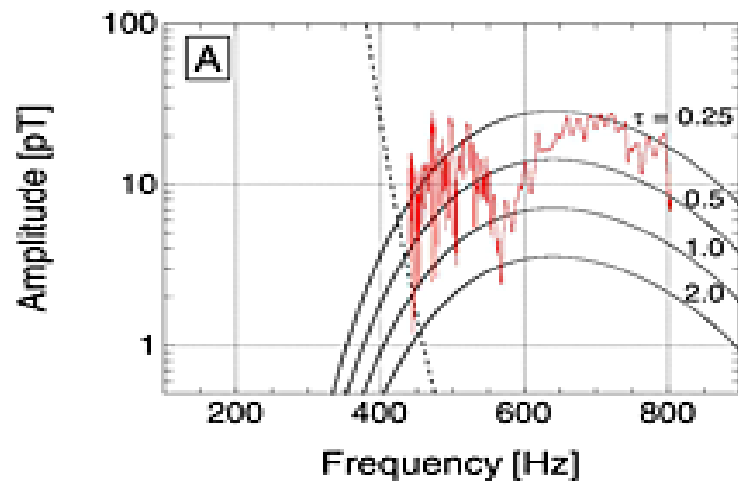
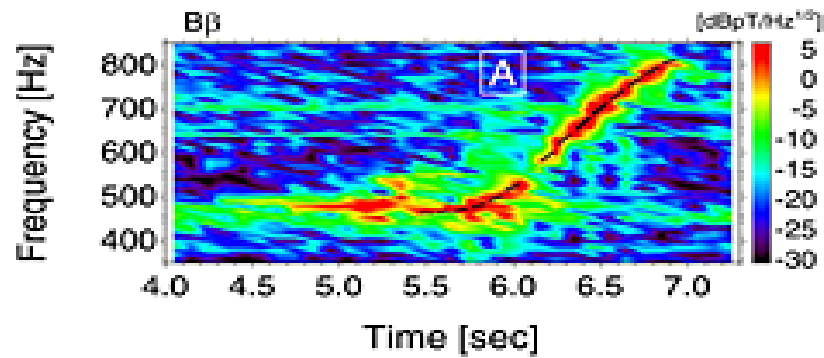
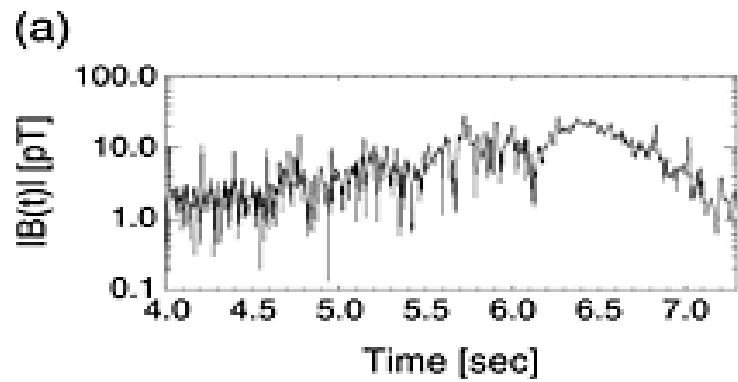
$$V_g = V_p$$

$$\tilde{v}_{\parallel} = v_{\parallel} - V_p$$

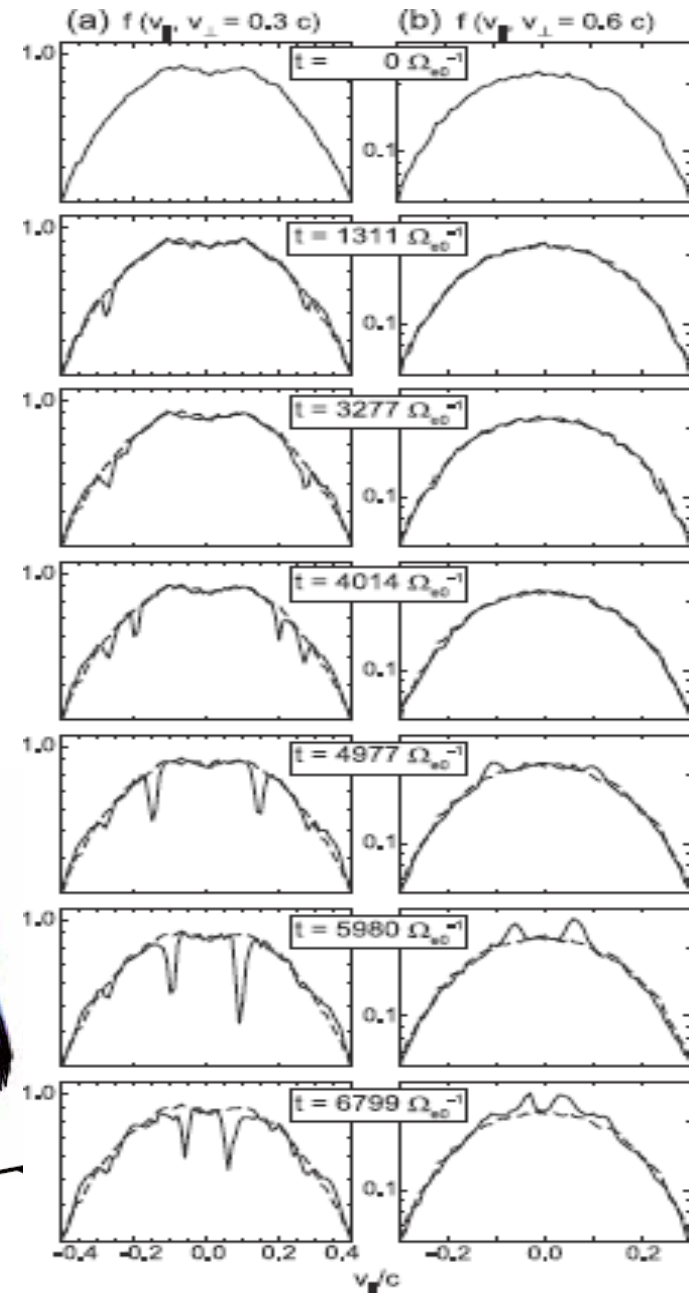
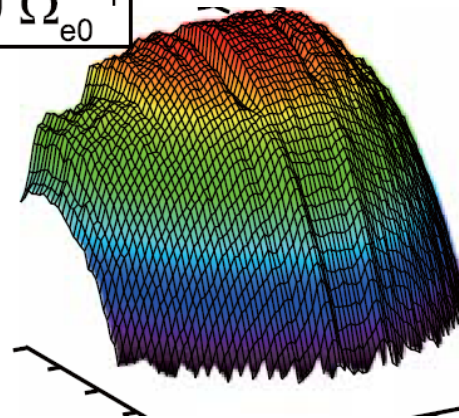
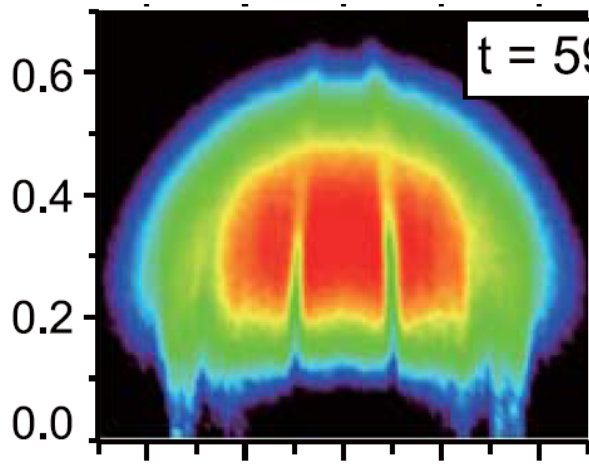
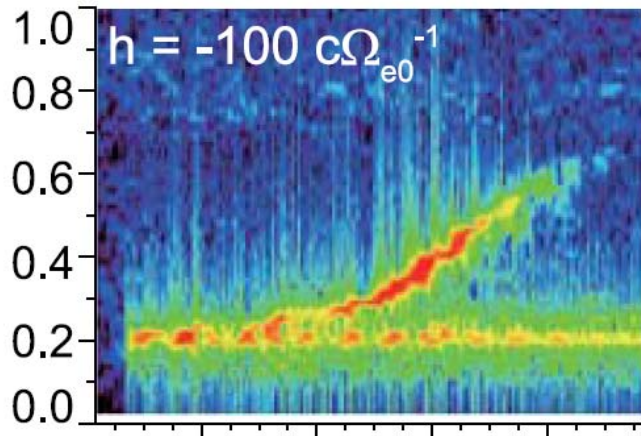


$$\frac{d\tilde{v}_{\parallel}}{dt} = -\frac{eE_{w\parallel}}{\gamma m_0} \sin \phi - \frac{v_{\perp}^2}{2\Omega_e} \frac{\partial \Omega_e}{\partial h}$$



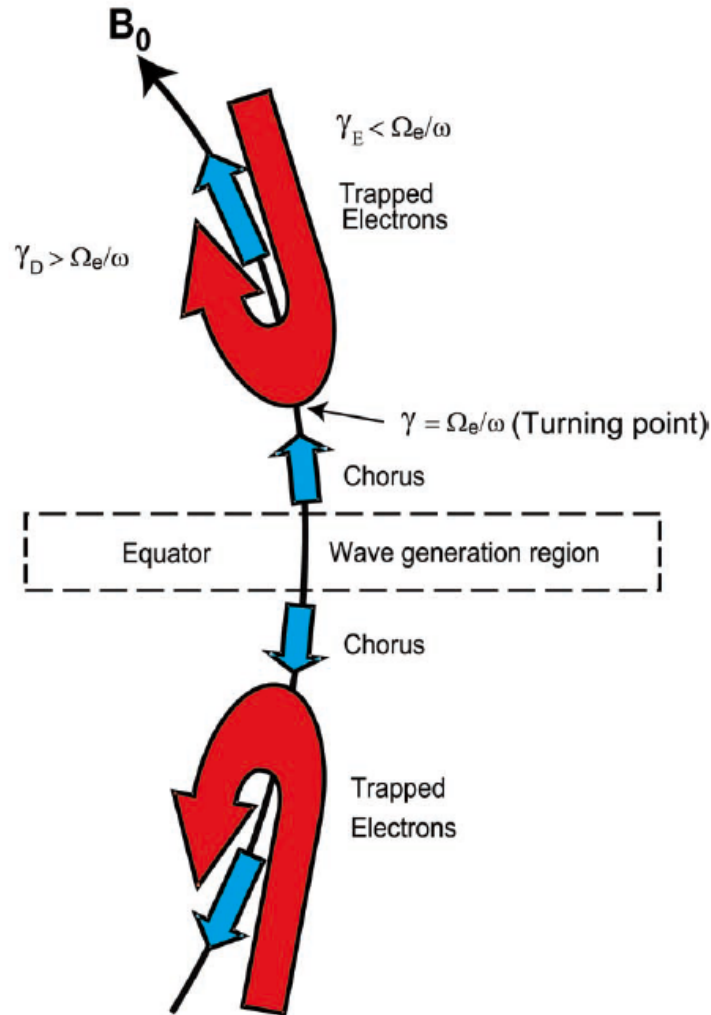


Formation of Electron Hole and Bump

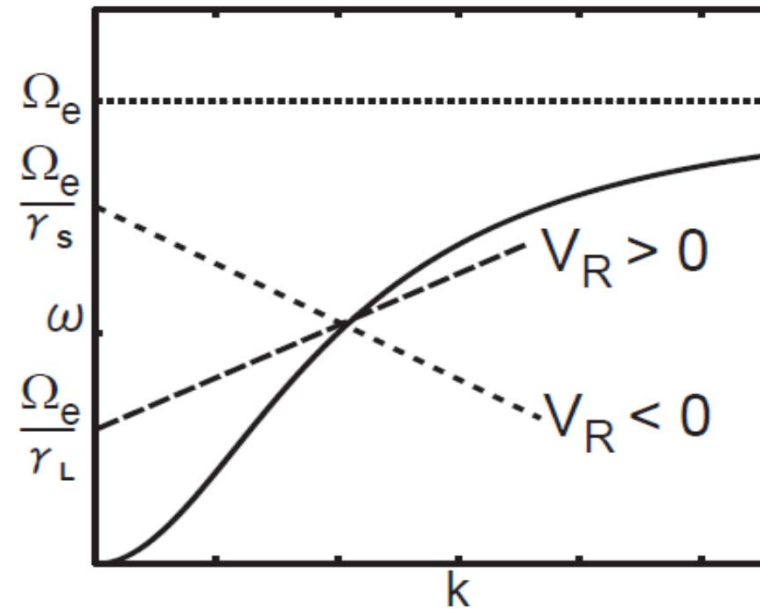


[Hikishima et al., JGR, 2010]

Relativistic Turning Acceleration



$$V_R = \frac{\omega}{k} \left(1 - \frac{\Omega_e(h)}{\omega \gamma} \right)$$

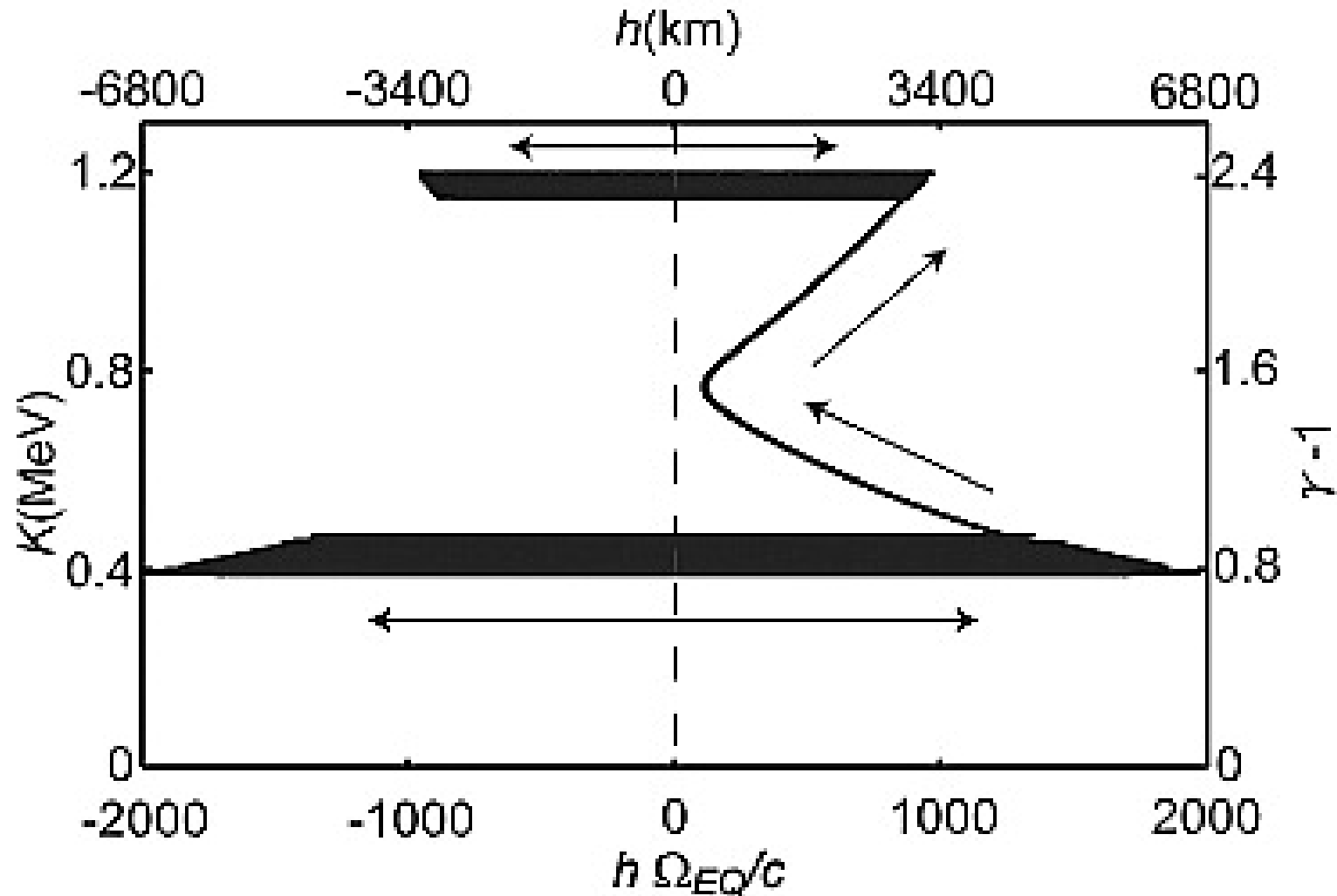


Ultra-Relativistic Acceleration

$$\gamma \geq \Omega_e(h)/\omega \Rightarrow V_R \geq 0$$

Trajectories of Resonant Electrons (400 keV)

Relativistic Turning Acceleration (RTA)



Bw = 125 pT

$$\omega_p = 2.0\Omega_{e0}$$

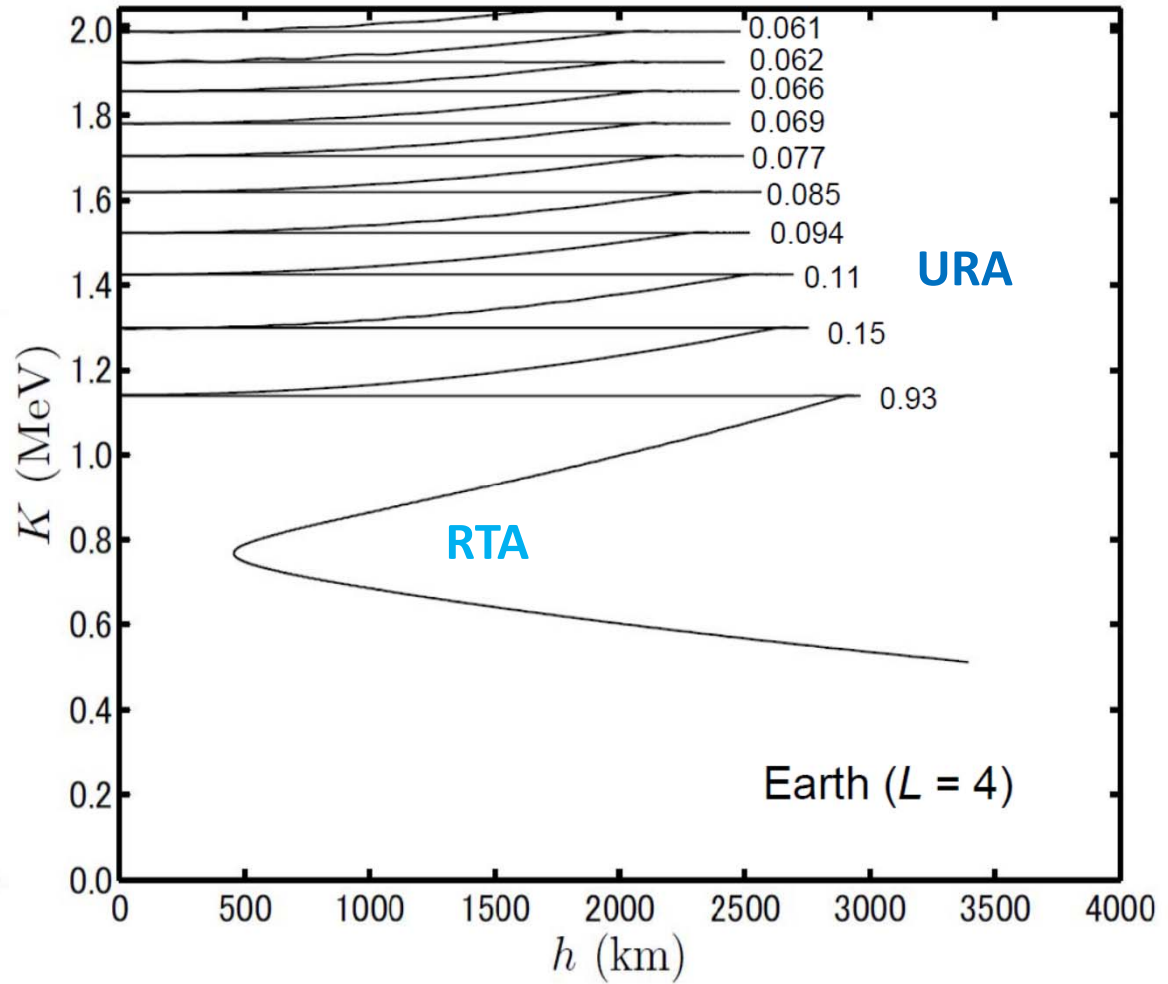
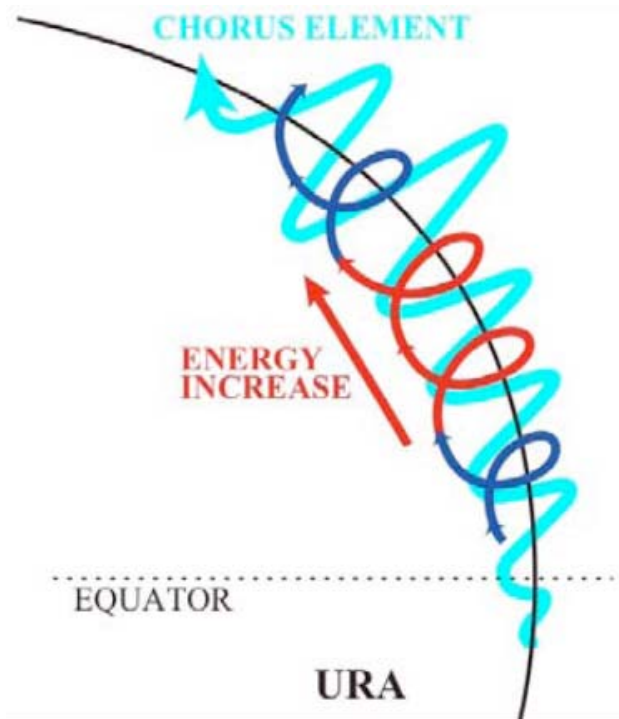
$$\omega = 0.4\Omega_{e0}$$

[Omura, et al., JGR, 2007]

Ultra-Relativistic Acceleration (URA)

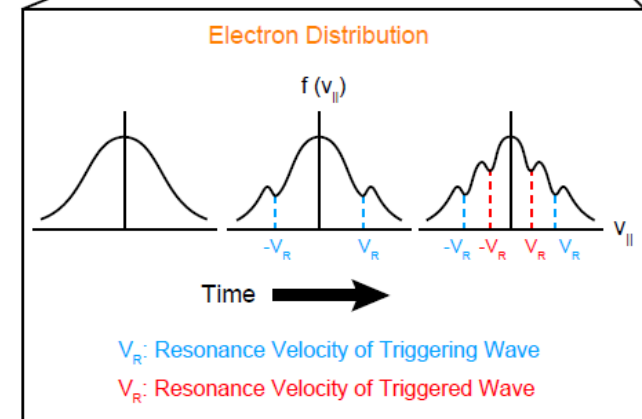
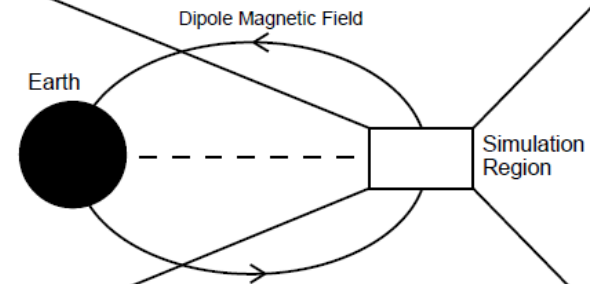
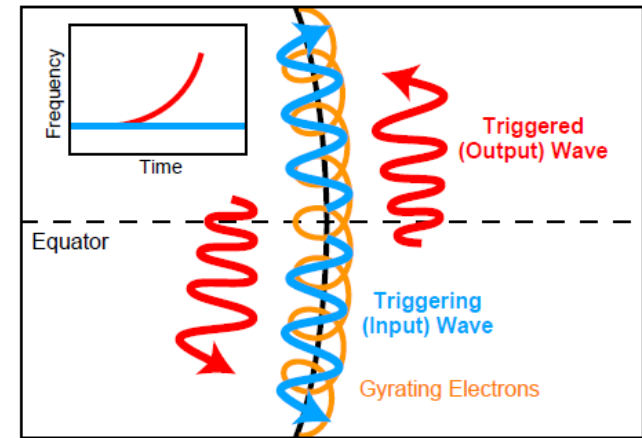
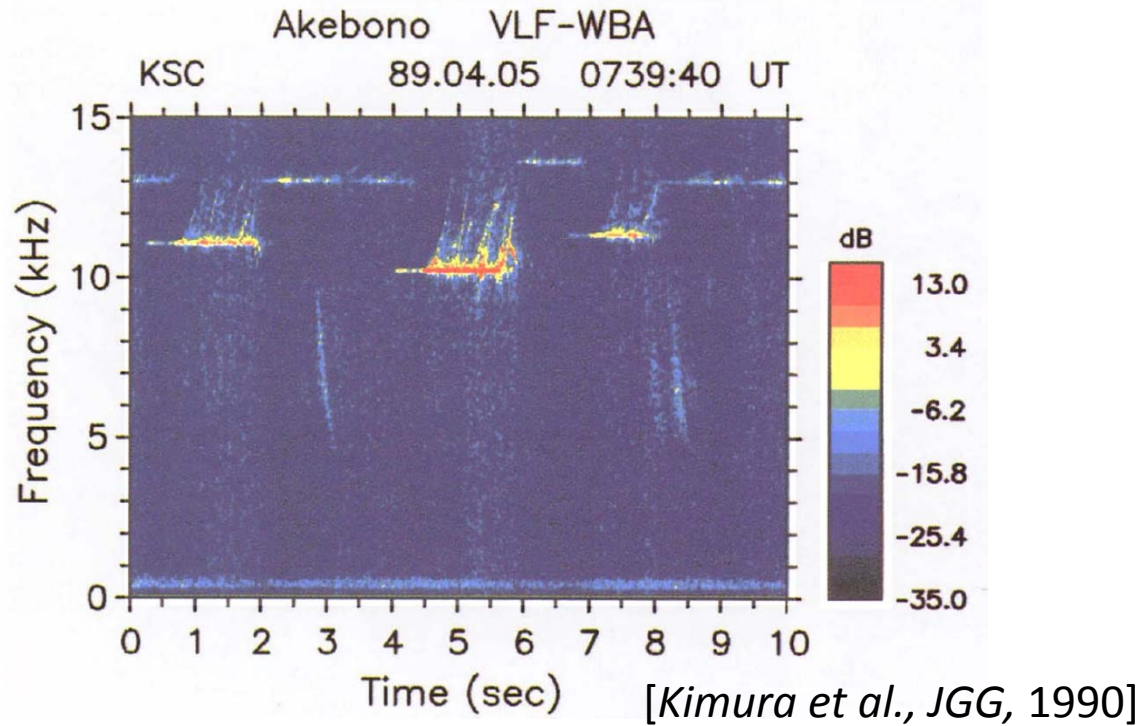
$$\gamma_0 > \Omega_{EQ}/\omega$$

$$V_{R0} > 0$$

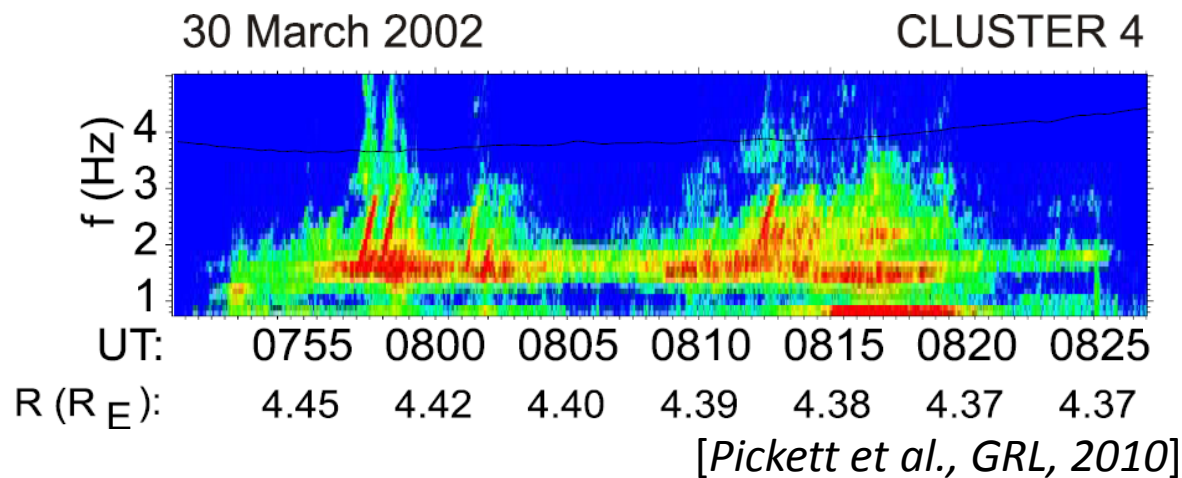


[Summers and Omura, GRL, 2007]

Whistler-mode Triggered Emissions

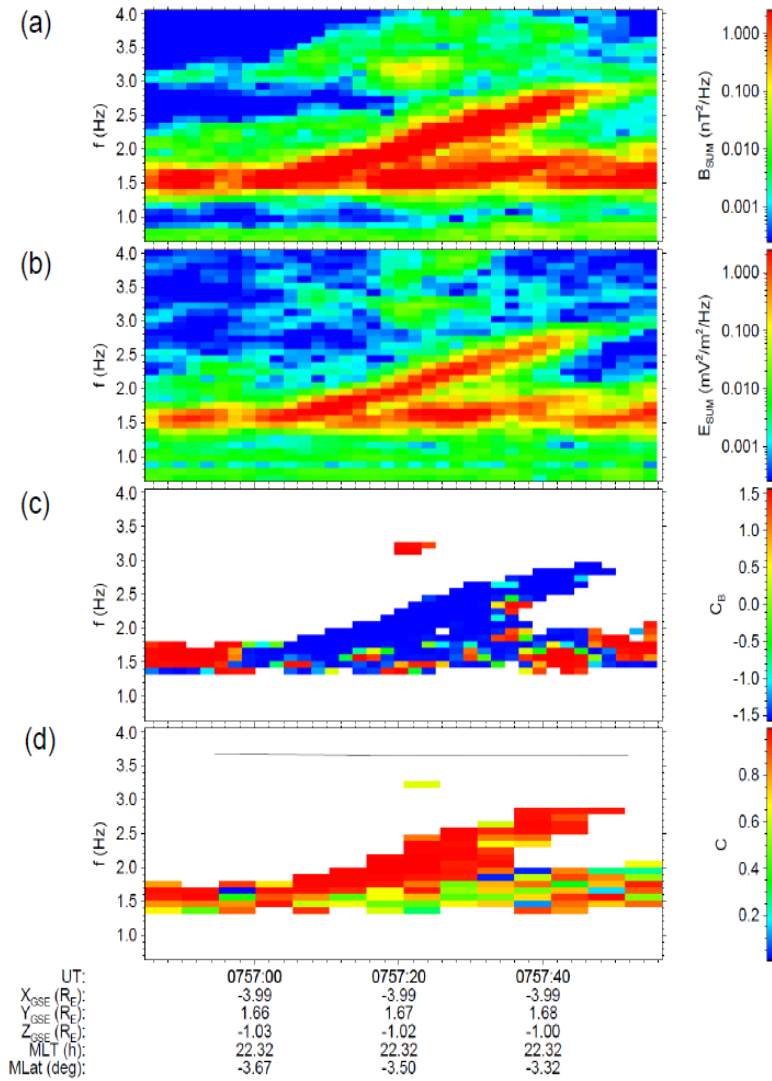


EMIC Triggered Emissions



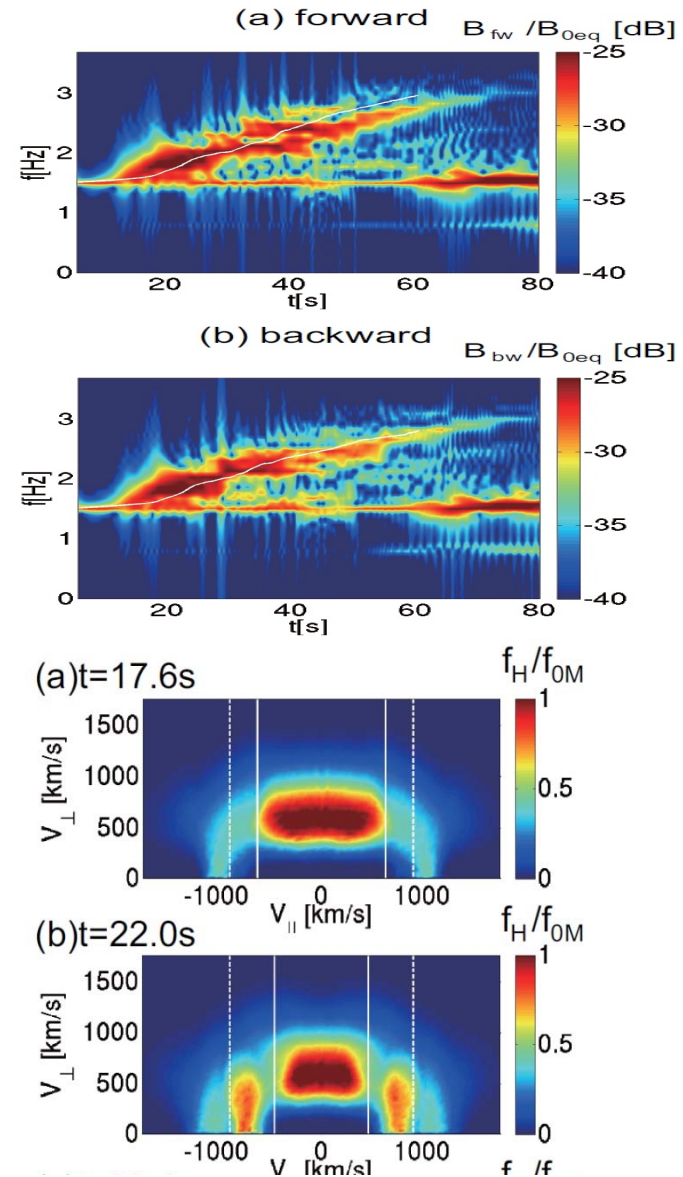
EMIC Triggered Emissions

Cluster Spacecraft Observation



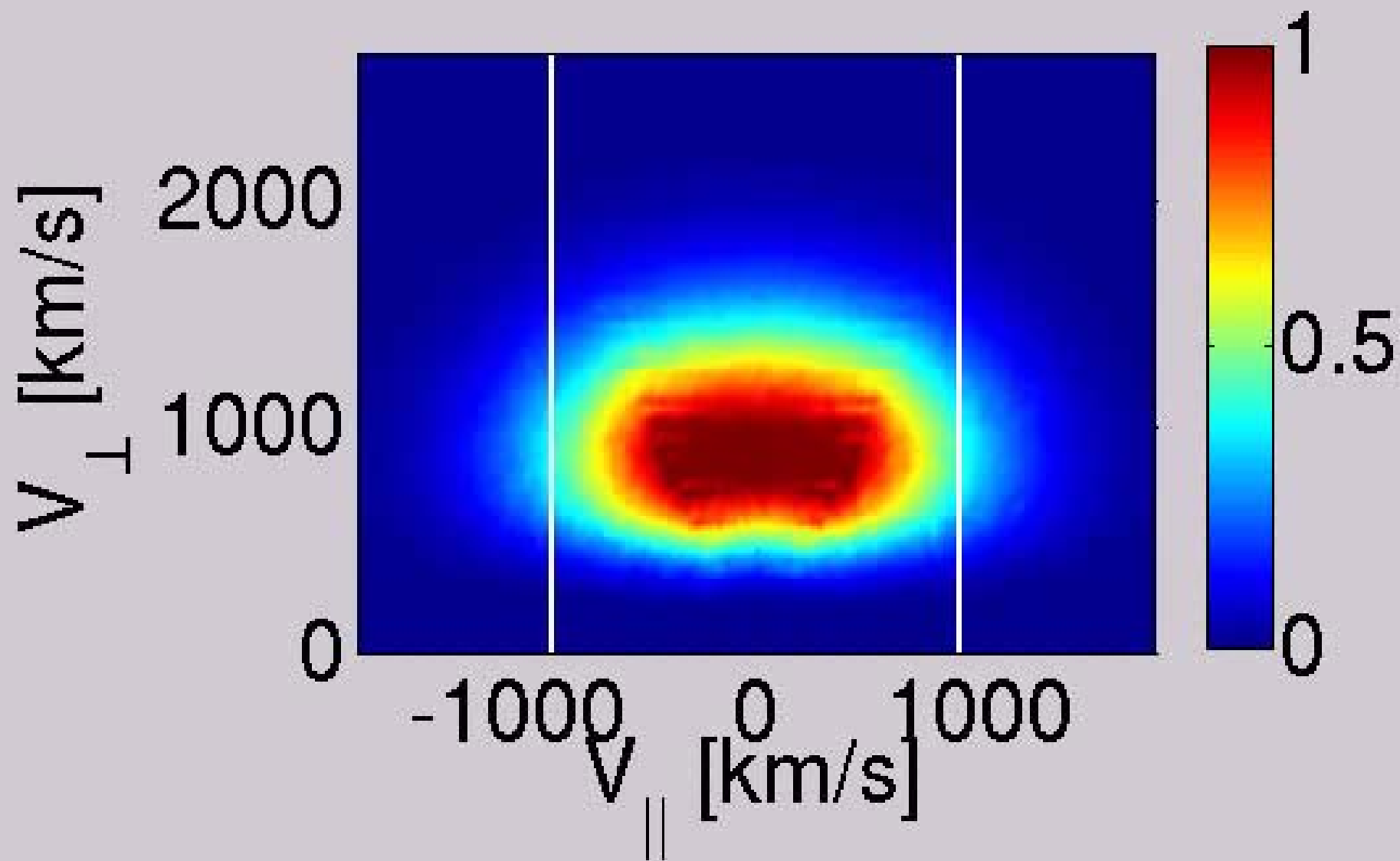
[Omura et al., JGR, 2010]

Hybrid Code Simulation



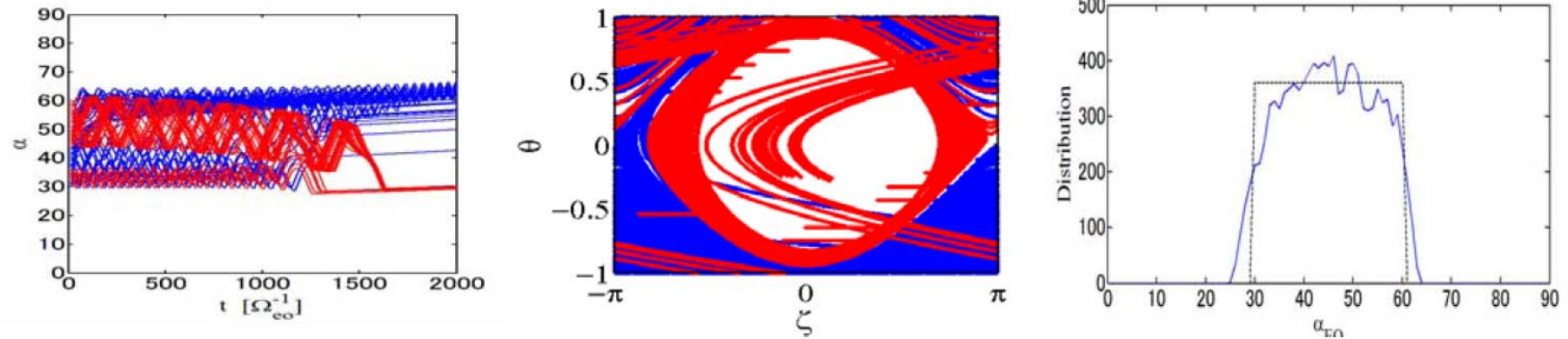
[Shoji and Omura, JGR, 2011]

t=0s

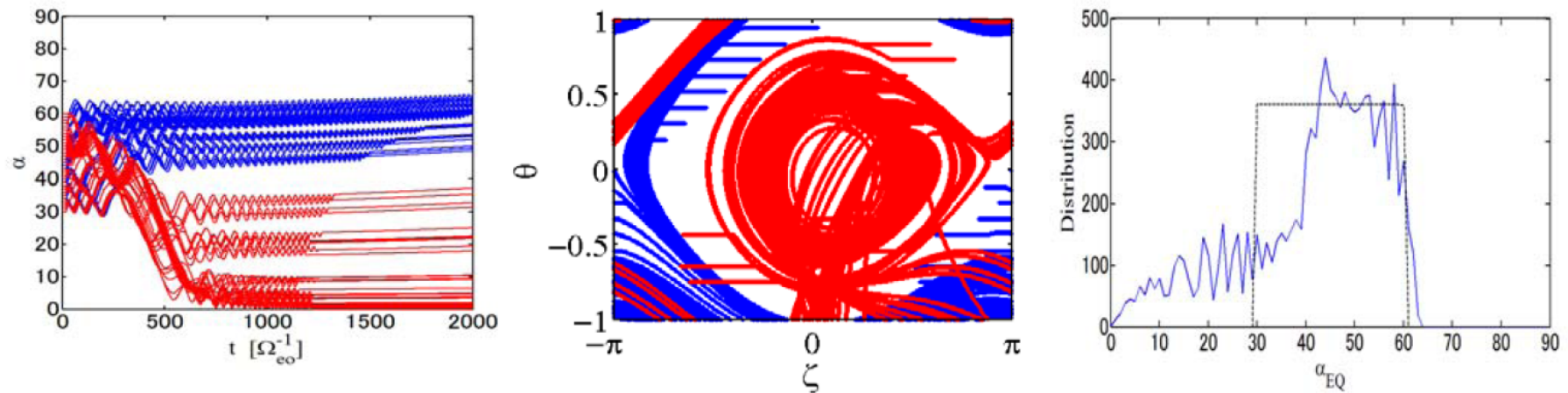


Test Particle Simulation of EMIC Wave-Electron Interaction

(a) Case A (0.98MeV, 2.8Hz-2.8Hz, $a = 0.8e-7$)

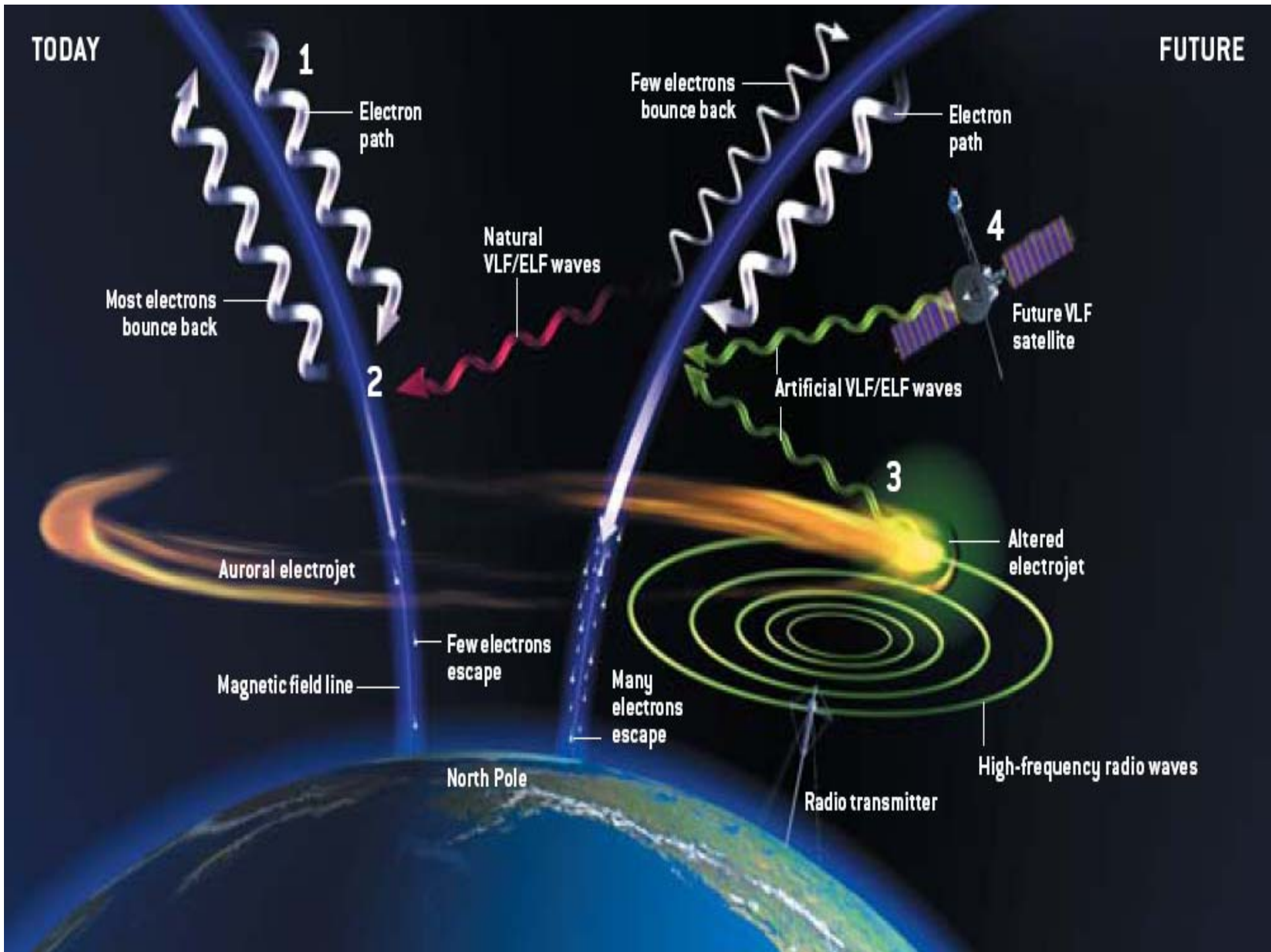


(d) Case D (0.98MeV, 2.8Hz-1.7Hz, $a = 0.8e-7$)



TODAY

FUTURE



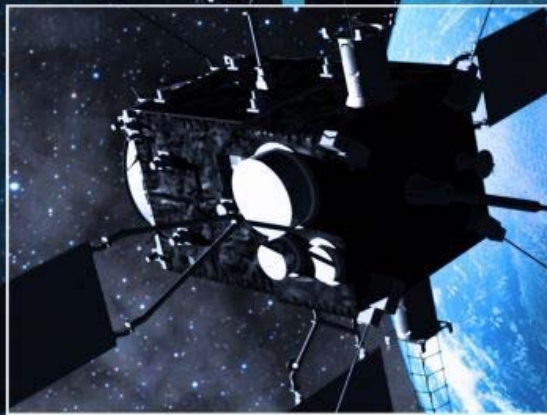
2. *ERG* Project Group

Science Core Team
Science Center

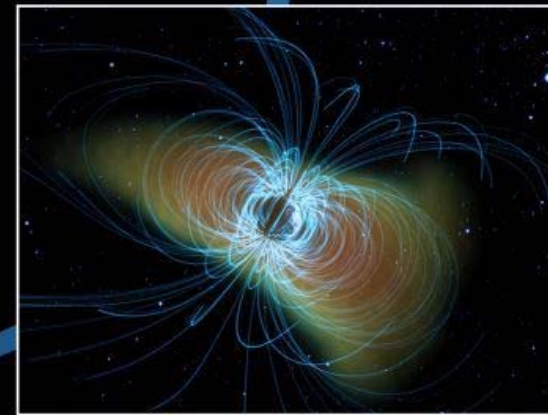


Geospace remote sensing from Ground

ERG Project Team



In-situ observation

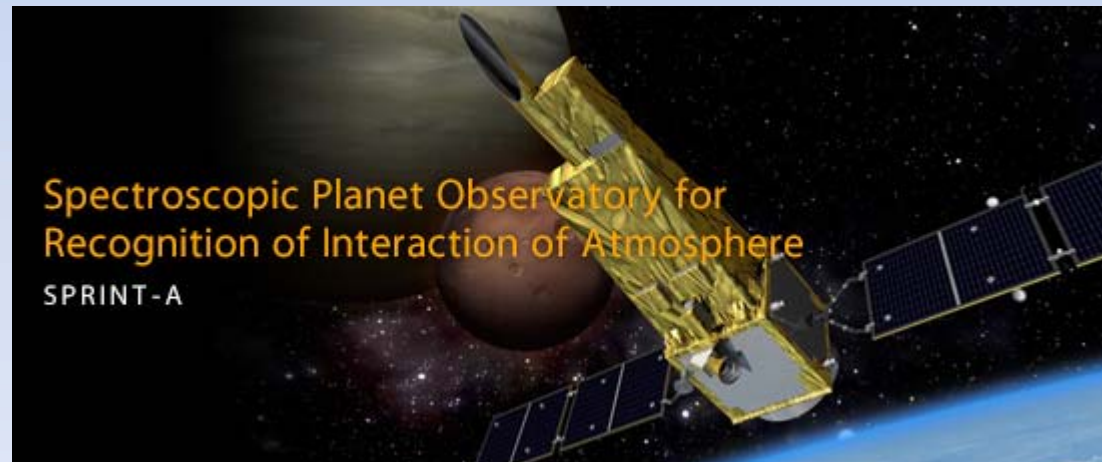


Simulation/Integrated Studies

First launch of the Epsilon launch vehicle on September 13, 2013.

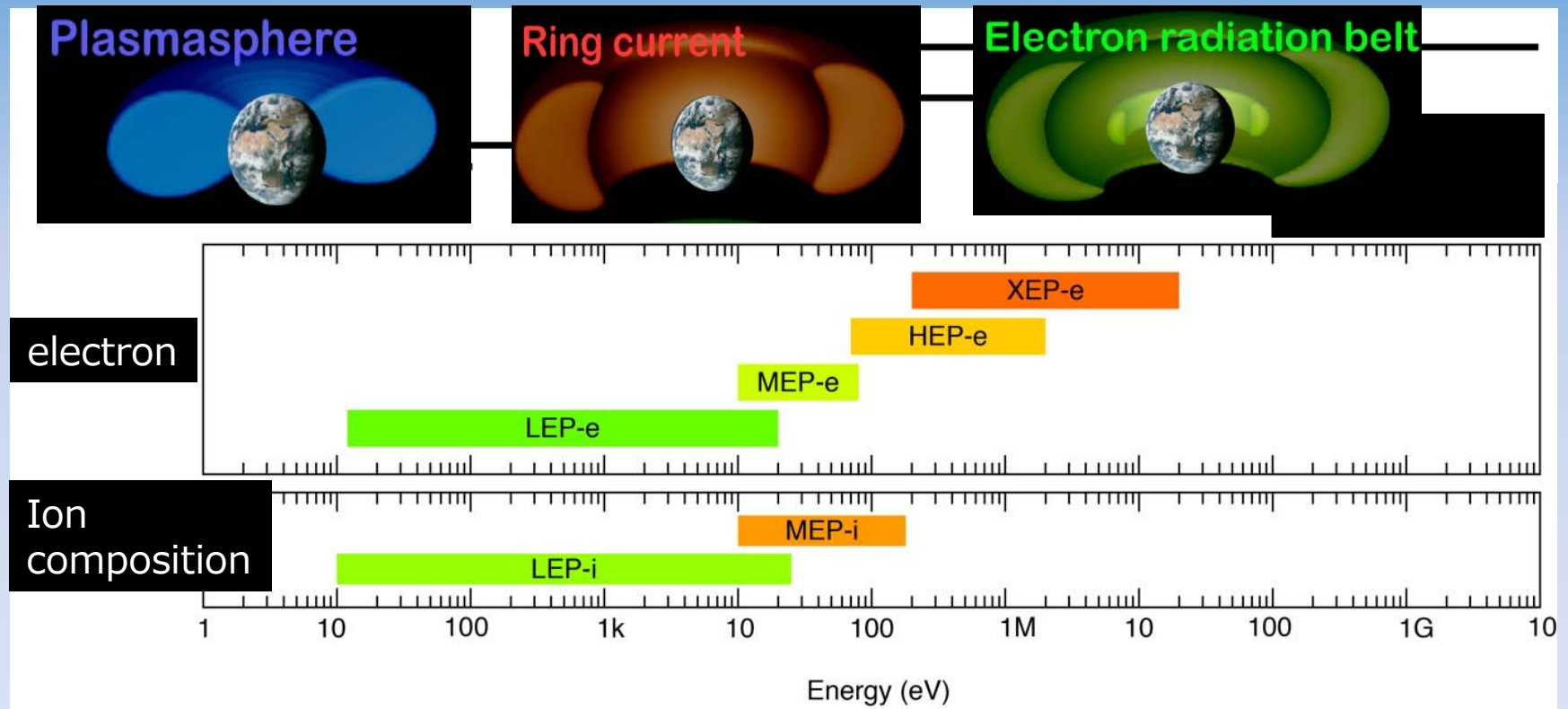


- Hisaki [Spectroscopic Planet Observatory] was successfully launched Epsilon that is newly developed solid rocket on Sep. 13, 2013.
- ERG is the second M-class mission to be launched by Epsilon.



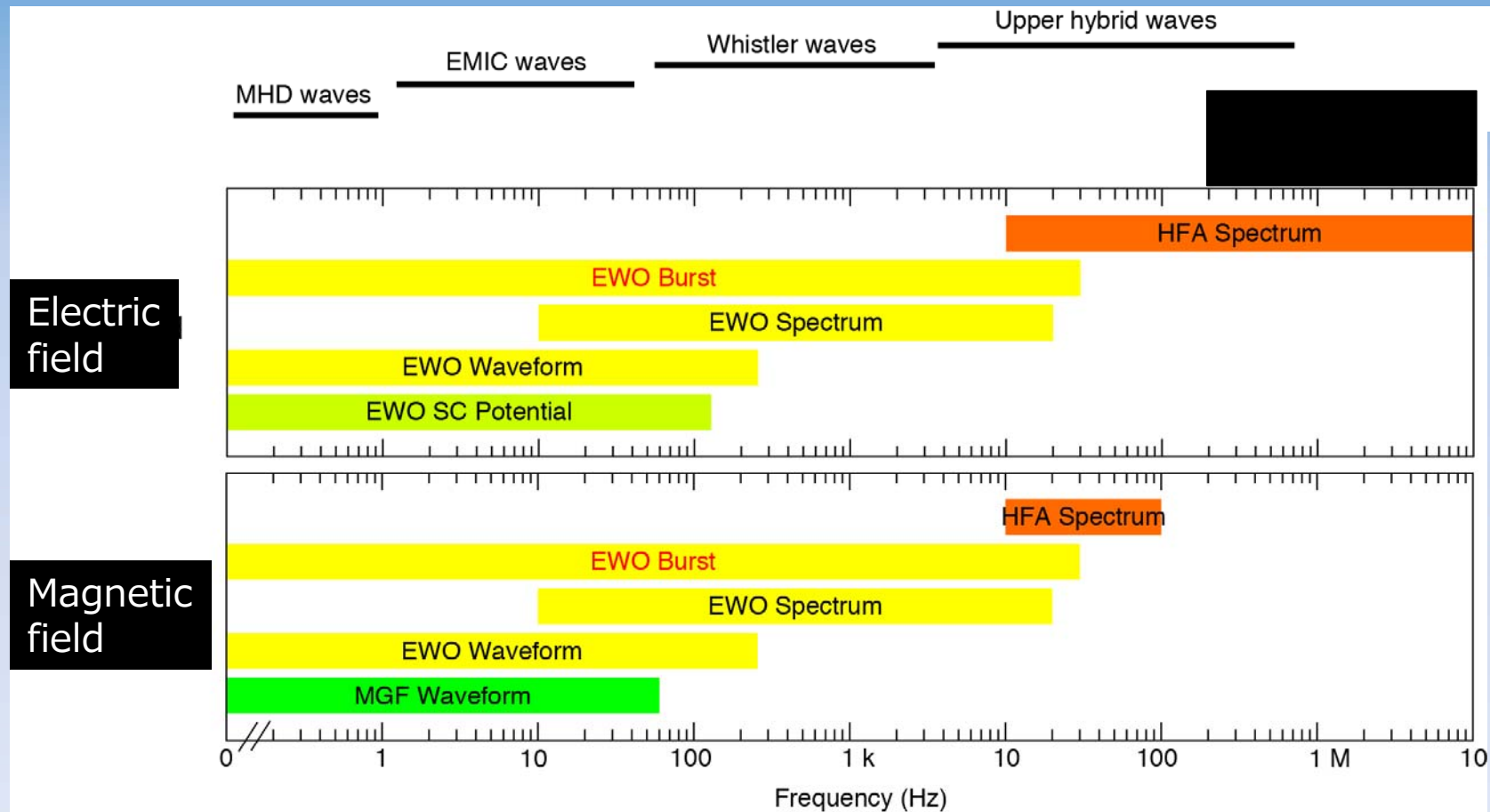
ERG: plasma & particles

PPE: Plasma and Particle Experiment Suite



ERG: Field and Waves

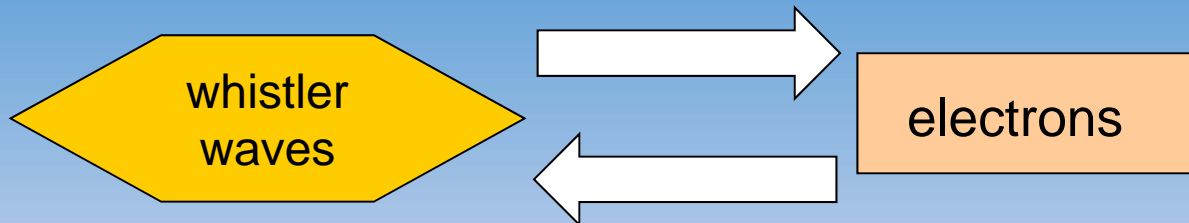
PWE: Plasma Wave and Electric Field Experiment
MGF: Measurement of Geomagnetic Field



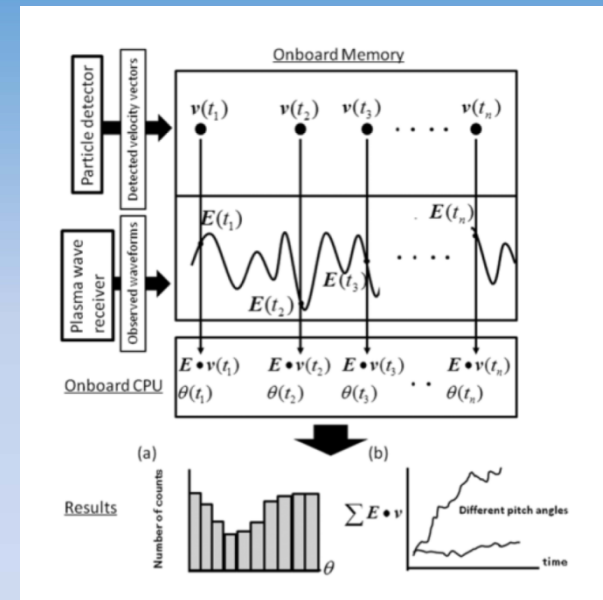
Wave-Particle Interaction Analyzer

S-WPIA: Software-type Wave Particle Interaction Analyzer

Direct measurement of energy transfer between whistler waves and electrons is essential to understand wave-particle interactions.



$$\frac{dK}{dt} = qE \cdot v = |E| |v| \sin \theta$$



Phase difference θ determines the direction of energy transfer.
(Electrons generate waves or Waves accelerate electrons)

ERG-satellite will directly measure the energy transfer between whistler waves and electrons in space for the first time.

Mission Status & Schedule

- FY 2009 - Mission Definition Review.
System Requirement Review.
- FY 2011 - System Definition Review
- FY 2012 - Preliminary Design Review
- FY 2013 - Critical Design Review
- FY 2014-15 - Development of the flight model
- 2016 - Launch of the satellite

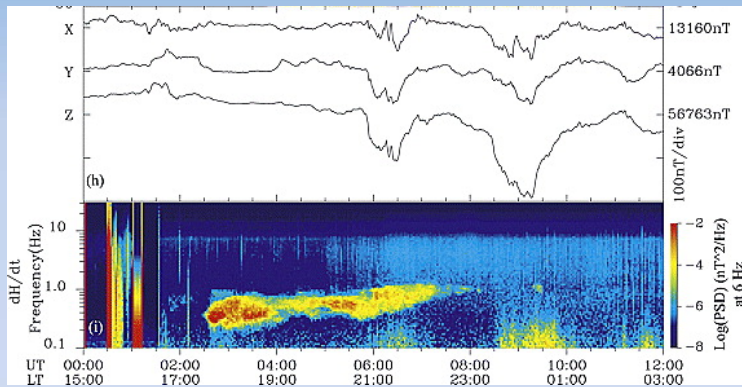
The **ERG** ground networks : waves

• Radar Network: SuperDARN network



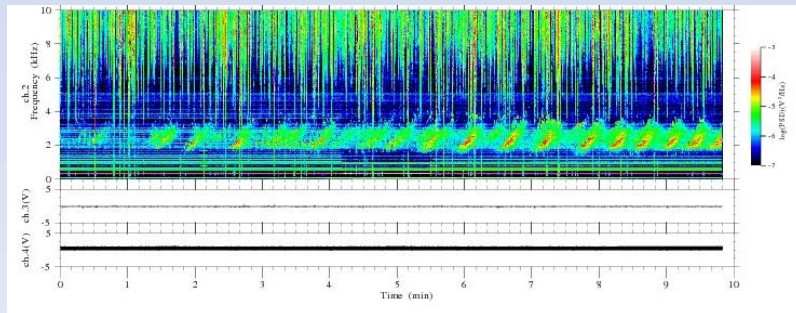
- global convective electric field
- ULF pulsation (Pc5)
- Electric field penetration

• Magnetometer Network : MAGDAS/CPMN,210MM Antarctica Network



- ionospheric current / ring current.
- ULF pulsation (Pc5).
- EMIC (Pc1).
- diagnostics of plasmasphere

• VLF Network : Canada, Antarctica

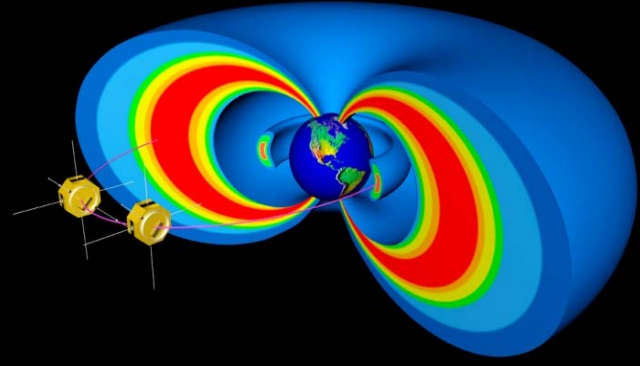


- whistler (chorus, hiss).

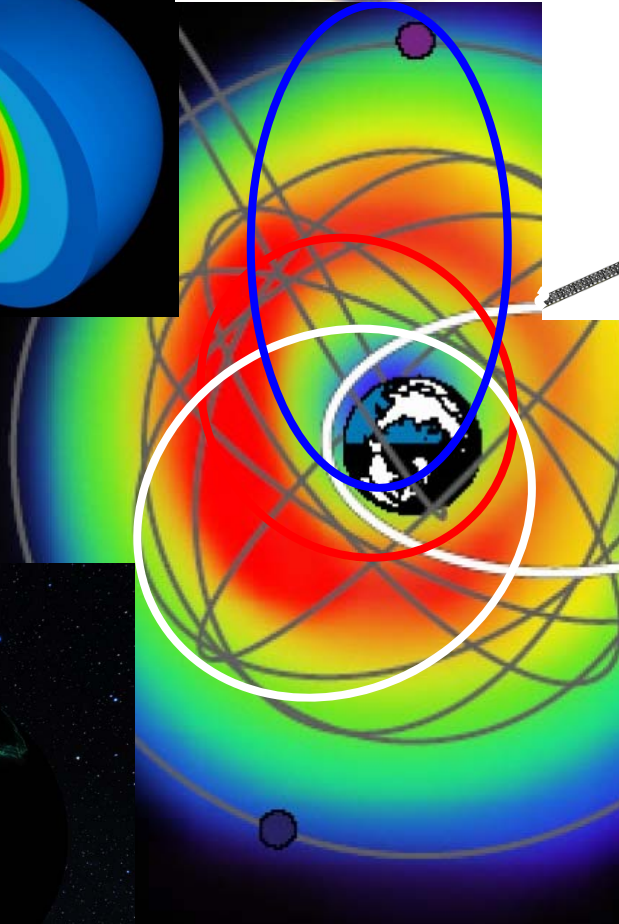
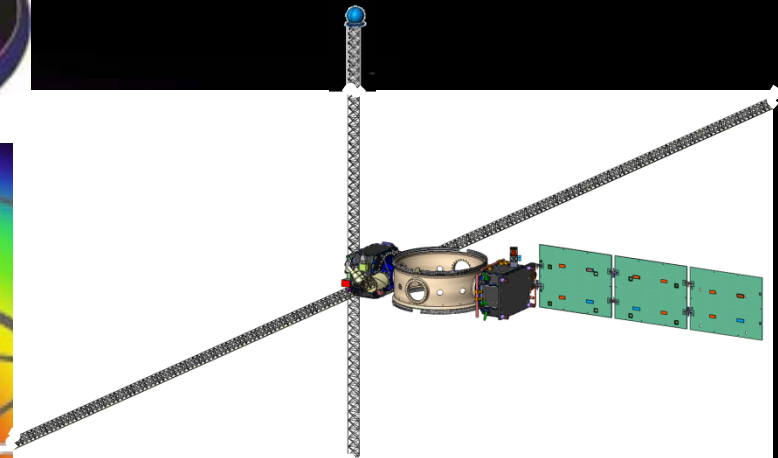
3. International Collaboration: A golden era for geospace

US/THEMIS

US/Van Allen Probes



US/DSX



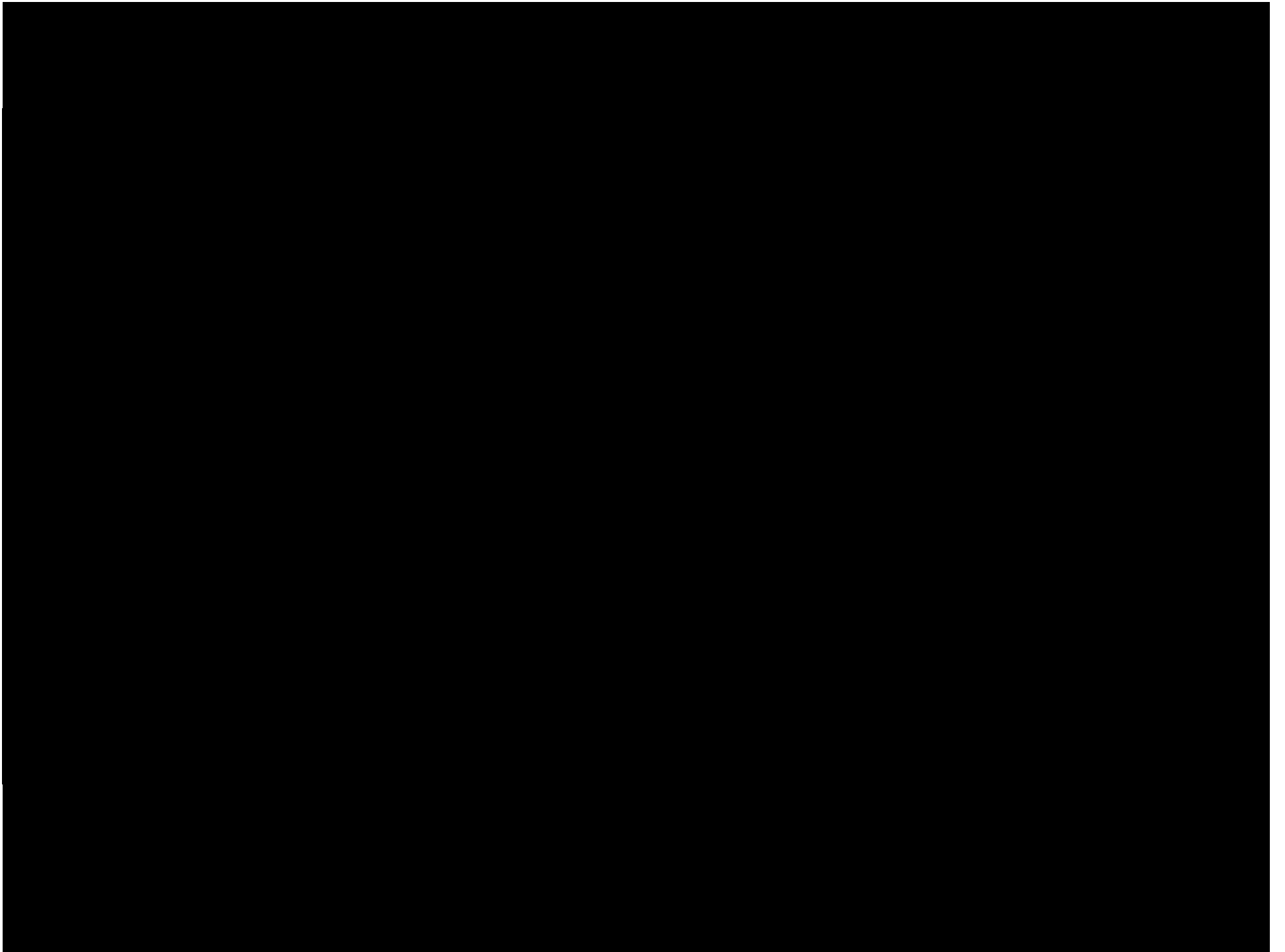
Japan/*ERG*



Russia/*RESONANCE*



Low-altitude satellites
Ground-based observations



レポート課題

MHDシミュレーションと粒子シミュレーションの本質的な違いについて簡単に述べよ。